Exploring the potential of nano-Köhler theory to describe the growth of atmospheric molecular clusters by organic vapors using cluster kinetics simulations

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Abstract. Atmospheric new particle formation (NPF) occurs by the formation of nanometer-sized molecular clusters and their subsequent growth to larger particles. NPF involving sulfuric acid, bases and oxidized organic compounds is an important source of atmospheric aerosol particles. One of the mechanisms suggested to depict this process is nano-Köhler theory, which describes the activation of inorganic molecular clusters to growth by a soluble organic vapor. In this work, we studied the capability of nano-Köhler theory to describe the initial growth of atmospheric molecular clusters by simulating the dynamics of a cluster population in the presence of a sulfuric acid–base mixture and an organic compound. We observed nano-Köhler-type activation in our simulations when the saturation ratio of the organic vapor and the ratio between organic and inorganic vapor concentrations were in a suitable range. However, nano-Köhler theory was unable to predict the exact size at which the activation occurred in the simulations. In some conditions, apparent cluster growth rate (GR) started to increase close to the activation size determined from the simulations. Nevertheless, because the behavior of GR is also affected by other dynamic processes, GR alone cannot be used to deduce the cluster growth mechanism.

1 Introduction

Atmospheric new particle formation (NPF) is a significant source of global cloud condensation nuclei (CCN) (Kerminen et al., 2012; Spracklen et al., 2008), and thus it affects the magnitude of indirect aerosol radiative forcing (Kazil et al., 2010; Makkonen et al., 2012). NPF has also been observed to contribute to particulate pollution events in urban environments, such as Chinese megacities (Guo et al., 2014). Therefore, accurate understanding of NPF, specifically the formation of the initial nanometer-sized molecular clusters and their further growth to larger particles, is necessary both to decrease uncertainties in climate projections and to tackle urban air quality problems.

According to current knowledge, sulfuric acid is a major driver of the first steps of NPF in most environments (Kuang et al., 2008; Paasonen et al., 2010; Kulmala et al., 2013). Base compounds, such as ammonia and amines, are also important due to their ability to cluster efficiently with sulfuric acid and stabilize the initial nanoparticles (Almeida et al., 2013; Jen et al., 2014, 2016; Kirkby et al., 2011). In addition, electric charge may enhance clustering when electrically neutral clusters are unstable or vapor concentrations are low (Lehtipalo et al., 2016; Kirkby et al., 2016). Low-volatile organic vapors have long been considered responsible for growing the freshly formed particles to larger sizes.
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Understanding the physics and chemistry of NPF involving organic compounds is still very limited, largely because the identities and properties of the organic species are poorly known (Donahue et al., 2013). In particular, there is a lack of a robust physical description of the formation of the initial nanoparticles in the presence of sulfuric acid, bases and organic compounds. Such a description is needed for correct interpretation of the experimental data on NPF but also for implementing the process accurately in larger-scale atmospheric transport models.

NPF is often described as a two-step process (Kulmala et al., 2000). In the first step, a stable cluster that is more likely to grow than to evaporate is formed by nucleation, and in the second step the cluster grows to larger sizes by condensation. The latter step is often referred to as activation of the clusters. Accordingly, particle formation involving sulfuric acid, bases and low-volatile organic compounds can be considered to proceed via the formation of a stable sulfuric acid–base cluster, followed by its growth by condensation of organic vapor (Kulmala et al., 2004). However, if the participation of organic vapor in NPF occurs simply by condensation, the organic vapor needs to have an extremely high saturation ratio to be able to contribute to the growth at nanometer sizes (Kulmala et al., 2004). This is due to the large surface-to-volume ratio of the clusters, which makes attachment of molecules thermodynamically unfavorable. This is qualitatively depicted by the Kelvin effect, in which the saturation ratio over the surface of a spherical particle increases with decreasing particle size. Several mechanisms have been proposed to describe how nanometer-sized clusters can overcome this thermodynamic barrier. These mechanisms include heterogeneous nucleation of organic vapors (Wang et al., 2013), heterogeneous reactions between clusters and organic vapors (Wang et al., 2010; Zhang and Wexler, 2002), adsorption of organics on cluster surface (Wang and Wexler, 2013) and a nano-Köhler-type mechanism (Kulmala et al., 2004). In this study, we focus on nano-Köhler mechanism and its capability to describe the growth of atmospheric clusters.

Nano-Köhler theory was first proposed by Kulmala et al. (2004). It describes the activation of nanometer-sized inorganic clusters to growth by condensation of organic vapor, which is soluble in the inorganic compound and water. Thus, nano-Köhler theory is analogous to Köhler theory describing the activation of CCN to cloud droplets. The fact that nano-Köhler theory is based on the macroscopic properties of the condensing vapors makes it appealing to use for describing the initial particle formation. The nano-Köhler mechanism has been applied in aerosol dynamics models (Anttila et al., 2004; Korhonen et al., 2004), used to describe activation of particles inside condensation particle counters (Giechaskiel et al., 2011; Kulmala et al., 2007) and suggested to explain observed behavior of sub-5 nm particle populations in field and laboratory measurements (Kuang et al., 2012; Kulmala et al., 2013; Tröstl et al., 2016). In a recent laboratory study, Tröstl et al. (2016) examined particle growth rates (GRs) in the presence of monoterpene oxidation products and observed accelerating growth at sizes below 5 nm. Using a volatility distribution growth model, where the condensational growth of a single representative particle is described by nano-Köhler mechanism, the authors suggest that the particle growth at sizes below ~2 nm is governed by organic vapors with extremely low volatility. At larger sizes, where the Kelvin effect is reduced, more abundant vapors with slightly higher volatilities can start to contribute to the growth, resulting in a higher GR.

Although nano-Köhler theory has been applied in aerosol dynamics and single-particle growth models, these modeling approaches provide only limited knowledge of the capability of the theory to describe the very first steps of NPF. This is because these models describe condensation macroscopically, which means that all particles of a given size grow or shrink at the same rate. However, the formation and growth of the smallest sizes is affected by stochastic collision and evaporation processes, which causes widening of the nanoparticle size distribution and enables the crossing of thermodynamic barriers by nucleation (Wang et al., 2013). Furthermore, single-particle modeling approaches assume that particles grow only by vapor monomer collisions, while both experimental and modeling studies indicate that cluster–cluster collisions may significantly contribute to particle growth in some conditions (Kontkanen et al., 2016; Lehtipalo et al., 2016). Modeling the initial NPF accurately requires using a cluster kinetics model, which simulates the time development of cluster concentrations explicitly considering stochastic effects and including all collision and evaporation processes between vapor molecules and clusters (Olenius and Riipinen, 2017).

In this study, our aim is to investigate the potential of nano-Köhler theory to describe the initial growth of atmospheric molecular clusters by organic vapors considering the complex dynamics of a cluster population. For this, we use a molecular-resolution model, which allows us to explicitly simulate the time evolution of a cluster population involving organic and inorganic species. First, we discuss similarities and differences between nano-Köhler theory and the traditional Köhler theory and compare their assumptions to real atmospheric molecular systems. Then, we apply cluster kinetics simulations to study the conditions under which nano-Köhler-type behavior can be observed assuming representative molecular systems. Specifically, we investigate the effects of vapor properties, such as volatility and vapor concentrations, on the dynamics of the cluster population. We also compare the results on cluster activation obtained from the detailed simulations to the predictions of the nano-Köhler theory. This way, we can assess to what extent nano-Köhler
theory, which describes the behavior of the cluster population in a very simplified manner, is able to capture the cluster growth.

2 Theory

Nano-Köhler theory describes the activation of inorganic clusters to grow by spontaneous condensation of organic vapor, which is soluble in the inorganic compound and water (Kulmala et al., 2004). In the original nano-Köhler theory, presented by Kulmala et al. (2004), a system involving sulfuric acid–ammonia clusters, an organic compound, and water is studied. However, the theory can also be applied to other seed compositions and to systems containing only inorganic clusters and an organic vapor without water, which is the case in this study.

Nano-Köhler theory is based on assuming a thermodynamic equilibrium between the clusters and the condensing organic vapor. In an analogous way to the traditional Köhler theory, the equilibrium saturation ratio of the organic compound ($S_{\text{org, eq}}$) is obtained from

$$S_{\text{org, eq}} = x_{\text{org}} f_{\text{org}} \exp \left( \frac{4 \sigma m_{\text{org}}}{k_B T \rho_{\text{org}} d_p} \right), \tag{1}$$

where $x_{\text{org}}$ is the molar fraction of the organic compound in the particle phase, $f_{\text{org}}$ is the activity coefficient, $m_{\text{org}}$ is the molecule mass, $\rho_{\text{org}}$ is the liquid-phase density, $\sigma$ is the cluster surface tension, and $d_p$ is the cluster diameter. $k_B$ is the Boltzmann constant and $T$ is temperature. A similar equation can be written for the equilibrium saturation ratio of water if it is included in the studied system (Kulmala et al., 2004).

From Eq. (1), it is possible to solve the equilibrium saturation ratio of the organic compound for different cluster sizes $d_p$ in the presence of an initial seed cluster with diameter $d_{p,s}$. When the resulting equilibrium saturation ratios are plotted as a function of the cluster size, a curve similar to traditional Köhler curves is obtained. The curve exhibits a peak resulting from the combination of Kelvin and Raoult effects, caused by the curvature of the cluster surface and solubility of the compounds (Vehkamäki and Riipinen, 2012). When the saturation ratio of the organic compound is lower than the peak value, the seed clusters trapped behind the peak maintain their equilibrium size but they cannot grow further. When the saturation ratio increases beyond the peak value, the clusters start to grow spontaneously by condensation of organic vapor (see Fig. 1). Thus, the ascending part of the curve corresponds to the stable equilibrium state and the descending part to the unstable equilibrium (Reiss and Koper, 1995). Note that this behavior is different than in classical heterogeneous nucleation, where the seed is insoluble in the nucleating vapor, and the saturation ratio needed for the cluster activation decreases as a function of cluster size without a maximum (Winkler et al., 2008).

Although the thermodynamic equilibrium is described in an analogous way in nano-Köhler theory and in the traditional Köhler theory, there are differences between these two theories, especially related to the systems that they are describing (Anttila et al., 2004; Kulmala et al., 2004). The comparison between the theories is presented in Table 1. Furthermore, the real systems differ significantly from the simplified system assumed in nano-Köhler theory (see Table 1 and Fig. 1). In real systems, there is no specific non-evaporating seed or condensing vapor but there is a distribution of inorganic and organic vapor molecules and clusters which all can collide and evaporate. Furthermore, there does not necessarily exist an energy barrier that needs to be overcome, but the growth of clusters may be entirely governed by kinetic collisions. If an energy barrier exists, clusters may overcome the barrier even before the critical saturation ratio is reached as a result of stochastic collisions, i.e., nucleation, and thus the system is not in thermodynamic equilibrium all the time (Vehkamäki and Riipinen, 2012). In addition, in real systems, organic and inorganic vapors are not lost solely due to scavenging by pre-existing particle population but also due to collisions with clusters. Furthermore, vapor concentrations and external losses may vary over time, which can affect the dynamics of the cluster population.

3 Methods

3.1 Cluster kinetics model

We used a molecular-resolution cluster kinetics model to simulate the time development of atmospheric cluster concentrations. Two model compounds, one corresponding to an inorganic compound and one corresponding to an organic compound, were used in the simulations (see the next section for the properties of the model compounds). The cluster population was simulated starting from vapor monomers up to clusters with mass diameter of 3.2–3.4 nm, including all possible cluster compositions. The largest simulated clusters correspond to the size of a pure inorganic cluster composed of 100 molecules.

In the model, the discrete general dynamic equation (GDE; Friedlander, 1977), which is also called an extended Smoluchowski coagulation equation, is numerically solved for each cluster composition $i$ including all processes where a cluster can be formed or lost:

$$\frac{dC_i}{dt} = \frac{1}{2} \sum_{j<i} \beta_{j,(i-j)} C_j C_{i-j} + \sum_{j>i} \gamma_{(i+j)\rightarrow i,j} C_{i+j} - \sum_{j<i} \gamma_{i\rightarrow (i-j),j} C_i C_j - \frac{1}{2} \sum_{j<i} \gamma_{i\rightarrow (i+j),j} C_i + Q_i - L_i C_i. \tag{2}$$

Here, $C_i$ is the concentration of cluster $i$, and $\beta_{i,j}$ is the collision rate coefficient between cluster $i$ and cluster $j$. $\gamma_{(i+j)\rightarrow i,j}$ is the evaporation rate coefficient of cluster $(i+j)$.
Figure 1. Schematic figure illustrating how the growth of atmospheric molecular clusters is described by nano-Köhler theory, and how the growth occurs in real molecular systems affected by various dynamic processes.

Table 1. Comparison between Köhler theory, nano-Köhler theory and real systems of atmospheric molecular clusters.

<table>
<thead>
<tr>
<th>Köhler theory</th>
<th>Nano-Köhler theory</th>
<th>Real molecular systems</th>
</tr>
</thead>
<tbody>
<tr>
<td>Describes the activation of CCN ($d_p &gt; 50$ nm) to cloud droplets by spontaneous condensation of water vapor.</td>
<td>Describes the activation of inorganic clusters ($d_p \approx 1-3$ nm) for growth by spontaneous condensation of organic vapor.</td>
<td>A distribution of clusters of varying sizes and compositions including inorganic and organic compounds can exist simultaneously at all times.</td>
</tr>
<tr>
<td>The condensing vapor is water vapor with typical atmospheric concentrations of $\sim 10^{17}$ cm$^{-3}$.</td>
<td>The condensing vapor is a water-soluble organic compound with concentrations likely ranging from $\sim 10^5$ to $10^8$ cm$^{-3}$ (Jokinen et al., 2017).</td>
<td>Vapor concentrations are not constant but may vary over time.</td>
</tr>
<tr>
<td>The seed consists of a mixture of inorganic/organic compounds and is water soluble. The seed compounds do not evaporate.</td>
<td>The seed consists of sulfuric acid and bases and is soluble in the condensing organic compound. The seed compounds do not evaporate but condense irreversibly on the cluster.</td>
<td>There is no seed in the same sense as in the theory. Both inorganic and organic compounds can condense and evaporate and may contribute to the growth.</td>
</tr>
<tr>
<td>Thermodynamic equilibrium between water and the seed particle is assumed.</td>
<td>Thermodynamic equilibrium between the organic compound, the seed cluster and water is assumed. The energy barrier width in nano-Köhler is very narrow with respect to the number of molecules compared to Köhler theory, and thus addition of only few molecules may result in overcoming the barrier.</td>
<td>Clusters can nucleate over barriers and they may not be in thermodynamic equilibrium before activation to growth.</td>
</tr>
<tr>
<td>The growing cloud droplets scavenge the available water vapor thereby limiting the activation process.</td>
<td>The loss rate of organic vapor is determined mainly by larger background aerosol particles and not the growing clusters.</td>
<td>The cluster population is affected by losses due to background particles, and cluster self-coagulation may also be important. The magnitude of external losses may vary over time.</td>
</tr>
</tbody>
</table>
to clusters $i$ and $j$, which we considered only for evaporation
to vapor monomers. $Q_i$ is the source rate, here included
only for vapor molecules. $L_i$ is the loss rate coefficient corre-
sponding to the external sink for vapors and clusters. The set
of GDEs was generated and solved with the ACDC (Atmo-
spheric Cluster Dynamics Code) program (McGrath et al.,
2012; Olenius and Riipinen, 2017).

The collision rate coefficients $\beta_{i, j}$ were calculated assum-
hard-sphere collisions. The evaporation rate coefficients
of vapor monomers were calculated according to the Kelvin
formula:

$$\gamma_{i+j \rightarrow i, j} = \beta_{i, j} \frac{p_{\text{sat}, i}}{k_B T} \sigma_i \exp \left( \frac{4 \sigma m_i}{k_B T \rho_i d_p i, j} \right). \quad (3)$$

Here, $\beta_{i, j}$ is the collision rate coefficient between vapor
compound $i$ and cluster $j$. $p_{\text{sat}, i}$ is the saturation vapor
pressure of the compound, $\sigma_i$ is the molar fraction of the com-
ponent in cluster $j$, $\sigma$ is the cluster surface tension, $m_i$ is
the molecule mass, $\rho_i$ is the liquid-phase density of $i$, and
$\rho_{p, i}$ is the cluster diameter. $k_B$ is the Boltzmann constant
and $T$ is the temperature. Calculating evaporation rates from
Eq. (3) is consistent with calculating equilibrium saturation
ratios from Eq. (1) when assuming that the activity coeffi-
cient $f = 1$. One should note that these evaporation rates can
significantly differ from the real cluster evaporation rates in a
system involving sulfuric acid and organic compounds. How-
ever, in this study, our aim is not to use as complex evapora-
tion rates in which dimethylamine and ammonia cluster with sulfu-
ric acid, dimethylamine forming seemingly non-evaporating
clusters (Jen et al., 2014; Kürten et al., 2014).

In most simulations, the inorganic compound was set to have the mass of a sulfuric acid–dimethylamine cluster
(SA–DMA) and $p_{\text{sat}} = 0$. Additional simulations were
performed using the mass of ammonium bisulfate (SA–
NH$_4$) and $p_{\text{sat}} = 10^{-9}$ Pa. The properties of these model sub-
stances are consistent with observations on a 1 : 1 molar ra-
tio in which dimethylamine and ammonia cluster with sulfu-
ric acid, forming seemingly non-evaporating
clusters (Jen et al., 2014; Kürten et al., 2014).

In most simulations, the organic compound (ORG) was set
to have a mass of 300 amu and its $p_{\text{sat}}$ was varied between
10$^{-6}$ and 10$^{-12}$ Pa. Of these saturation vapor pressures, two
were selected for a more detailed study: $p_{\text{sat}} = 10^{-8}$ Pa,
representing a low-volatile organic compound (LVOC), and
$p_{\text{sat}} = 10^{-11}$ Pa, representing an extremely low-volatile or-
compound (ELVOC). In addition, simulations were
performed using a compound with $p_{\text{sat}} = 10^{-8}$ Pa and a mass
of 600 amu, corresponding to LVOC with a larger mass
(LVOC$_\text{large}$). The saturation vapor pressures of the LVOC and
ELVOC species are consistent with the volatility basis set
classification of organic compounds with low and extremely
low volatilities (Donahue et al., 2012). They also may repres-
t typical saturation vapor pressures of $\alpha$-pinene oxidation
products (Tröstl et al., 2016), but as different methods give
g very different estimates for saturation vapor pressures, the
exact values are uncertain (Kurtén et al., 2016).

In addition to the saturation vapor pressures and mole-
cular masses, the assumed liquid-phase densities, the parti-
cle surface tension and the activity coefficients can have
significant effects on the results. In earlier studies investi-
gating nano-Köhler theory, these properties have been ob-
tained by fitting a simple thermodynamic model to measured
data on particle properties (Anttila et al., 2004; Kulmala et
al., 2007). One should note that if cluster losses were sig-
ificantly changed in our simulations, the growth dynam-
ics of the cluster population could change. However, minor
changes in the losses are not expected to affect our results on
the qualitatively level.

### 3.2 Studied compounds

We simulated binary mixtures of inorganic and organic com-
ponents relevant for atmospheric particle formation. The inor-
ganic compound corresponds to a quasi-uniary sulfuric acid–
dimethylamine forming seemingly non-evaporating
clusters. However, in this study, our aim is not to use as complex evapora-
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the qualitatively level.
Table 2. Model compounds, their molecular mass (m), saturation vapor pressure (p\text{sat}) and the corresponding number concentration (C_{\text{sat}}) and mass concentration (C_{\text{mass, sat}}) at T = 278 K. Note that LVOC and ELVOC are two cases of the organic compound (ORG) selected for more detailed studies.

<table>
<thead>
<tr>
<th>Model substance</th>
<th>m (amu)</th>
<th>p\text{sat} (Pa)</th>
<th>C_{\text{sat}} (cm^{-3})</th>
<th>C_{\text{mass, sat}} (\mu g m^{-3})</th>
</tr>
</thead>
<tbody>
<tr>
<td>SA–DMA</td>
<td>143</td>
<td>10^{-9}</td>
<td>2.6 \times 10^5</td>
<td>5.0 \times 10^{-5}</td>
</tr>
<tr>
<td>SA–NH\textsubscript{3}</td>
<td>115</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>ORG</td>
<td>300</td>
<td>10^{-12}–10^{-6}</td>
<td>2.6 \times 10^2–2.6 \times 10^8</td>
<td>1.3 \times 10^{-7}–1.3 \times 10^{-1}</td>
</tr>
<tr>
<td>LVOC</td>
<td>300</td>
<td>10^{-8}</td>
<td>2.6 \times 10^6</td>
<td>1.3 \times 10^{-3}</td>
</tr>
<tr>
<td>ELVOC</td>
<td>300</td>
<td>10^{-11}</td>
<td>2.6 \times 10^3</td>
<td>1.3 \times 10^{-6}</td>
</tr>
<tr>
<td>LVOC\textsubscript{large}</td>
<td>600</td>
<td>10^{-8}</td>
<td>2.6 \times 10^6</td>
<td>2.6 \times 10^{-3}</td>
</tr>
</tbody>
</table>

Table 3. Description of the simulation sets. The variables are varied at intervals of 1 order of magnitude. Note that the presented vapor concentrations are steady-state values for sets 1–4 and the maximum values for set 5.

<table>
<thead>
<tr>
<th>Simulation set</th>
<th>Compounds</th>
<th>Vapor concentrations (cm^{-3})</th>
<th>Conditions</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>SA–DMA</td>
<td>C_{\text{SA}} = 10^6</td>
<td>constant C_{\text{SA}} and C_{\text{ORG}}- chamber experiment losses (Eq. 4)</td>
</tr>
<tr>
<td></td>
<td>ORG, p\text{sat} = 10^{-12} \ldots 10^{-6} Pa</td>
<td>C_{\text{ORG}} = 10^4 \ldots 10^{10}</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>SA–DMA</td>
<td>C_{\text{SA}} = 10^7</td>
<td>constant C_{\text{SA}} and C_{\text{ORG}}- chamber experiment losses (Eq. 4)</td>
</tr>
<tr>
<td></td>
<td>LVOC or ELVOC</td>
<td>C_{\text{ORG}} = 10^7 \ldots 10^{10}</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>SA–NH\textsubscript{3}</td>
<td>C_{\text{SA}} = 10^6</td>
<td>constant C_{\text{SA}} and C_{\text{ORG}}- chamber experiment losses (Eq. 4)</td>
</tr>
<tr>
<td></td>
<td>LVOC</td>
<td>C_{\text{ORG}} = 10^6 \ldots 10^{9}</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>SA–DMA</td>
<td>C_{\text{SA}} = 10^6</td>
<td>constant C_{\text{SA}} and C_{\text{ORG}}- chamber experiment losses (Eq. 4)</td>
</tr>
<tr>
<td></td>
<td>LVOC\textsubscript{large}</td>
<td>C_{\text{ORG}} = 10^6 \ldots 10^{9}</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>SA–DMA</td>
<td>C_{\text{SA, max}} = 10^6</td>
<td>varying C_{\text{SA}} and C_{\text{ORG}}, background particle losses (Eq. 5)</td>
</tr>
<tr>
<td></td>
<td>LVOC</td>
<td>C_{\text{ORG, max}} = 5 \times 10^6, 10^{7}</td>
<td></td>
</tr>
</tbody>
</table>

system would mainly lower the saturation vapor pressure of the organic compound through the solute effect (Raoult’s law). We address the effect of the organic compound volatility by performing simulations with a large range of organic saturation vapor pressures. One should note, though, that in reality water can also affect the surface tension and density of the clusters as well as the activity coefficient when assuming non-ideal mixing. Furthermore, water molecules increase the cluster size, thus affecting the collision coefficients, and consequently also the evaporation coefficients through the detailed balance (Eq. 3; see also Henschel et al., 2016).

3.3 Simulation sets

All performed simulation sets are described in Table 3. In simulation sets 1–4, the concentrations of the inorganic vapor (C_{\text{SA}}) and the organic vapor (C_{\text{ORG}}) were set to constant values and the simulations were run until the steady state was reached. In addition, in order to mimic a laboratory set-up, simulations with constant vapor source rates, resulting in the same steady-state vapor concentrations, were performed to study the cluster GRs. By default, the inorganic and organic species were SA–DMA and LVOC or ELVOC, unless otherwise stated. Temperature was set to 278 K in all the simulations. The sets address the effect of the volatility p_{\text{sat, ORG}} and concentration C_{\text{ORG}} of the organic vapor (set 1), the effect of relatively high sulfuric acid concentration C_{\text{SA}} (set 2), the effect of the properties of the inorganic vapor (set 3) and the effect of the mass of the organic vapor (set 4). The simulation set 5 addresses the effect of time-dependent vapor concentration profiles corresponding to atmospheric conditions. Two different simulations were performed: (1) a simulation where inorganic and organic vapor source rates exhibit maxima and (2) a simulation where the inorganic vapor source rate exhibits a maximum but the organic vapor source rate is constant. These simulations were run for 12 h.

3.4 Analysis of simulated data

From the simulated cluster concentrations, we determined the contributions of different vapor monomers and clusters to the growth over selected threshold sizes d_{th} between 1 and 3 nm. The net cluster flux J_{th} past each threshold size was determined by considering all the collisions and evaporations between different clusters or vapor molecules that
lead to crossing of the threshold as

\[ J_{dp} = \frac{1}{2} \sum (\beta i, j C_i C_j - \gamma i, j \rightarrow i, j C_i + j), \]

where \( d_{p,i} \) and \( d_{p,j} < d_{p}^{th} \), and \( d_{p,i+j} \geq d_{p}^{th} \). The contribution of an individual molecule or cluster to this flux was determined so that for each collision–evaporation process between species \( i \) and \( j \) leading to the crossing of the threshold, the resulting flux was attributed to the species with the smaller number of molecules. The reasoning behind this is that when, for example, a vapor monomer \( i \) collides with cluster \( j \) composed of several molecules, the monomer is causing the cluster to grow in size, and thus the flux is assigned to be due to \( i \).

In addition, we determined the apparent cluster GRs using the experimental approach that is often applied for measured particle size distribution data (Lehtipalo et al., 2014). In order to treat the simulation data similarly to measured particle concentrations, we divided the clusters into linearly spaced size bins of a width of 0.1 nm based on their mass diameter. Vapor monomers were, however, omitted from the size bins to ensure that they do not dominate the smallest bins. Then, we determined the appearance time (\( t_{app} \)) for each size bin as the time at which the concentration of the bin reaches 50% of the total concentration increase in the bin (Lehtipalo et al., 2014). Finally, we determined GR for each bin \( k \) with the mean diameter \( d_{p,k} \) by numerically differentiating the (\( t_{app}, d_p \)) data:

\[ GR_k = \frac{d_{p,k+1} - d_{p,k}}{t_{app,k+1} - t_{app,k}}. \]

### 3.5 Nano-Köhler calculations

To compare the predictions of nano-Köhler theory to the results of the cluster kinetics simulations, we calculated the equilibrium saturation ratio of the organic vapor from Eq. (1) and determined the activation diameter and the corresponding saturation ratio for different seed cluster sizes. In these calculations, we used the same properties of the compounds as in the cluster population simulations (see Sect. 3.2), and varied the seed cluster size between 0.9 and 2.9 nm.

## 4 Results and discussion

The cluster kinetics simulations indicate that nano-Köhler-type activation occurs in specific conditions, determined by vapor concentrations and the organic vapor saturation ratio. In this section, we first go through two example cases: one case where nano-Köhler-type activation is observed and another case without activation. Then, we discuss more generally the conditions where activation occurs, and compare the activation sizes determined from the simulations to those based on nano-Köhler theory. We also study the connection between the activation sizes and the behavior of apparent cluster GRs. Finally, we discuss the sensitivity of the results to vapor properties and the time evolution of the vapor concentrations.

### 4.1 Effects of organic vapor volatility and vapor concentrations on the growth mechanism

#### 4.1.1 Simulations with LVOC

Figures 2–4 show the results for the simulations where the model compounds were SA–DMA and LVOC, \( C_{SA} = 10^6 \text{ cm}^{-3} \) and \( C_{OR} = 10^6 - 10^9 \text{ cm}^{-3} \). Figure 2 presents the steady-state cluster distributions, illustrating how the relative contributions of SA and LVOC to the growth of the cluster population depend on their concentrations. When both \( C_{OR} \) and \( C_{SA} \) are \( 10^6 \text{ cm}^{-3} \), the growth proceeds mainly by additions of SA molecules, while at \( C_{OR} = 10^7 \text{ cm}^{-3} \), both SA and LVOC participate in the growth. At \( C_{OR} = 10^8 \text{ cm}^{-3} \) or higher, the growth is clearly dominated by LVOC. A more detailed picture of the roles of SA and LVOC in the cluster growth is obtained by studying the particle fluxes past selected threshold sizes caused by different vapor monomers or clusters. Figure 3 shows the steady-state flux fractions for five threshold sizes between 1 and 3 nm in different simulations. The flux fractions are presented for SA monomer, SA dimer, pure SA clusters (trimers or larger), LVOC monomer, LVOC dimer, pure LVOC clusters (trimers or larger) and the clusters containing both SA and LVOC (dimers or larger).

When \( C_{OR} = 10^6 \text{ cm}^{-3} \), SA monomer dominates the flux at all sizes, and the rest of the flux is mainly caused by SA dimer and SA clusters. The contribution of LVOC monomer to the flux is minor at all sizes. When \( C_{OR} = 10^4 \text{ cm}^{-3} \), the fractions of the flux due to SA and LVOC exhibit a distinct size dependency. The contribution of SA monomer to the flux is highest at 1.5 nm and lowest at 3 nm. LVOC has a significant contribution to the flux at 1 nm, a minor contribution at 1.5 nm and a larger, increasing contribution at 2 nm and above. This behavior resembles nano-Köhler-type activation where the critical size, corresponding to the peak of the Köhler curve, is around 2 nm; at sizes smaller than that, the growth by organic vapor is minor due to the Kelvin barrier, while at larger sizes, organic vapor can start to spontaneously condense on the clusters. When interpreting the cluster flux results, it should be kept in mind, though, that only the collisions between vapor monomers and the smallest clusters can contribute to the flux past 1 nm due to their small size.

When \( C_{OR} = 10^8 \text{ cm}^{-3} \), LVOC monomer dominates the flux at 1 nm as well as at 2 nm and above. However, at 1.5 nm, most of the flux is caused by LVOC clusters, and the net flux of LVOC monomer is negative due to its high evaporation flux. Thus, this can also be considered a nano-Köhler-type situation where the critical size is around 2 nm, and at sizes just below that the growth can occur only by self-coagulation and not by condensation of vapor monomers.
It should be noted, though, that large uncertainties are related to calculating the evaporation rate of LVOC monomers from Kelvin formula (Eq. 3). Therefore, LVOC dimers and other small clusters may become unrealistically stable compared to monomers, and their contribution to the growth may be overestimated. Evaporation rates assessed by more sophisticated methods, namely quantum-mechanics-based approaches, also exhibit very high quantitative uncertainties (see, e.g., Elm et al., 2017 and references therein).

When $C_{\text{ORG}} = 10^9 \text{ cm}^{-3}$, LVOC monomer contributes to the flux at all sizes. The fluxes due to LVOC dimer and LVOC clusters are also significant at sizes above 1 nm. Thus, this simulation corresponds to the situation where the Kelvin barrier does not exist at any size, due to high vapor concentration.

We also studied GRs determined for different size bins based on their appearance times (Fig. 4). When $C_{\text{ORG}} = 10^9 \text{ cm}^{-3}$, GR varies between 0.2 and 0.7 nm h$^{-1}$, being highest at the smallest sizes. When $C_{\text{ORG}} = 10^7 \text{ cm}^{-3}$, GR is between 0.3 and 0.9 nm h$^{-1}$, increasing with size in the bins above $\sim 2.6$ nm. When $C_{\text{ORG}} = 10^8 \text{ cm}^{-3}$, GR varies between 0.5 and 12 nm h$^{-1}$, and it increases with size above $\sim 1.6$ nm. When $C_{\text{ORG}} = 10^9 \text{ cm}^{-3}$ (not shown), GR fluctuates strongly, and it obtains either extremely high ($\sim 400$ nm h$^{-1}$) or negative values. This is due to very rapid appearance of different sized clusters in this simulation, which makes deducing GR from appearance times ambiguous. GR also fluctuates in other simulations at the smallest sizes. This results from the fact the bins at the smallest sizes contain only a few clusters, whereas the bins at the largest sizes contain hundreds of different clusters. In previous experimental studies, increase of GR as a function of size has been attributed to the activation of clusters by nano-Köhler mechanism (Kulmala et al., 2013; Tröstl et al., 2016). We study the connection between the size dependency of GR and nano-Köhler activation in Sect. 4.2.

### 4.1.2 Simulations with ELVOC

Figures 5–7 present the results of the simulations where the model compounds were SA–DMA and ELVOC and $C_{\text{SA}} = 10^6 \text{ cm}^{-3}$ and $C_{\text{ORG}} = 10^6-10^9 \text{ cm}^{-3}$. Thus, the only difference compared to the simulations discussed in the previous section is the lower volatility ($p_{\text{sat}}$) of the organic compound.

The steady-state cluster distributions show that the organic compound contributes to the growth of the cluster population clearly more in the simulations with ELVOC than with LVOC (Fig. 5). When $C_{\text{SA}}$ and $C_{\text{ORG}}$ are $10^6 \text{ cm}^{-3}$, SA and ELVOC contribute to the growth approximately equally.
When $C_{\text{ORG}} = 10^7 \text{ cm}^{-3}$ or higher, the growth is already dominated by ELVOC.

Consistently with the cluster distributions, the fractions of the cluster flux caused by the organic compound are clearly higher in the simulations with SA–DMA and ELVOC than in the simulations with LVOC (Fig. 6). When $C_{\text{ORG}} = 10^6 \text{ cm}^{-3}$, SA monomer has only a rather small contribution to the fluxes at all sizes. ELVOC monomer dominates the flux at 1 nm and contributes to the fluxes significantly also at larger sizes. The clusters containing both SA and ELVOC molecules also contribute to the fluxes above 1 nm. When $C_{\text{ORG}} = 10^7 \text{ cm}^{-3}$, SA monomer has only a negligible contribution to the fluxes at all sizes. ELVOC monomer dominates the flux at 1 nm. At larger sizes, the fluxes are mainly caused by ELVOC monomer, ELVOC dimer, larger ELVOC clusters and clusters containing both SA and ELVOC molecules. In the simulations where $C_{\text{ORG}} = 10^8 \text{ cm}^{-3}$ or $10^9 \text{ cm}^{-3}$, the fluxes at all sizes are due to ELVOC monomer, ELVOC dimer and ELVOC clusters. ELVOC monomer dominates the growth below 2 nm and ELVOC clusters at the larger sizes.

Overall, in the simulations with ELVOC, no nano-Köhler-type behavior is observed. In these simulations, the organic vapor can contribute to the growth at all sizes without an apparent barrier that should be overcome at small sizes.

The behavior of GR is also different in simulations with ELVOC compared to simulations with LVOC (Fig. 7). When $C_{\text{ORG}} = 10^6 \text{ cm}^{-3}$, GR varies between 0.7 and 2.2 nm h$^{-1}$
and reaches its highest values in the smallest size bins. When $C_{\text{ORG}} = 10^7 \text{ cm}^{-3}$, GR mostly varies between 6.5 and 9.5 nm h$^{-1}$, but in the smallest size bins reaches values as high as 180 nm h$^{-1}$. When $C_{\text{ORG}} = 10^8 \text{ cm}^{-3}$, GR varies between 60 and 120 nm h$^{-1}$, without a clear size dependency. Thus, in the simulations with ELVOC, GR does not increase with the increasing size in the same way as in the simulations with LVOC. This indicates that increasing GR observed in simulations with LVOC may be linked to nano-Köhler-type activation.

4.1.3 Overall picture

In the simulations performed with different vapor concentrations and with a variety of organic saturation vapor pressures (simulation set 1 in Table 3), different growth mechanisms can be recognized. In some simulations, sulfuric acid dominates the growth of the cluster population at all sizes, whereas in other simulations the organic compound dominates. In some simulations, we observe a nano-Köhler-type activation, where the organic vapor starts to condense on clusters and dominate the growth after a certain size is reached. In other simulations, there is a transition between the dominance of inorganic and organic vapor but no specific size at which the dominating compound changes.

The main variables determining which of the growth mechanisms prevails in a simulation are the saturation ratio of the organic compound ($S_{\text{ORG}}$) and the ratio between the concentrations of organic and inorganic vapors ($C_{\text{ORG}}/C_{\text{SA}}$). Figure 8 illustrates the dominating growth mechanism at different values of these variables. Nano-Köhler activation is observed only in rather specific conditions when $S_{\text{ORG}} \approx 4–40$ and $C_{\text{ORG}}/C_{\text{SA}} \approx 10–10000$. When $S_{\text{ORG}}$ and $C_{\text{ORG}}/C_{\text{SA}}$ are lower than these values, sulfuric acid dominates the growth at all sizes, while at larger values the organic vapor dominates. When $C_{\text{ORG}}/C_{\text{SA}} = 1$ and $S_{\text{ORG}}$ is $\approx 40$ or larger, a transition without a clear activation is observed. It should be noted, though, that the activation may also occur at lower $S_{\text{ORG}}$ and $C_{\text{ORG}}/C_{\text{SA}}$ values at sizes above 3 nm, which are beyond the simulated size range. In addition, it is important to keep in mind that the conditions for different growth mechanisms depend on vapor properties and environmental conditions, and thus they cannot be generalized to arbitrary compounds and conditions.

In simulations with SA–DMA and LVOC discussed in Sect. 4.1.1 (see Fig. 3), three of the different growth mech-
Figure 6. Contribution of different vapor monomers and clusters to the net flux past certain threshold sizes in simulations with SA–DMA and ELVOC at $C_{SA} = 10^6$ cm$^{-3}$ and $C_{ORG} = 10^6$–10$^9$ cm$^{-3}$. The values are at steady state.

Figure 7. GRs determined for different size bins in simulations with SA–DMA and ELVOC. The colors indicate vapor concentrations in each simulation.

Figure 8. GRs determined for different size bins in simulations with SA–DMA and ELVOC. The colors indicate vapor concentrations in each simulation.

In the simulations with SA–DMA and ELVOC discussed in Sect. 4.1.2 (see Fig. 6), nano-Köhler-type behavior cannot be seen. At $C_{ORG} = 10^6$ cm$^{-3}$, the growth occurs both by ELVOC and SA–DMA without a clear size dependency, and thus this simulation represents the transition case. With higher $C_{ORG}$, ELVOC dominates the growth at all sizes.

On a general level, Fig. 8 can be interpreted to give information on the relative thermodynamic barriers of inorganic and organic compounds: the compound that has no barrier or has a significantly lower barrier to cluster and condense than the other compound is likely to dominate the growth of the cluster population.

4.2 Comparison between activation size in simulations and in nano-Köhler theory

To study the cluster activation size from the simulations, we determined the contribution of different compounds to cluster flux with a higher size resolution in four simulations where nano-Köhler activation is observed (Fig. A2). We determined the size at which at least 50% of the flux is due to organic vapor monomer, which we define as the activation size $d_{sim}$ (Table 4). To compare these results to the predictions of nano-Köhler theory, we calculated the equilibrium saturation ratio of LVOC for different seed cluster sizes.
Figure 8. Growth mechanisms with different organic vapor saturation ratios ($S_{\text{ORG}}$) and the ratios of organic vapor concentration ($C_{\text{ORG}}$) to sulfuric acid concentration ($C_{\text{SA}}$). In the red area, the growth is dominated by sulfuric acid, and in the green area by the organic vapor. In the yellow and gray areas, neither of them clearly dominates: in the yellow area, nano-Köhler-type activation, involving an increasing contribution of the organic vapor with increasing particle size, is observed, and in the gray area, there is a transition between these compounds without an activation.

Figure 9. Köhler curves showing the equilibrium particle size at different saturation ratios for LVOC. The line color shows the diameter of the seed particle ($d_s$). The maxima of the curves correspond to the critical sizes.

from Eq. (1). The resulting Köhler curves are illustrated in Fig. 9 and the critical diameters from the theory ($d_{\text{theory}}$) corresponding to the simulated conditions are shown in Table 4. In addition, to study the connection between accelerating growth and nano-Köhler activation, we determined the sizes at which the appearance time GR starts to significantly increase with size in each of these simulations ($d_{\text{GR}}$). This was done by finding the size at which the relative increase of GR between two adjacent size bins is more than 10%. Note, though, that $d_{\text{GR}}$ could not be determined for the simulation with $C_{\text{ORG}} = 10^9 \text{ cm}^{-3}$ due to strong fluctuation of GR.

In the simulations where $S_{\text{ORG}} = 38$, $d_{\text{sim}}$ and $d_{\text{theory}}$ are rather close to each other: the difference between them is 0.05–0.3 nm depending on vapor concentrations. However, when $S_{\text{ORG}} = 3.8$, $d_{\text{sim}}$ is clearly lower (∼1 nm) than $d_{\text{theory}}$. This discrepancy is likely related to the fact that the theory does not account for the stochastic collisions between inorganic and organic vapor molecules and clusters, which can result in the growth of the clusters by organic vapor already before the theoretical critical size (see also Sect. 2). Thus, although nano-Köhler-type behavior occurs in the simulated systems, the theory cannot be used to predict the exact size at which the organic vapor starts to dominate the cluster growth.

On the other hand, the difference between $d_{\text{sim}}$ and $d_{\text{GR}}$ is only 0.05–0.35 nm in different simulations. This suggests that, at least in some conditions, the increase in particle GR may indicate that the organic vapor starts to condense on the clusters around that size. However, as the behavior of GR is also affected by the variation of vapor concentrations and other conditions, this does not necessarily apply in real atmospheric systems (see Sect. 4.3.2).

It should finally be noted that it is not entirely obvious how $d_{\text{sim}}$ should be defined. In some simulations, there is a distinct size after which most of the flux is due to organic vapor monomer, but in some simulations the change is more gradual. In addition, in many simulations, organic dimer or larger organic clusters contribute to the growth significantly at sizes where the net flux of the organic vapor monomer is negative. Thus, in these cases, the growth is governed by the organic compound already before the activation size, which we determine only based on the contribution of the organic monomer.
Table 4. The activation size ($d_{\text{sim}}$) determined from four simulations, the corresponding critical size from nano-Köhler theory ($d_{\text{theory}}$) and the size at which GR starts to increase with size in each simulation ($d_{\text{GR}}$). The activation size is here defined as the size when 50% of the cluster flux is due to organic vapor monomer. The concentrations of sulfuric acid ($C_{\text{SA}}$) and organic vapor ($C_{\text{ORG}}$), their ratio, organic saturation vapor pressure ($P_{\text{sat, ORG}}$) and organic saturation ratio ($S_{\text{ORG}}$) are shown for each case.

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<tr>
<th>$C_{\text{SA}}$ (cm$^{-3}$)</th>
<th>$C_{\text{ORG}}$ (cm$^{-3}$)</th>
<th>$C_{\text{ORG}}/C_{\text{SA}}$</th>
<th>$P_{\text{sat, ORG}}$ (Pa)</th>
<th>$S_{\text{ORG}}$</th>
<th>$d_{\text{sim}}$ (nm)</th>
<th>$d_{\text{theory}}$ (nm)</th>
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4.3 Sensitivity of the results to vapor properties and time dependency of vapor concentrations

4.3.1 Effect of inorganic vapor properties and organic compound mass

To study the effect of inorganic vapor properties on the growth of the cluster population, we performed additional simulations (simulation set 3 in Table 3) where the organic compound was LVOC and the inorganic compound was SA–NH$_3$, which has a non-zero saturation vapor pressure ($10^{-9}$ Pa) and a slightly smaller mass than SA–DMA (see Table 2). In these simulations, the contribution of inorganic compound to the cluster fluxes, especially that of vapor monomer, is smaller than in the simulations with SA–DMA, due to higher evaporation flux (Fig. A3). The GRs determined for different size bins are generally slightly lower in the simulations with SA–NH$_3$ than with SA–DMA (Fig. A4). However, when $C_{\text{SA}} = 10^6$ cm$^{-3}$ and $C_{\text{ORG}} = 10^6$ cm$^{-3}$, GR at sizes above 2.5 nm is higher in the simulations with SA–NH$_3$ than with SA–DMA. In this case, the GRs determined based on the appearance times seem not to represent the magnitude of collision–evaporation fluxes which are larger in the simulation with SA–DMA.

We also performed simulations with SA–DMA and an organic compound with the same saturation vapor pressure as LVOC ($10^{-9}$ Pa) but two times larger mass (LVOC$_{\text{large}}$) (simulation set 4 in Table 3). In the simulations where $C_{\text{SA}} = 10^6$ cm$^{-3}$, and $C_{\text{ORG}} = 10^7$–$10^9$ cm$^{-3}$, the organic compound was found to contribute to the growth clearly less than in the simulations with LVOC (Fig. A5). The main reason for the difference is that the evaporation rate is higher for the compound with a higher mass, due to a larger molecular volume ($m_{\text{ORG}}/\rho_{\text{ORG}}$) and thus also a larger surface area of a molecule at the cluster surface (see Eq. 3). In addition, the diameter of LVOC$_{\text{large}}$ monomer is higher than 1 nm, it cannot contribute to the flux at 1 nm by default. Consistently with the lower contribution of the organic compound to the growth, the apparent cluster GRs are also lower in the simulations with LVOC$_{\text{large}}$ than with LVOC (Fig. A6). Overall, these results demonstrate that the properties of both inorganic and organic compounds, including saturation vapor pressure but also other properties, can significantly affect the contribution of different compounds to the cluster growth. Therefore, our simulation results regarding, for example, the conditions for different growth mechanisms (Sect. 4.1.3) cannot be generalized for arbitrary compounds.

4.3.2 Effect of time dependency of vapor concentrations

To study the effect of time-dependent vapor concentrations, two additional simulations were performed using SA–DMA and LVOC as model compounds (simulation set 5 in Table 3). In the first simulation, the behavior of both vapor source rates was set to resemble the diurnal cycle of atmospheric sulfuric acid concentration (Petäjä et al., 2009). In the second simulation, the source rate of SA–DMA had a similar behavior but the source rate of LVOC was set constant. The resulting vapor concentrations and the GRs determined for different size bins are shown in Fig. 10. The time evolution of the net flux caused by different vapor monomers and clusters past different sizes in these simulations is shown in Fig. A7. Based on the flux results, in both of these simulations, the organic vapor starts to significantly contribute to cluster growth around 2 nm, which corresponds to nano-Köhler-type activation. In the simulation where both $C_{\text{SA}}$ and $C_{\text{ORG}}$ have maxima, the activation can also be seen as an increase in GR at sizes above 2 nm. However, in the simulation with constant $C_{\text{ORG}}$, GR increases with size almost linearly, without any signs of activation. This shows that the size dependency of GR is affected by dynamic variations in the system, and therefore GR alone cannot be used to deduce the cluster growth mechanism.

5 Conclusions

Recent experimental results indicate that organic vapors can participate in the growth of nanometer-sized atmospheric molecular clusters. One of the mechanisms proposed to depict this process is nano-Köhler theory, which describes the activation of inorganic clusters to growth by a soluble organic vapor. However, it is unclear how well the simple theory is...
able to describe the dynamics of real molecular systems with a distribution of clusters of varying size and composition and time-dependent environmental conditions.

In this work, we studied the capability of nano-Köhler theory to describe the growth of atmospheric clusters by simulating the dynamics of a cluster population in the presence of a sulfuric acid–base mixture and an oxidized organic compound. We found that nano-Köhler-type behavior occurs when the saturation ratio $S_{\text{ORG}}$ of the organic vapor and the ratio $C_{\text{ORG}}/C_{\text{SA}}$ between organic and inorganic vapor concentrations are in the correct range, for the used model parameters at $C_{\text{ORG}}/C_{\text{SA}} = \sim 10^{-10000}$ and $S_{\text{ORG}} = \sim 4-40$. When $S_{\text{ORG}}$ and $C_{\text{ORG}}/C_{\text{SA}}$ are lower than these values, sulfuric acid dominates the growth at the studied sizes, whereas with the larger values the organic compound dominates. However, it must be kept in mind that the quantitative results depend on the exact vapor and cluster properties. The conditions in which we observe nano-Köhler-type behavior can also occur in the atmosphere: in boreal forests, $C_{\text{SA}}$ is typically $\sim 10^6 \text{ cm}^{-3}$ during NPF events (Petäjä et al., 2009), and $C_{\text{ORG}}$ is likely between $\sim 10^5$ and $10^8 \text{ cm}^{-3}$ (Jokinen et al., 2017), which would result in $S_{\text{ORG}} = \sim 0.04-40$ with $p_{\text{sat, ORG}} = 10^{-8} \text{ Pa}$ and $S_{\text{ORG}} = \sim 40-40 \times 10^3$ with $p_{\text{sat, ORG}} = 10^{-11} \text{ Pa}$.

Although nano-Köhler-type activation occurs in our simulations, nano-Köhler theory is too simple to predict the exact size at which the organic vapor starts to significantly condense on the clusters. This observation demonstrates that the growth of sub-3 nm clusters can be described accurately only if the whole cluster distribution with a variety of different cluster composition and sizes is taken into account. Especially when vapor saturation ratios are high, cluster–cluster collisions contribute substantially to the growth in addition to vapor monomers.

Finally, we also observed that in the simulations with nano-Köhler-type behavior, apparent cluster GRs start to increase close to the size at which the organic vapor starts to dominate the growth. However, such behavior of GR may also be due to other dynamic processes, such as varying vapor concentrations, and therefore one should not make conclusions about the cluster growth mechanism solely based on GR. To accurately determine the initial growth mechanisms and the participating compounds would ideally require (1) quantitative measurements of the composition of sub-3 nm clusters and (2) improved understanding of cluster thermodynamics, including composition and size-dependent evaporation rates. Combined with cluster population modeling, such assessments will be able to provide a more comprehensive understanding of the clustering processes.
Code and data availability. Model simulations were performed using Atmospheric Cluster Dynamics Code (ACDC). The code and the simulated data are available upon request from the authors.
Figure A1. Contribution of different vapor monomers and clusters to the net flux past certain threshold sizes in simulations with SA–DMA and an organic compound (ORG) with $p_{\text{sat}} = 10^{-7}$ Pa at $C_{SA} = 10^7$ cm$^{-3}$ and $C_{ORG} = 10^7$–$10^{10}$ cm$^{-3}$. The values are at steady state.

Figure A2. Contribution of different vapor monomers and clusters to the net flux past different threshold sizes in simulations with SA–DMA and an organic compound (ORG). The vapor concentrations and the saturation ratio of the organic compound ($S_{ORG}$) are shown above the figures for each simulation. The values are at steady state.
Figure A3. Contribution of different vapor monomers and clusters to the net flux past different threshold sizes in simulations with SA–NH$_3$ and LVOC at $C_{SA} = 10^6$ cm$^{-3}$ and $C_{ORG} = 10^6$–$10^9$ cm$^{-3}$. The values are at steady state.

Figure A4. GRs determined for different size bins in simulations with SA–NH$_3$ and LVOC. The colors indicate vapor concentrations in each simulation.
Figure A5. Contribution of different vapor monomers and clusters to the net flux past certain threshold sizes in simulations with SA–DMA and an organic compound with $p_{\text{sat}} = 10^{-8}$ Pa and $m = 600$ amu (LVOC$\text{large}$) at $C_{\text{SA}} = 10^6$ cm$^{-3}$ and $C_{\text{ORG}} = 10^6$–$10^9$ cm$^{-3}$. The values are at steady state.

Figure A6. GRs determined for different size bins in simulations with SA–DMA and an organic compound with $p_{\text{sat}} = 10^{-8}$ Pa and $m = 600$ amu (LVOC$\text{large}$). The colors indicate vapor concentrations in each simulation.
Figure A7. The net flux caused by different vapor monomers and clusters past certain threshold sizes in the simulations with time-dependent concentrations of SA–DMA and LVOC. The left and right panels correspond to the left and right panels in Fig. 10.
Author contributions. JK, TO, IR and MK planned the model simulations and JK performed them. JK prepared the manuscript with contributions from all co-authors.

Competing interests. The authors declare that they have no conflict of interest.

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References


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