HDO measurements with MIPAS

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Received: 8 December 2006 – Published in Atmos. Chem. Phys. Discuss.: 19 January 2007
Revised: 24 April 2007 – Accepted: 8 May 2007 – Published: 16 May 2007

Abstract. We have used high spectral resolution spectroscopic measurements from the MIPAS instrument on the Envisat satellite to simultaneously retrieve vertical profiles of H2O and HDO in the stratosphere and uppermost troposphere. Variations in the deuterium content of water are expressed in the common δ notation, where δD is the deviation of the Deuterium/Hydrogen ratio in a sample from a standard isotope ratio. A thorough error analysis of the retrievals confirms that reliable δD data can be obtained up to an altitude of ∼45 km. Averaging over multiple orbits and thus over longitudes further reduces the random part of the error. The absolute total error of averaged δD is between 36‰ and 111‰. With values lower than 42‰ the total random error is significantly smaller than the natural variability of δD. The data compare well with previous investigations. The MIPAS measurements now provide a unique global data set of high-quality δD data that will provide novel insight into the stratospheric water cycle.

1 Introduction

Water is the most important trace species in Earth’s atmosphere and heavily influences the radiative balance of the planet. In the stratosphere, it is the main substrate from which polar stratospheric clouds are formed and thus a key contributor to polar stratospheric chemistry. Therefore, a possible significant increase in stratospheric water vapor as inferred from a combination of several observational series in the past is of concern (Rosenlof et al., 2001). However, the processes that control the input of water into the stratosphere are still under debate, and even the reliability of the reported water trend has been questioned (Füglistaler and Haynes, 2005).

Isotope measurements may have the potential to distinguish between different pathways of dehydration, in particular the “gradual dehydration” mechanism (Holton and Gettelmann, 2001) and the “convective overshooting” theory (Sherwood and Dessler, 2000). In addition, ice lofting has been recognized as an important process which causes water vapor in the lower stratosphere to be less depleted in the heavy isotopes than expected from a pure gas phase distillation process, where the heavy isotopologues are removed preferentially in a one-step condensation process (Moyer et al., 1996; Smith et al., 2006; Dessler and Sherwood, 2003). At least on small spatial scales these processes could be clearly distinguished by their deuterium signatures in recent in situ measurements in the tropical tropopause region (Webster and Heymsfield, 2003). In the stratosphere, oxidation of methane produces water that is significantly enriched relative to the water imported from the troposphere and thus leads to a gradual isotope enrichment (Moyer et al., 1996; Johnson et al., 2001a; Zahn et al., 2006).

As water isotope data can provide important new insight into many of the large scale transport processes in the UT/LS region a global set of high accuracy data would be particularly valuable. In previous studies of water isotopes in the UT/LS (upper troposphere/lower stratosphere) region space borne (e.g. ATMOS (Rinsland et al., 1991; Irion et al., 1996), sub-millimeter receiver SMR (Lautie et al., 2003), balloon borne (e.g. mid-infrared limb sounding spectrometer MIPAS-B (Fischer, 1993; Stowasser et al., 1999), far infrared spectrometer FIRS-2 (Johnson et al., 2001a,b)), airborne instruments (Webster and Heymsfield, 2003; Coffey et al., 2006) and sampling techniques (Pollock et al., 1980; Zahn et al., 1998; Zahn, 2001; Franz and Röckmann, 2005) have been used. The results obtained in these studies provide a solid basis for advanced analysis. However, most of these measurements do not provide long term global data sets of isotopologues and thus do not allow to study seasonal effects. Further, some of the (space borne) measurements do

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Table 1. Microwindows used in the HDO measurements of MIPAS.

<table>
<thead>
<tr>
<th>Microwindow</th>
<th>Left border [cm⁻¹]</th>
<th>Right border [cm⁻¹]</th>
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</thead>
<tbody>
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<td>1</td>
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<td>1253.1750</td>
</tr>
<tr>
<td>2</td>
<td>1272.9000</td>
<td>1273.7000</td>
</tr>
<tr>
<td>3</td>
<td>1286.5000</td>
<td>1288.1750</td>
</tr>
<tr>
<td>4</td>
<td>1358.2250</td>
<td>1361.0500</td>
</tr>
<tr>
<td>5</td>
<td>1364.5750</td>
<td>1365.9250</td>
</tr>
<tr>
<td>6</td>
<td>1370.7500</td>
<td>1373.1500</td>
</tr>
<tr>
<td>7</td>
<td>1410.4250</td>
<td>1413.4000</td>
</tr>
<tr>
<td>8</td>
<td>1421.0500</td>
<td>1424.0250</td>
</tr>
<tr>
<td>9</td>
<td>1424.1750</td>
<td>1427.1500</td>
</tr>
<tr>
<td>10</td>
<td>1432.9500</td>
<td>1435.9250</td>
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<tr>
<td>11</td>
<td>1449.6250</td>
<td>1452.6000</td>
</tr>
<tr>
<td>12</td>
<td>1452.8500</td>
<td>1455.2000</td>
</tr>
<tr>
<td>13</td>
<td>1467.6750</td>
<td>1470.6250</td>
</tr>
<tr>
<td>14</td>
<td>1479.4750</td>
<td>1482.4500</td>
</tr>
</tbody>
</table>

not penetrate the atmosphere deep enough to study processes at the tropopause and on the other side air borne measurements often do not reach far into the stratosphere. A continuous, global observation of the stratosphere and uppermost troposphere carried out by an instrument with high spectral resolution can provide a wealth of new information. In this paper we prove the feasibility of global space-borne HDO measurements with the Michelson Interferometer for Passive Atmospheric Sounding (MIPAS, Fischer et al. (2000)).

2 MIPAS

Space borne limb sounding instruments yield a sufficiently high vertical resolution to retrieve atmospheric profiles of trace species. Possibly the best suited instrument at present for stratospheric isotope research from space is MIPAS. MIPAS is a Fourier transform interferometer with a spectral resolution of 0.05 cm⁻¹ (apodized with Norton-Beer “strong” apodization function; 0.035 cm⁻¹ unapodized) designed to study the chemistry of the middle atmosphere detecting trace gases in the mid-infrared (4–15 µm). The spectral resolution is given as the full width half maximum (fwhm) of the instrument line shapes. It is flown on Envisat (Environmetal Satellite) on a sun-synchronous orbit (98° inclination, 101 min orbit period, 800 km orbit height). MIPAS scans the Earth limb in backward-looking viewing geometry. A complete vertical scan in the original nominal measurement mode from the top to the bottom of the atmosphere is made up of up to 17 spectral measurements (“sweeps”) at 6,9,12...,42, 47, 52, 60 and 68 km. The vertical step width between the sweeps is 3 km at lower heights and increases in the upper stratosphere.

3 Retrieval of HDO and H₂O

3.1 Theory

The processing software used to retrieve vertical HDO and H₂O profiles from spectral measurements has been described by von Clarmann et al. (2003), where a constrained non-linear least squares approach is used. All variables related to one limb scan are fitted simultaneously as suggested by Carlotti (1988). By using Tikhonov-type regularization (Tikhonov, 1963) smoothness of the profiles is the applied constraint. We use a first order difference operator. The radiative transfer through the atmosphere is modeled by the Karlsruhe Optimized and Precise Radiative Transfer Algorithm, KOPRA (Stiller, 2000). Spectroscopic data is taken from a special compilation of the HITRAN 2000 data base (Rothman et al., 2003) including a number of recent updates (Flaud et al., 2003). We use the microwindow approach to select relevant spectral regions for our observations. The definition of microwindows is done following an algorithm described by von Clarmann et al. (2003). This leads to the set of microwindows we use, shown in Table 1. An altitude dependent microwindow selection was performed using a procedure suggested by Echle et al. (2000). A final optimization was done by visual inspection of resulting modeled spectra with respect to cross influences of different species.

The scientific use of the isotope data lies in the comparison of changes in HDO to changes in H₂O, thus the ratio of the two species. Inferring a ratio of two species makes it advantageous that the retrieved profiles of which the ratio is calculated, have the same height resolutions in order to avoid the introduction of artifacts. The height resolution in the present study is computed from the full width at half maximum of the columns of the averaging kernel A (Rodgers, 2000)

\[ \mathbf{A} = \mathbf{GK} \]  

\( \mathbf{K} \) is a weighting function (Jacobian) which contains the sensitivities of the spectral measurement to changes in related quantities, i.e. temperature, pressure. \( \mathbf{G} \) is a gain matrix. In our retrieval approach \( \mathbf{G} \) is

\[ \mathbf{G} = (\mathbf{K}^T \mathbf{S}_y^{-1} \mathbf{K} + \mathbf{R})^{-1} \mathbf{K}^T \mathbf{S}_y^{-1} \]  

\( \mathbf{R} \) is a regularization matrix which constrains the retrieval and \( \mathbf{S}_y \) is the covariance matrix of the measurement noise error. In our implementation a priori information is solely used to constrain the shape of the profile, not the abundances.

While a water vapor data set retrieved from MIPAS is already available (Milz et al., 2005; Raspollini et al., 2006) we have decided to jointly retrieve the volume mixing ratio (vmr) of HDO and H₂O. The joint retrieval of H₂O and HDO helps to minimize mutual error propagation. As a priori knowledge we use 4 seasonal sets of water profiles divided in 6 latitude bands (tropics 0° to 30° N/S, mid latitudes 30° to 65° N/S and high latitudes 65° to 90° N/S) from the data set compiled by Remedios (1999). These profiles are also used
as first guess profiles to start the iterative calculation process. The a priori for HDO is computed from these profiles by applying a height independent fractionation profile with values taken from the HITRAN data base (Rothman et al., 2003). Together with HDO and H₂O we also retrieve HNO₃, CH₄ and N₂O to capture the influence these species have in the error calculation for the retrieval. Initial guess profiles (profiles needed to start the iterative calculation scheme) for HNO₃, CH₄, N₂O were taken from previous analysis of the measurement under investigation. Additionally, background continuum radiation and radiance calibration offset are retrieved (see von Clarmann et al. (2003) for details). The actual temperature profile also was taken from previous MIPAS retrievals, while climatological abundance profiles are used for other interfering species, except for O₃ and N₂O₅ where we also use previously retrieved profiles. For retrieval, we use spectral measurements from tangent altitudes between 12 and 68 km. The actual tangent heights in km on which the spectral measurements for the representative profiles used in this work (13 January 2003 at 12°N and 28°W) were carried out, are: 12.1, 15.1, 17.9, 20.8, 23.8, 26.8, 29.8, 32.3, 35.4, 38.4, 41.3, 46.3, 51.3, 59.4 and 67.4 km. However, the profiles in this paper are presented only in the height range from 11 km to 45 km. In this height region we considered the measurements to be of sufficient quality (i.e. with respect to cloud interference or signal to noise ratio) to match the requirements for studying isotope variability.

3.2 HDO and H₂O profiles

In this paper, a thorough error analysis is carried out for a pair of representative H₂O and HDO profiles. Figure 1a shows the corresponding profile of water vapor. In this context that means total water, including all isotopologues. Figure 2a shows the corresponding HDO profile from the same set of measurements. The height resolution of both profiles is between 6 km (at 10 km) and 8 km (at 45 km) as shown in Figs. 3c and d. The height resolution becomes worse with higher altitudes, due to the coarser measurement grid and the decreasing signal to noise ratio. The fact that both species are retrieved with the same vertical resolution is important when calculating the isotopic composition (see Sect. 5.2.3), and it is reflected by the nearly identical averaging kernels (Fig. 3a and b). Matching averaging kernels are achieved by appropriate choice of the respective $R$-matrix in the joint retrieval of HDO and H₂O.

4 Error assessment

Following Rodgers (2000), the covariance matrix $S_i$ of the total error of a retrieved profile is characterized by

$$S_i = S_n + S_p + S_s$$

where $S_n$ is the covariance matrix of the noise error (i.e. measurement noise), $S_p$ represents the covariance of the parameter error (i.e. instrumental effects, forward modeling errors) and $S_s$ is the covariance matrix of the smoothing error. To assess and quantify the total error of our results it is necessary to discuss the covariance matrices and the related errors in the following sections in more detail.

4.1 Noise error

The random error due to measurement noise is calculated as

$$S_n = G S_y G^T.$$  (4)

Figures 2 and 1 show that the noise error is considerably more important for HDO than for H₂O, which is expected due to the much lower abundance of HDO and the decreasing signal to noise ratio. Whereas the noise error is always
4.2 Parameter error

We compute the profile errors $\sigma_p$ due to parameter uncertainties $\Delta b$ as

$$\sigma_p = G K_b \Delta b$$  \hspace{1cm} (5)

$K_b$ is the sensitivity of the measurements to parameter errors. For the current study the total parameter error is composed of 23 different components. The computation is done independently for the 23 contributions from additional atmospheric constituents (listed below). The four major categories of parameter errors are

- Influence of $1\sigma$ uncertainties in the abundance of interfering species on the retrieval targets. The following gases are considered $\mathrm{SO}_2$, $\mathrm{CO}_2$, $\mathrm{O}_3$, $\mathrm{NO}_2$, $\mathrm{NH}_3$, $\mathrm{OCS}$, $\mathrm{HOCl}$, $\mathrm{HCN}$, $\mathrm{H}_2\mathrm{O}_2$, $\mathrm{C}_2\mathrm{H}_2$, $\mathrm{COF}_2$, $\mathrm{CFC}-11$, $\mathrm{CFC}-12$, $\mathrm{CFC}-14$, and $\mathrm{N}_2\mathrm{O}_5$.

- Uncertainties ($1\sigma$) due to temperature (tem) and horizontal temperature gradients (tgra). These uncertainties are in approximation considered random in time but are fully correlated in altitude.

- Uncertainties ($1\sigma$) of the instrument characterization: line of sight (los), spectral shift (shift), gain calibration (gain), instrumental line shape (ils). These systematic uncertainties are considered correlated for all species.

- Uncertainties of line intensities and pressure broadening ($1\sigma$ of the fwhm of the lines) in the HITRAN database for HDO and $\mathrm{H}_2\mathrm{O}$ (hitmid). These uncertainties play an important role in the error budget, especially for the error budget of the ratio of HDO and $\mathrm{H}_2\mathrm{O}$. The reason is that these uncertainties are of a systematic nature but the line strength and line intensity uncertainties of HDO and $\mathrm{H}_2\mathrm{O}$ are not correlated. This may be over pessimistic, but due to this these uncertainties will not cancel out when creating a ratio nor are they reduced when averaging.

Table 2 shows the assumed $1\sigma$ parameter uncertainties for the most prominent error sources. Each of the following parameters has a share of the total parameter error of at least 1%: $\mathrm{SO}_2$, temperature and its horizontal gradient, spectroscopic data uncertainty, line-of-sight uncertainty, spectral shift, gain calibration uncertainty and residual instrumental line shape error. Figures 4a and b show the contribution of the major parameter errors to the total parameter error for HDO and $\mathrm{H}_2\mathrm{O}$ respectively. The strongest influence on the parameter error in both cases is due to uncertainties in spectroscopic data when looking at altitudes above 17 km. At lower altitudes the random parts of the parameter error are bigger.

The total parameter error for the HDO profile is between 0.10 and 3 ppb (parts per billion, $10^{-9}$) for altitudes between

<table>
<thead>
<tr>
<th>perturbed quantity</th>
<th>value and unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\mathrm{SO}_2$</td>
<td>10–37 km: $10^{-3}$ ppm, above 37 km $10^{-5}$ ppm</td>
</tr>
<tr>
<td>$T$</td>
<td>2 K (constant over height)</td>
</tr>
<tr>
<td>Hor. T gradient (lat)</td>
<td>0.01 K/km (constant over height)</td>
</tr>
<tr>
<td>ils</td>
<td>3% at 600 and 1600 cm$^{-1}$</td>
</tr>
<tr>
<td>los</td>
<td>0.15 km</td>
</tr>
<tr>
<td>spectral shift</td>
<td>0.0005 cm$^{-1}$</td>
</tr>
<tr>
<td>gain</td>
<td>1%</td>
</tr>
</tbody>
</table>

- Influence of $1\sigma$ uncertainties in the abundance of interfering species on the retrieval targets. The following gases are considered $\mathrm{SO}_2$, $\mathrm{CO}_2$, $\mathrm{O}_3$, $\mathrm{NO}_2$, $\mathrm{NH}_3$, $\mathrm{OCS}$, $\mathrm{HOCl}$, $\mathrm{HCN}$, $\mathrm{H}_2\mathrm{O}_2$, $\mathrm{C}_2\mathrm{H}_2$, $\mathrm{COF}_2$, $\mathrm{CFC}-11$, $\mathrm{CFC}-12$, $\mathrm{CFC}-14$, and $\mathrm{N}_2\mathrm{O}_5$.

- Uncertainties ($1\sigma$) due to temperature (tem) and horizontal temperature gradients (tgra). These uncertainties are in approximation considered random in time but are fully correlated in altitude.

- Uncertainties ($1\sigma$) of the instrument characterization: line of sight (los), spectral shift (shift), gain calibration (gain), instrumental line shape (ils). These systematic uncertainties are considered correlated for all species.

- Uncertainties of line intensities and pressure broadening ($1\sigma$ of the fwhm of the lines) in the HITRAN database for HDO and $\mathrm{H}_2\mathrm{O}$ (hitmid). These uncertainties play an important role in the error budget, especially for the error budget of the ratio of HDO and $\mathrm{H}_2\mathrm{O}$. The reason is that these uncertainties are of a systematic nature but the line strength and line intensity uncertainties of HDO and $\mathrm{H}_2\mathrm{O}$ are not correlated. This may be over pessimistic, but due to this these uncertainties will not cancel out when creating a ratio nor are they reduced when averaging.
10 and 45 km (Fig. 2a). At most altitudes it is approximately 0.10 ppb. For H₂O, parameter errors are the dominating error source compared to the noise error (Fig. 1a). They are in the range between 0.5 to 5 ppm (parts per million) for a single profile (the latter in the troposphere only). The contribution from SO₂ may be over pessimistic because it is based on assumptions on the amount of SO₂ in the atmosphere which were made before Envisat was launched.

4.3 Smoothing error

The smoothing error $S_\text{s}$ is introduced by the limited capability of an instrument to resolve fine structures. To calculate the smoothing error it would be necessary to evaluate

$$S_\text{s} = (\mathbf{A} - \mathbf{I})\mathbf{S}_\text{e}(\mathbf{A} - \mathbf{I})^T$$

with $\mathbf{I}$ being the unity matrix. As we do not accurately know the variability of the true atmospheric state (represented by matrix $\mathbf{S}_\text{e}$) we are not able to statistically evaluate the smoothing error. Instead, the effect of smoothing
is addressed in our sensitivity study (see Sect. 5.2.4), where we show that an artificially introduced sharp disturbance is smoothed out over a region that corresponds to the width of the averaging kernels (Fig. 3a).

4.4 Total error

The total error variance $\sigma_{t,i}^2$ at altitude $i$ is calculated as

$$\sigma_{t,i}^2 = (S_l)_{i,i} = (S_n)_{i,i} + \sum \sigma_{p,i}^2.$$  (7)

Figure 2 shows the total error for a typical HDO profile (red line). The total error lies between 3.30 ppb at 11 km (6 km height resolution) and 0.16 ppb at 23 km (6–7 km height resolution). At most altitudes above 23 km it does not exceed 0.30 ppb. Figure 1 shows the total error for H$_2$O. The total error is between 5.20 ppm at 11 km (6 km height resolution) and 0.5 ppm above 38 km (7–8 km height resolution) when spectroscopic uncertainties are taken into account. The total random error for single profiles (total error without spectroscopic error contribution) improves above 17 km because there the parameter error is dominated by spectroscopic uncertainties rather than by random components (Fig. 4). The total random error for a single HDO profile is between 3.30 ppb at 11 km and 0.15 ppb at 22 km. For H$_2$O the range is 4.79 ppm (11 km) to 0.20 ppm (37 km).

At most of the altitudes it is approximately 0.20 ppm. The reduction of the random error with altitude is stronger for the H$_2$O profiles, because the HDO measurements carry more noise. We note that the errors reported here are not the limit for the conventional retrieval of H$_2$O, but the precision is artificially reduced due to the chosen altitude resolution. Dedicated water retrievals achieve better results (Milz et al., 2005).

5 Isotope fractionation

5.1 From HDO measurements to $\delta$D values

The target quantity for isotope assessment is the heavy-to-light isotopic ratio $R$ of a sample. In our case $R=[D]/[H]$. The brackets indicate that we refer to vmr. For quantifying heavy isotope abundances, this ratio is usually compared to a standard ratio in the common $\delta$ notation

$$\delta D = \left( \frac{R}{R_{VSMOW}} - 1 \right) \times 1000 \text{‰}.$$  (8)

where VSMOW stands for the international standard material Vienna Standard Mean Ocean Water ($R_{VSMOW}=155.76 \times 10^{-6}$). Rather than the atomic D/H ratio, our optical measurements return the molecular abun-
dances of HDO and H$_2$O. A modified $\delta$ value can be defined for the molecular ratio $R_{\text{HDO}}^{\text{HDO}}$=[HDO]/[H$_2$O] as

$$\delta_{\text{HDO}}= (\frac{R_{\text{HDO}}^{\text{HDO}}}{R_{\text{VSMOW}}^{\text{HDO}}}) - 1) \times 1000$$ (9)

but in practice these molecular $\delta$ values are very similar to the atomic values. As the abundance of double deuterated water molecules is negligible small and the fraction H in HDO relative to H$_2$O is also negligible for our purposes, we can approximate

$$\begin{bmatrix} \delta \text{HDO} \\ \delta \text{H}_2 \text{O} \end{bmatrix} \approx \begin{bmatrix} [\text{HDO}] \\ 2[\text{H}_2\text{O}] + [\text{HDO}] \end{bmatrix} \approx \begin{bmatrix} [\text{HDO}] \\ 2[\text{H}_2\text{O}] \end{bmatrix}$$ (10)

Because of its low abundance in the order of ppb, HDO is a highly challenging target for remote sensing systems and it is mandatory to closely look at the accuracy of the final data. Thus, it is necessary to provide error estimates for the individual species as well as for $\delta$. A ratio profile $q_{\text{HDO}}^{\text{HDO}}$ is a vector of the shape

$$q_{\text{HDO}}^{\text{HDO}} = \left[ \frac{[\text{HDO}]}{[\text{H}_2\text{O}]}_1, ..., \frac{[\text{HDO}]}{[\text{H}_2\text{O}]}_i, ..., \frac{[\text{HDO}]}{[\text{H}_2\text{O}]}_n \right]^T.$$ (11)

where the subscripts indicate altitudes. Using Eq. (9) and $\delta \text{D} \approx \delta \text{HDO}$, this can be rewritten in terms of $\delta$ values, since

$$\begin{bmatrix} [\text{HDO}] \\ [\text{H}_2\text{O}] \end{bmatrix} \approx R_{\text{VSMOW}}^{\text{HDO}}(\delta \text{D} + 1) \approx 311.5 \times 10^{-6} (\delta \text{D} + 1)$$ (12)

Thus, our measurements can easily be translated to common isotope notation and a profile of $\delta_i$D values is derived. Figure 5a shows a typical $\delta$D profile inferred from the above described HDO and H$_2$O measurements at 12° N. The minimum (~800‰) is at ≈19 km which is close to the expected entry value of ~650‰ (Moyer et al., 1996) when the total error is taken into account. Above the minimum, $\delta$ D values increase with altitude.

5.2 Errors and their propagation in $\delta$D

Attempting to detect the natural variability in stratospheric $\delta$D requires the assessment of the precision of the single HDO and H$_2$O profiles. The resulting precision for the $\delta$D values has to be inferred from the combined errors of the H$_2$O and HDO profiles. Linear error analysis requires linearization of the ratio term in Eq. (9). The dependence of $\delta_i$D on [HDO]$_i$ is ($f=3.2 \times 10^{6} \approx 1000 \times 2 \times \frac{1}{R_{\text{VSMOW}}^{\text{HDO}}}$)

$$(J_{\text{HDO}, \text{HDO}})_{i,i} = f \times \frac{\partial [\delta \text{D}]_i}{\partial [\text{HDO}]_i} = f \times \frac{1}{[\text{H}_2\text{O}]_i},$$ (13)

and the dependence of $\delta$ D on [H$_2$O]$_i$ is

$$(J_{\text{HDO}, \text{H}_2\text{O}})_{i,i} = f \times \frac{\partial [\delta \text{D}]_i}{\partial [\text{H}_2\text{O}]_i} = f \times \frac{-[\text{HDO}]_i}{[\text{H}_2\text{O}]_i^2},$$ (14)

The linearization around the retrieved profile $x$ in matrix notation then yields

$$(\delta_{1D}, ..., \delta_{nD})^T = Jx - c = (J_{\text{HDO}}, -J_{\text{H}_2\text{O}}) \times (x_{\text{HDO}}, x_{\text{H}_2\text{O}})^T - c,$$ (15)

where $J_{\text{HDO}}$ is a diagonal matrix with $(J_{\text{HDO}, \text{HDO}})_{i,i}$ along the diagonal, and $J_{\text{H}_2\text{O}}$ with $(J_{\text{HDO}, \text{H}_2\text{O}})_{i,i}$, respectively. $(x_{\text{HDO}}, x_{\text{H}_2\text{O}})^T$ is the profile vector composed of the profile values [HDO]$_i$ and [H$_2$O]$_i$. $c$ is a vector with $n$ elements where each element has a constant value, $c_1=1000$. With the linearization of the ratio available in matrix notation, the error covariance matrix of the $\delta$D profile can be written as

$$S_{\delta D} = JSxJ^T,$$ (16)
5.2.1 Noise error for $\delta D$

With the noise retrieval error covariance matrix $S_n$ available for $(x_{HDO}^T, x_{H_2O}^T)$, the evaluation of the noise error of $\delta D$ with Eq. (18) is straightforward. Single profile $\delta D$ noise errors are reported in Fig. 5a. In the error propagation the noise error of the ratio is dominated by the product of the noise error of [HDO] with [H$_2$O]. This term is at least one magnitude larger than the other terms. That implies that the noise error of the ratio is dominated by the noise error of HDO, i.e. the relative noise error of HDO maps directly onto the $\delta D$ profile. Figure 5a shows the contribution of the noise error to the error budget for a single $\delta D$ profile. The values lie between 15%$_e$ (11 km) and 112%$_e$ (43 km). At most heights we find values of approximately 90%$_e$.

5.2.2 Parameter error for $\delta D$

The contributions of the parameter errors without spectroscopic errors to the error budgets of HDO and H$_2$O are notable (see Figs. 2a and 1a). The positively correlated parts of the parameter errors, i.e. the portion that is not hitmid, of HDO and H$_2$O show a tendency to cancel out when creating the ratio ($r\approx1$ in Eq. (18)). Thus, the parameter errors of $\delta D$ reduce relatively compared to HDO and H$_2$O. The total parameter error for $\delta D$ is dominated by the spectroscopic uncertainties in HDO and H$_2$O. Figure 5a shows that the total parameter error is the main error source for the single $\delta D$ profiles with values between 46%$_e$ (18 km) and 188%$_e$ (14 km). Above 18 km we mostly find values lower than 100%$_e$.

5.2.3 Smoothing error for $\delta D$

As outlined in Sect. 4.3, the smoothing error can only be evaluated if a true climatological covariance matrix of the target quantity is known. While the smoothing error caused by the limited altitude resolution often is sufficiently characterized by reporting the altitude resolution of the profile, artifacts in the profile of ratios are a major concern when the two quantities are retrieved with different altitude resolutions.

There are several options to solve or bypass this problem. Ratio profiles can be retrieved directly instead of dividing retrieved mixing ratios (Schneider et al., 2006; Payne et al., 2004). The smoothing error can also be evaluated explicitly using a climatological covariance matrix estimated by the help of a model (Worden et al., 2005).

We have chosen another approach, which is to calculate the ratio of two profiles of nearly the same altitude resolution in order to avoid artifacts in the ratio profile. Using profiles with similar averaging kernels allows us to calculate the ratios without the risk of artifacts and the altitude resolution of the resulting ratio profile is close to equal to that of the original HDO and H$_2$O profiles. This is sufficiently valid for altitudes between 11 and 45 km (Figs. 3c and d).

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Fig. 6. H$_2$O input profile for sensitivity study. We introduced artificial spikes of +20% at 14, 17 and 25 km altitude either only to the total water profile (all isotopologues) or to all water isotopologues but HDO (dashed line). The solid line shows the undisturbed water input profile.

where $S_X$ is the combined covariance matrix of HDO and H$_2$O

$$S_X = \begin{pmatrix} S_{HDO} & C_{HDO,H_2O}^T \\ C_{HDO,H_2O} & S_{H_2O} \end{pmatrix}$$

(17)

The sub-matrix $C$ contains the related covariances between HDO and H$_2$O. This formulation holds for all types of errors (noise, parameter and smoothing). For the standard deviation $\sigma_{i,\delta D}$ at altitude level $i$ Eq. (16) gives

$$\sigma_{i,\delta D} = f \times \frac{1}{[H_2O]_i^2} \times ([HDO]_i^2\sigma_{i,H_2O}^2 + [H_2O]_i^2\sigma_{i,HDO}^2 + 2r_{HDO,H_2O}\sigma_{i,HDO}\sigma_{i,H_2O}[HDO]_i \times [H_2O]_i)^{1/2},$$

where $r$ is the correlation coefficient of the errors of HDO and H$_2$O at altitude $i$. 
5.2.4 Sensitivity study

To check the validity of the underlying assumptions and approximations, two sensitivity tests were carried out with simulated profiles. As reference profile we used a typical tropical H$_2$O profile as shown in Fig. 6 and a corresponding HDO profile that had the isotopic composition of the VSMOW, thus an enrichment of 0‰. The corresponding retrieval result is shown in Fig. 7, which shows that for this single profile retrieval we obtain a resulting profile with an average δD value of ~2‰ (thus very close to 0‰) and moderate oscillations smaller than 20‰ in the lower stratosphere.

In the first sensitivity test we then added 3 sharp positive 20% perturbations at 14, 17 and 25 km (see Fig. 6) on the total water vapor profile, i.e., for all isotopologues, to the atmosphere used to generate synthetic observations. The retrieval reproduced the higher total water content due to these spikes, but strongly smoothed out the spikes according to the limited altitude resolution (not shown). The isotopic fractionation, however, changed by less than 10‰ (Fig. 7). This result confirms that no significant artifacts in the isotopic fractionation profiles due to smoothing error propagation are to be expected and that the strategy to use equally resolved profiles for ratio calculation is sufficiently robust. This is particularly remarkable considering the fact that the 20% perturbations applied are large compared to natural total water variations and the 10‰ response of inferred δD values is much smaller than the expected and observed δD variations.

In the second sensitivity study we applied the retrieval to perturbations as described above to all water isotopologues except HDO. This implies that the input signal was isotopically strongly depleted at the height levels of the disturbances where 20% more H$_2^{18}$O was artificially added (Fig. 6). The resulting δD profiles (Fig. 7) show a clear response to this perturbation. However, as expected the perturbation is smoothed out according to the actual altitude resolution of the retrieved HDO and H$_2$O profiles. In fact, the two peaks at 14 and 17 km altitude cannot be resolved with our altitude resolution and are retrieved as one broad structure. On average δD values are decreased by ~−50‰, which reflects the smoothing of the input of ~−200‰ H$_2^{18}$O. On the tail of this broad structure we see the response to the second perturbation at 25 km altitude, which is clearly resolved by the retrieval. Over the altitude range 10 to 30 km where we observe a response to the perturbation, the average enrichment is ~−35‰. This integrated response compares well with the input signal, where H$_2^{18}$O was disturbed by ~−200‰ at 3 out of 21 altitude levels, which corresponds to an average perturbation of ~−29‰.

5.3 Total error of δD-Profiles

Figure 5a shows the representative δD profile and the associated errors. At first we note the important contribution of the parameter error: In the HDO and H$_2$O case the parameter error had a share of ~20 to 30%. In the δD case this is very similar which is a consequence of the strong influence of the uncorrelated spectroscopic errors of HDO and H$_2$O. Thus, we obtain a height dependent total parameter error profile with values between 46 and 188‰. The noise error has a magnitude of 15 to 112‰. Together this leads to a height dependent total error for a single δD profile in the range between 80‰ (11 km) and 195‰ (14 km). Most values are between 90 and 145‰.

6 Averaging

Envisat performs 14 orbits per day. As longitudinal variability in the stratosphere is generally much smaller than latitudinal variability, we have averaged all H$_2$O and HDO measurements by longitude and calculated daily δD profiles. At each altitude level $i$ the random error of the average, i.e., the noise error and random parts of the parameter error, is reduced by a factor of $1/\sqrt{N_i}$, where $N_i$ is the number of profile values...
at altitude \( i \) which were actually used for averaging. The retrieval algorithm identifies problematic measurements, e.g., measurements affected by clouds, and excludes them from the ongoing calculation. This leads to the altitude dependence of \( N_i \) as shown in Table 3.

From Figs. 2b and 1b the estimated reduction of the total error due to averaging is visible for the representative individual HDO and \( \text{H}_2\text{O} \) profiles. In the lower stratosphere below 20 km random errors dominate the error budget for both species and averaging leads to a strong improvement in the total error. In the case of \( \text{H}_2\text{O} \), above 20 km the parameter error components dominate the error profile and averaging leads to marginal improvement of the total error only. For HDO, the random errors are still the most important part of the error in this region, and the total error is strongly reduced by the averaging. After averaging, the total random errors are only dominating below 15 km, thus further averaging will not significantly reduce the errors at higher altitudes. Here the improvement of the spectroscopic uncertainty portion of the parameter error is the key to improving the total error.

The theoretically derived errors as estimated above (“estimated errors”) are compared to the actually derived variability of averaged HDO and \( \text{H}_2\text{O} \) profiles, quantified in terms of the standard deviation of the ensemble

\[
\sigma_{\text{ens},i} = \sqrt{\frac{\sum_{n=1,N_i}(x_{i,n} - \bar{x}_i)^2}{N_i - 1}}.
\]

and standard deviation of the mean

\[
\sigma_{\text{mean},i} = \frac{1}{\sqrt{N_i}} \sqrt{\frac{\sum_{n=1,N_i}(x_{i,n} - \bar{x}_i)^2}{N_i - 1}}.
\]

Table 3. Number of measurements per height step taken into account for averaging, for the measurements on 13 January 2003 between 7.5° N and 12.5° N.

<table>
<thead>
<tr>
<th>Altitude(s) [km]</th>
<th>Number of measurements</th>
</tr>
</thead>
<tbody>
<tr>
<td>11</td>
<td>9</td>
</tr>
<tr>
<td>12</td>
<td>9</td>
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<tr>
<td>13</td>
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</tr>
<tr>
<td>19</td>
<td>26</td>
</tr>
<tr>
<td>20–44</td>
<td>28</td>
</tr>
</tbody>
</table>

The theoretically derived errors as estimated above (“estimated errors”) are compared to the actually derived variability of averaged HDO and \( \text{H}_2\text{O} \) profiles, quantified in terms of the standard deviation of the ensemble

\[
\sigma_{\text{ens},i} = \sqrt{\frac{\sum_{n=1,N_i}(x_{i,n} - \bar{x}_i)^2}{N_i - 1}}.
\]

and standard deviation of the mean

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\]


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6.1 Latitudinal and vertical distribution of \( \text{H}_2\text{O} \)

In the zonal mean, water shows the expected distribution that has been established in numerous studies carried out in the past (e.g. (Randel et al., 2001)): For 13 January 2003 we observe values >100 ppm in the troposphere, which decrease rapidly towards the tropopause (Fig. 8) due to decreasing temperatures. Values between 3 and 5 ppm are observed in the tropopause region and lower stratosphere (Fig. 8) and the minimum is located at the tropical tropopause of the winter hemisphere. A secondary minimum at around 23 km in the tropical stratosphere indicates the upward propagation of the seasonal cycle as part of the atmospheric tape recorder effect (Mote et al., 1996). In the stratosphere, \( \text{H}_2\text{O} \) levels increase again with increasing altitude and latitude up to values of about 7.5 ppm at the top of the shown height range. This shows the in situ production of \( \text{H}_2\text{O} \) from \( \text{CH}_4 \) oxidation, which increases as air ages in the stratospheric circulation. In the cold Arctic winter vortex, we observe air from higher altitudes with high water content descending into the stratosphere down to 25 km. Deviations of our averaged water profiles retrieved with limited vertical resolution from validated water retrievals of better altitude resolution (Milz et al., 2005) do generally not exceed 1 ppm when looking at annual averages. Occasionally, larger differences (up to 2 ppm) occur at the tropopause. In the present case there is such a feature at 10° S. However, close to the tropopause larger deviations are expected due to strong vertical gradients both in \( \text{H}_2\text{O} \) and HDO there. Also, the artificially reduced height resolution of our \( \text{H}_2\text{O} \) retrievals (to match the altitude resolution of HDO) compared to Milz et al. (2005) influences the quality of the results. Thus, these deviations are intrinsic to our retrieval approach.

For the day of our retrieval, the retrieved profiles suggest a sharp hygropause, particularly in the region around 65° S. Such a sharp hygropause cannot be resolved by MIPAS, and it leads to oscillations above the hygropause which produce an artificial \( \text{H}_2\text{O} \) minimum there. Those oscillations also lead to unusually high variability in this region, and indeed the standard deviation shows a pronounced maximum there. Therefore, this structure is excluded from further examination.
Fig. 8. Zonal mean distribution of H$_2$O 13 January 2003, measured by MIPAS. 9 to 28 measurements were taken into account for averaging at each altitude and latitude level (see Table 3 for details).

6.2 Latitudinal and vertical distribution of HDO

Figure 9 shows the zonal mean distribution of HDO on 13 January 2003. The general distribution of HDO, i.e., its increase above the tropopause as well as the general latitudinal shape, is similar to that of H$_2$O, which reflects the fact that both species have a common in situ source in the stratosphere i.e. oxidation of CH$_4$ and H$_2$. The HDO minimum at the northern tropical tropopause corresponds to the H$_2$O minimum with values of approximately 0.2 ppb. Corresponding to H$_2$O we observe a secondary minimum in the tropical stratosphere around 23 km also for HDO. The descent of air in the winter vortex is amplified in HDO compared to H$_2$O, because the descending water is strongly enriched in deuterium. As a general characteristic, the HDO contours are less smooth than those of H$_2$O. As noted for H$_2$O, the HDO minimum at 60–70° S and 13 km altitude is caused by the sharp retrieved hygropause and is not statistically significant. The standard deviation of the negative HDO values reach up to 250% in this region. This negative artifact causes a positive compensating feature in the layer above at 15–17 km altitude.

6.3 Latitudinal and vertical distribution of δD

The δD value quantifies the ratio of HDO and H$_2$O and it therefore highlights the differences in the general behavior of the two species. If changes in HDO perfectly mirrored changes in H$_2$O in the stratosphere, Fig. 10 would show constant values throughout the stratosphere. However, we observe an increase in δD with altitude above the tropopause and with latitude, thus as water increases it also gets isotopically enriched. This shows directly that H$_2$O derived from the oxidation of CH$_4$ and H$_2$ is isotopically enriched relative to the H$_2$O that is injected from the troposphere, in agreement with the expectations and with results from earlier measurement and model results (Moyer et al., 1996; Zahn et al., 2006; Johnson et al., 2001a; Stowasser et al., 1999; Rinsland et al., 1991). However, here for the first time we see a full two dimensional plot of δD in the stratosphere. The data indicate lower near tropopause δD values in the winter hemisphere compared to the summer hemisphere, from the tropics to the high latitudes (with the exception of the artificial structure at 60–70° S). A detailed scientific interpretation of all those structures will follow in a dedicated publication.

In this paper we have shown that the natural variations in stratospheric δD values can be clearly resolved because they are larger than the total errors derived above. As shown in Fig. 5b, the estimated total error of an averaged δD profile reduces to values between 35‰ (11 km) and 110‰ (36 km) when the noise part of the total error has been reduced by a factor of $1/\sqrt{N_i}$. Most values are around 80‰. The estimated total random error for the averaged δD profiles is below 42‰ for all heights with a minimum of 16‰ (18 km) and a maximum of 41‰ (14 km). In comparison, the natural variations recorded in the MIPAS data span several hundred ‰.

The MIPAS measurements thus provide a unique data set that will enable us to study various parts of the stratospheric water cycle in unprecedented detail. Because of the limited vertical resolution we are not able to resolve individual small scale processes (<4 km) like convective updraft that might also affect the isotopic fractionation of water in the stratosphere (Webster and Heymsfield, 2003). However, their large scale relevance may well be assessed, and for the global stratospheric water cycle, this may even be the more important information.
Fig. 9. Zonal mean distribution of HDO for 13 January 2003, measured by MIPAS, 9 to 28 measurements were taken into account for averaging at each altitude and latitude level (see Table 3 for details).

Fig. 10. Zonal mean distribution of δD, 13 January 2003, inferred from averaged HDO and H2O measurements by MIPAS.

6.3.1 Comparison to other data sets

Figure 11 shows a comparison of our MIPAS retrievals to published values from the literature (Rinsland et al., 1991; Kuang et al., 2003; Johnson et al., 2001a; Dinelli et al., 1991, 1997). The general trends in the stratosphere from the earlier studies are captured by the MIPAS data. Perfect agreement cannot be expected, because

1. our profile was actually taken in the tropics with colder tropopause temperatures compared to the Johnson et al. (2001a) data that were obtained at 33° N and the Rinsland et al. (1991) data obtained at 30° N and 47° N; The Dinelli data were taken at 32° N (Dinelli et al., 1991) and 34° N (Dinelli et al., 1997);

2. the earlier recorded profiles were obtained at different times of the year and differences could be due to a possible seasonal effect and

3. near the tropopause both HDO and H2O have strong gradients, which can potentially cause averaging problems when the vertical resolution is limited.
The MIPAS profile shows the averages from 9 to 28 measurements per altitude level (Table 3) on 13 January 2003. Note that the different data sets were obtained in different seasons and at different latitudes.

Below the tropopause, our $\delta$D values are more enriched than most of the Kuang et al. (2003) data. However, large variability in the upper troposphere was recently reported from in situ measurements (Webster and Heymsfield, 2003). Overall, the vertical structure, in particular the increase of $\delta$D with altitude above the point of minimum temperature, is in good agreement with the available data.

### 7 Conclusions

We have shown that MIPAS limb emission spectra can be used to investigate the isotopic composition of water vapor in the stratosphere on a global scale. HDO and H$_2$O profiles are retrieved in a multiple target retrieval using the microwindow approach. In order to avoid artifacts in the resulting $\delta$D profiles both HDO and H$_2$O are retrieved at the same altitude resolution. A thorough error analysis is carried out to evaluate and distinguish noise and parameter errors. In the HDO/H$_2$O ratio a considerable fraction of the parameter error cancels out, and the resulting $\delta$D profiles are dominated by spectroscopic uncertainties, resulting in a total error for single profiles of the order of 80‰ (11 km) to 195‰ (14 km) with most values between 90 and 145‰. The random component of the estimated total error can strongly be reduced by taking averages over multiple orbits on a single day. Thus, random errors are no longer limiting the measurement precision for one day averaging. The estimated total error of the averaged profiles (including spectroscopic uncertainties) is between 35‰ (11 km) and 110‰ (36 km). The random component of the total error is below 42‰ at all heights. The precision and altitude resolution of these zonal mean profiles is sufficient to study fractionation processes on a large scale, e.g., the principle role of different stratospheric dehydration mechanisms, or in situ formation from methane oxidation. Thus the MIPAS measurements will provide unique information about the stratospheric water cycle.

### Acknowledgements

This work was carried out as part of the AFO2000 project ISOSTRAT (07ATC01) funded by the German Ministry for Education and Research (BMBF). We thank ESA for access to the data.

Edited by: P. Hartogh

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