Inverse modeling of GOSAT-retrieved ratios of total column CH$_4$ and CO$_2$ for 2009 and 2010

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Abstract. This study investigates the constraint provided by greenhouse gas measurements from space on surface fluxes. Imperfect knowledge of the light path through the atmosphere, arising from scattering by clouds and aerosols, can create biases in column measurements retrieved from space. To minimize the impact of such biases, ratios of total column retrieved CH$_4$ and CO$_2$ ($X_{\text{ratio}}$) have been used. We apply the ratio inversion method described in Pandey et al. (2015) to retrievals from the Greenhouse Gases Observing Satellite (GOSAT). The ratio inversion method uses the measured $X_{\text{ratio}}$ as a weak constraint on CO$_2$ fluxes. In contrast, the more common approach of inverting proxy CH$_4$ retrievals (Frankenberg et al., 2005) prescribes atmospheric CO$_2$ fields and optimizes only CH$_4$ fluxes.

The TM5–4DVAR (Tracer Transport Model version 5–variational data assimilation system) inverse modeling system is used to simultaneously optimize the fluxes of CH$_4$ and CO$_2$ for 2009 and 2010. The results are compared to proxy inversions using model-derived CO$_2$ mixing ratios ($X_{\text{CO}_2^{\text{model}}}$) from CarbonTracker and the Monitoring Atmospheric Composition and Climate (MACC) Reanalysis CO$_2$ product. The performance of the inverse models is evaluated using measurements from three aircraft measurement projects. $X_{\text{ratio}}$ and $X_{\text{CO}_2^{\text{model}}}$ are compared with TCCON retrievals to quantify the relative importance of errors in these components of the proxy XCH$_4$ retrieval ($X_{\text{CH}_4^{\text{proxy}}}$). We find that the retrieval errors in $X_{\text{ratio}}$ (mean = 0.61 %) are generally larger than the errors in $X_{\text{CO}_2^{\text{model}}}$ (mean = 0.24 and 0.01 % for CarbonTracker and MACC, respectively). On the annual timescale, the CH$_4$ fluxes from the different satellite inversions are generally in agreement with each other, suggesting that errors in $X_{\text{CO}_2^{\text{model}}}$ do not limit the overall accuracy of the CH$_4$ flux estimates. On the seasonal timescale, however, larger differences are found due to uncertainties in $X_{\text{CO}_2^{\text{model}}}$, particularly over Australia and in the tropics. The ratio method stays closer to the a priori CH$_4$ flux in these regions, because it is capable of simultaneously adjusting the CO$_2$ fluxes. Over tropical South America, comparison to independent measurements shows that CO$_2$ fields derived from the ratio method are less realistic than those used in the proxy method. However, the CH$_4$ fluxes are more realistic, because the impact of unaccounted systematic uncertainties is more evenly distributed between CO$_2$ and CH$_4$. The ratio inver-
sion estimates an enhanced CO$_2$ release from tropical South America during the dry season of 2010, which is in accordance with the findings of Gatti et al. (2014) and Van der Laan et al. (2015).

The performance of the ratio method is encouraging, because despite the added nonlinearity due to the assimilation of $X_{\text{ratio}}$ and the significant increase in the degree of freedom by optimizing CO$_2$ fluxes, still consistent results are obtained with respect to other CH$_4$ inversions.

1 Introduction

Detailed knowledge of the global distribution of surface fluxes of potent greenhouse gases (GHGs) such as CH$_4$ and CO$_2$ is needed to investigate the uncertain feedback of the global carbon cycle to human disturbances. Atmospheric measurements of these GHGs can provide information about the atmospheric budget. Inverse modeling methods, also known as top-down approaches, have been developed to make use of that information to obtain improved estimates of surface fluxes. Bottom-up estimates of those fluxes are used as prior values in the top-down method, and are further improved using atmospheric measurements. Inversions assimilating flask and/or in situ measurements from surface networks have significantly improved our knowledge of the sources and sinks of GHGs (Bousquet et al., 2006; Bergamaschi et al., 2010; Hein et al., 1997; Houweling et al., 1999; Peters et al., 2007; Chevallier et al., 2010; Gurney et al., 2008). However, many regions with a key role in the global annual budgets of CO$_2$ and CH$_4$ are not adequately covered by the surface measurement network. This is especially true for tropical regions and the Southern Hemisphere.

The Greenhouse Gases Observing SATellite (GOSAT) is the first satellite dedicated to monitoring GHGs from space (Kuze et al., 2009; Yokota et al., 2009; Yoshida et al., 2011). Onboard are the Thermal And Near infrared Sensor for carbon Observation-Fourier Transform Spectrometer (TANSO-FTS) and a dedicated Cloud and Aerosol Imager (TANSO-CAI). TANSO-FTS measures the absorption spectra of Earth-reflected sunlight in the shortwave infrared (SWIR) spectral range, from which XCO$_2$ and XCH$_4$ are retrieved with global coverage. Several inverse modeling studies have applied these measurements to derive constraints on the surface fluxes of CH$_4$ and CO$_2$ (Alexe et al., 2015; Basu et al., 2013; Deng et al., 2014; Maksyutov et al., 2012; Bergamaschi et al., 2013; Fraser et al., 2013; Houweling et al., 2015; Monteil et al., 2013; Turner et al., 2015).

Systematic errors in satellite retrievals are an important factor limiting the scientific interpretation of the data, and various methods have been proposed to mitigate their impact on the inferred surface fluxes (Bergamaschi et al., 2007; Frankenberg et al., 2005; Butz et al., 2010; Parker et al., 2015). An important source of systematic error is the scattering of light by aerosols and thin cirrus clouds along the measured light path. Two types of retrieval methods have been developed in the past to account for atmospheric scattering, referred to as the full-physics and proxy approach. The full-physics approach tries to account for scattering-induced errors by explicitly modeling the scattering process, and retrieving scattering properties from the data (Butz et al., 2010). The proxy method, first introduced by Frankenberg et al. (2005), takes the ratio of XCH$_4$ and XCO$_2$ retrieved at nearby wavelengths (1562 to 1585 nm for XCO$_2$ and 1630 to 1670 nm for XCH$_4$) so that path length perturbations due to atmospheric scattering largely cancel out in the ratio (see Eq. 1). $X_{\text{ratio}}$ is multiplied with model-derived XCO$_2$ (XCO$_2^{\text{model}}$) to derive XCH$_4$ ($X_{\text{CH}_4}^{\text{proxy}}$) (see Eq. 2).

$$X_{\text{ratio}} = \frac{X_{\text{CH}_4}^{\text{ns}}}{X_{\text{CO}_2}^{\text{ns}}}$$

$$X_{\text{CH}_4}^{\text{proxy}} = X_{\text{ratio}} \times X_{\text{CO}_2}^{\text{model}}$$
surface fluxes of CH₄ and CO₂ on the model grid scale using a variational optimization method. Fraser et al. (2014) compared posterior CH₄ and CO₂ flux uncertainties derived from a ratio inversion with traditional CH₄ proxy and CO₂ full-physics inversions and reported a larger reduction in uncertainty than the two in the tropics for the fluxes of both tracers.

This study extends the work of Pandey et al. (2015), by separately inverting real GOSAT measurements of X_ratio and XCH₄_proxy in a consistent and comparable framework to investigate the following questions. (1) How do errors in XCO₂/CH₄ influence the results of a XCH₄_proxy inversion? (2) How does the X_ratio inversion system developed by Pandey et al. (2015) perform using real data? The performance of the inversions is evaluated using independent aircraft measurements. We provide an estimate of the posterior uncertainties of the X_ratio-inverted fluxes using the Monte Carlo method described by Chevallier et al. (2007).

This paper is organized as follows. The following section explains the methods used in this study. Section 2.1 describes the inverse model and the a priori flux assumptions. Section 2.2 lists the measurements that are assimilated in the inversions and used for validation. Section 2.3 provides an overview of the inversions performed in the study. Section 3 presents the inversion results and Sect. 4 discusses their implications for the use of satellite retrievals in inversion studies. Finally, we give the overall conclusions of this work.

2 Method

We invert GOSAT retrievals of X_ratio and XCH₄_proxy, each together with flask-air CH₄ and CO₂ measurements from the NOAA Global Greenhouse Gas Reference Network (GGGRN) to provide monthly surface fluxes of CO₂ and CH₄ using the TM5–4DV AR inversion system (Meirink et al., 2008). This is done as follows.

1. GOSAT-retrieved total column measurements of X_ratio are compared to measured ratios of XCH₄ : XCO₂ from the Total Carbon Column Observing Network (TCCON) of ground-based sun-tracking Fourier transform spectrometers (FTSs) (Wunch et al., 2011).

2. GOSAT X_ratio measurements are bias corrected by fitting a linear function of surface albedo to the residual differences between GOSAT and TCCON. This is done in X_ratio space.

3. GOSAT X_ratio measurements are multiplied by XCO₂/CH₄ to generate XCH₄_proxy measurements. Two different versions of XCO₂/CH₄ are used (see Sect. 2.2) to investigate the sensitivity to model errors.

4. The XCH₄_proxy and X_ratio measurements are inverted along with surface observations and the resulting posterior surface fluxes are integrated over the TransCom regions (see Fig. S4 in the Supplement).

5. The posterior flux uncertainty for all inversions is quantified using a Monte Carlo approach (see Appendix B) for consistent comparison.

6. The performance of the inversions is evaluated and compared using independent aircraft measurements.

The remainder of this section explains these steps in further detail.

2.1 Inversion setup

We use the TM5–4DVAR inversion modeling system. It is comprised of the Tracer Transport Model version 5 (TM5; Krol et al., 2005) coupled to a variational data assimilation system (4DVAR; Meirink et al., 2008). TM5 simulates the spatiotemporal distribution of a tracer in the atmosphere for a given set of fluxes. In this study, TM5 is run at a 6° × 4° horizontal resolution and 25 vertical hybrid sigma pressure levels from the surface to the top of the atmosphere. The meteorological fields for this offline model are taken from the European Centre for Medium-Range Weather Forecasts (ECMWF) ERA-Interim reanalysis (Dee et al., 2011).

CH₄ fluxes are optimized as a single flux category, representing the sum of all processes. For CO₂, biospheric and oceanic fluxes are optimized separately. The a priori CH₄ fluxes used in the study are the same as used in Houweling et al. (2014), except for the anthropogenic fluxes. We use the v.4.2FT2010 version of EDGAR (European Commission, Joint Research Centre (JRC)/Netherlands Environmental Assessment Agency), whereas Houweling et al. (2014) use version 4.1. The a priori CO₂ fluxes come from CarbonTracker, CT2013B (Peters et al., 2007), in which biosphere fluxes are based on the Carnegie-Ames-Stanford Approach (CASA) biogeochemical model, fire fluxes are based on the Global Fire Emissions Database v3.1 (GFED), and ocean fluxes are based on Jacobson et al. (2007). Fossil fuel fluxes in CarbonTracker are based on the Miller module (Tans et al., 2014). The a priori flux covariance matrix is constructed assuming relative flux uncertainties of 50, 84, and 60% per grid box and month for the total CH₄, biospheric CO₂, and oceanic CO₂ categories, respectively. The fluxes are assumed to be correlated temporally using an exponential correlation function with temporal scales of 3, 3, and 6 months, respectively, and spatially with Gaussian functions using corresponding length scales of 500, 500, and 3000 km for total CH₄, biospheric CO₂, and oceanic CO₂, respectively.

2.2 Measurements

Here we give a brief account of the measurements that were assimilated (GOSAT and NOAA) or used for validation (TCCON and aircraft measurements).
2.2.1 GOSAT

The $X_{\text{CH}_4}$ and $X_{\text{CO}_2}$ terms in Eq. (1) were taken from the RemoTeC $X_{\text{CH}_4}$ Proxy retrieval v2.3.5 (Butz et al., 2011). More information about the data set can be found in the Product User Guide on the ESA GHG CCI website (Detmers and Hasekamp, 2014). The RemoTeC algorithm uses GOSAT TANSO-FTS NIR and SWIR spectra to retrieve $X_{\text{CH}_4}$ and $X_{\text{CO}_2}$ simultaneously, assuming a non-scattering atmosphere (Schepers et al., 2012). $X_{\text{ratio}}$ values were translated into $X_{\text{CH}_4}^{\text{proxy}}$ using $X_{\text{CO}_2}^{\text{model}}$ derived from the following: (1) Monitoring Atmospheric Composition and Climate (MACC) reanalysis CO$_2$ product (www.copernicus-atmosphere.eu). It uses Laboratoire de Météorologie Dynamique transport model (LMDZ) (Chevallier, 2013). The corresponding $X_{\text{CH}_4}^{\text{proxy}}$ product will be referred to as $X_{\text{CH}_4}^{\text{ma}}$. (2) $X_{\text{CO}_2}^{\text{model}}$ is derived from CarbonTracker-2013B (http://www.esrl.noaa.gov/gmd/ccgg/carbontracker/). These CO$_2$ fields are calculated using the TM5 model as used in this study. The corresponding $X_{\text{CH}_4}^{\text{proxy}}$ product will be referred to as $X_{\text{CH}_4}^{\text{ct}}$.

Both data assimilation systems optimized the CO$_2$ fluxes using surface measurements of CO$_2$. For GOSAT measurements, we only used the high-gain soundings from GOSAT under cloud-free conditions from nadir mode. This was done to avoid any systematic inconsistency among the operation modes of TANSO. Figure 1 shows the spatial coverage of the GOSAT data set used in our inversions.

Systematic mismatches between NOAA-optimized and GOSAT-optimized TM5 CH$_4$ fields were observed by Mon-
observations were used from the same 51 sites. Figure 1 shows the location of the observation sites. 1σ uncertainties of 0.25 ppm and 1.4 ppb were assigned to CO₂ and CH₄ measurements, respectively (Basu et al., 2013; Houweling et al., 2014). Note that our system also assigns a modeling error to each observation depending on simulated local gradients in mixing ratio (Basu et al., 2013). Modeling error values have a mean of 27.5 ppb, 2.72 ppm (and 1σ of 25.5 ppb, 4 ppm) for CH₄ and CO₂, respectively.

### 2.2.4 Aircraft measurements

Airborne measurements from various aircraft measurement projects were used to test the inversion optimized model (see Sect. 3.2.5). The following projects have been used:

1. HIAPER Pole-to-Pole Observations (HIPPO) from Wofsy et al. (2012a);
2. Comprehensive Observation Network for TRace gases by AIrLiner (CONTRAIL) from Machida et al. (2008);
3. IPEN aircraft measurements over Brazil (referred as AMAZONICA) from Gatti et al. (2014).

HIPPO provides in situ measurements covering the vertical profiles of CO₂ and CH₄ over the Pacific, spanning a wide range in latitude (approximately pole-to-pole), from the surface up to the tropopause. We used data from the HIPPO 2 (26 October to 19 December 2009) and HIPPO 3 (20 March to 20 April 2010) campaigns. The continuous in situ measurements of CH₄ and CO₂ that were used have been bias corrected with flask-air samples that were collected during each flight and analyzed at NOAA (Wofsy et al., 2012b).

This allows us to make consistent comparison with our inversions models, as all of them assimilate NOAA flask measurements. CONTRAIL makes use of commercial airlines to measure in situ CO₂ by continuous measurement equipment. For some of the CONTRAIL flights CH₄ measurements are also available from flask-air samples. We use data from a lower-troposphere greenhouse-gas sampling program as part of the AMAZONICA project, over the Amazon Basin in 2010, measuring biweekly vertical profiles of CO₂ and CH₄ from above the forest canopy to 4.4 km above sea level at four locations: Tabatinga (TAB), RioBranco (RBA), Alta Floresta (ALF), and Santarem (SAN) (Gatti et al., 2014). The coverage of all aircraft measurements that were used in this study is shown in Fig. 1.

### 2.3 Inversion experiments

The following inversions have been performed:

1. SURF: inversions assimilating flask-air measurements of CH₄ or CO₂ to constrain surface fluxes of CH₄ or CO₂, respectively;
2. RATIO: inversion assimilating X₈ ratio and flask-air measurements of CH₄ and CO₂ to constrain surface fluxes of CH₄ and CO₂;
3. PR-MA: inversion assimilating proxy XCH₄ proxy and flask-air measurements of CH₄ to constrain surface fluxes of CH₄;
4. PR-CT: inversion assimilating proxy XCH₄ proxy and flask-air measurements of CH₄ to constrain surface fluxes of CH₄.

Table 1. TCCON validation of the components of XCH₄ proxy (see Eq. 2). The numbers represent mean percentage differences with TCCON (weighted with TCCON + GOSAT error). A negative number means that the satellite retrieval is lower than TCCON. Data from these stations were used: Sodankylä (Kivi et al., 2014), Białystok (Deutscher et al., 2014a), Bremen (Deutscher et al., 2014b), Garmisch (Sussmann and Rettinger, 2014), Karlsruhe (Hase et al., 2014), Parkfalls (Wennberg et al., 2014a), Orleans (Warneke et al., 2014), Tsukuba (Morino et al., 2014), Lamont (Wennberg et al., 2014b), Darwin (Griffith et al., 2014a), Lauder (Sherlock et al., 2014), and Wollongong (Griffith et al., 2014b), and are arranged from north to south (for TCCON site locations, see Fig. 1).

<table>
<thead>
<tr>
<th>Station</th>
<th>No. of collocated measurements</th>
<th>Mean differences with TCCON (%)</th>
<th>XCO₂ ns</th>
<th>XCH₄ ns</th>
<th>X₈ ratio</th>
<th>XCO₂ ct</th>
<th>XCO₂ ma</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sodankylä</td>
<td>434</td>
<td>–3.03</td>
<td>–2.81</td>
<td>0.21</td>
<td>0.68</td>
<td>0.34</td>
<td></td>
</tr>
<tr>
<td>Białystok</td>
<td>731</td>
<td>–2.46</td>
<td>–1.79</td>
<td>0.62</td>
<td>0.31</td>
<td>0.05</td>
<td></td>
</tr>
<tr>
<td>Bremen</td>
<td>426</td>
<td>–1.81</td>
<td>–0.99</td>
<td>0.76</td>
<td>–0.05</td>
<td>–0.32</td>
<td></td>
</tr>
<tr>
<td>Garmisch</td>
<td>1295</td>
<td>–1.93</td>
<td>–1.09</td>
<td>0.76</td>
<td>0.40</td>
<td>0.05</td>
<td></td>
</tr>
<tr>
<td>Karlsruhe</td>
<td>1244</td>
<td>–1.74</td>
<td>–1.00</td>
<td>0.69</td>
<td>0.15</td>
<td>–0.25</td>
<td></td>
</tr>
<tr>
<td>Parkfalls</td>
<td>2174</td>
<td>–1.23</td>
<td>–0.43</td>
<td>0.75</td>
<td>0.22</td>
<td>0.11</td>
<td></td>
</tr>
<tr>
<td>Orleans</td>
<td>808</td>
<td>–1.53</td>
<td>–0.75</td>
<td>0.75</td>
<td>0.21</td>
<td>–0.09</td>
<td></td>
</tr>
<tr>
<td>Tsukuba</td>
<td>135</td>
<td>–1.87</td>
<td>–1.24</td>
<td>0.63</td>
<td>0.57</td>
<td>–0.03</td>
<td></td>
</tr>
<tr>
<td>Lamont</td>
<td>5617</td>
<td>–0.73</td>
<td>–0.03</td>
<td>0.68</td>
<td>0.07</td>
<td>–0.00</td>
<td></td>
</tr>
<tr>
<td>Darwin</td>
<td>1065</td>
<td>–0.67</td>
<td>–0.19</td>
<td>0.47</td>
<td>0.02</td>
<td>0.14</td>
<td></td>
</tr>
<tr>
<td>Lauder</td>
<td>110</td>
<td>–1.05</td>
<td>–0.57</td>
<td>0.46</td>
<td>0.14</td>
<td>0.03</td>
<td></td>
</tr>
<tr>
<td>Wollongong</td>
<td>1515</td>
<td>–0.81</td>
<td>–0.45</td>
<td>0.35</td>
<td>0.10</td>
<td>0.00</td>
<td></td>
</tr>
</tbody>
</table>
To assess the relative performance of each inversion, we validate atmospheric concentrations as simulated using the optimized fluxes from the different inversions with aircraft measurements. We define a normalized chi-square statistic to quantify the agreement between the optimized model and aircraft measurements.

\[ \kappa = \frac{1}{n} (y - Hx)^T R^{-1} (y - Hx), \]

where \( y \) is a vector of the aircraft measurements, \( n \) is the length of \( y \), \( Hx \) is the TM5 simulation sampled at the measurement coordinates. The covariance matrix \( R \) represents the expected uncertainty in the model–data mismatch. Its diagonal elements are calculated as the sum of the model representation error of TM5 and the measurement uncertainty; all non-diagonal elements are set to 0.

3 Results

3.1 GOSAT–TCCON comparison

TCCON measurements are used to investigate the errors in GOSAT-retrieved XCH₄. Each term on the right-hand side of Eq. (2) contributes to the uncertainty in XCH₄ proxy. To quantify these error contributions, we compare TCCON measurements of XCH₄ proxy with co-located GOSAT-retrievals. The validation is carried out for the time period of 1 June 2009 to 31 December 2013, for which both proxy data sets (XCH₄ proxy and XCH₄) are available. Table 1 shows mean differences per TCCON station, expressed as fractional differences to facilitate the comparison of quantities with different units. As expected, the largest differences between GOSAT and TCCON are found for XCO₂ and XCH₄ proxy. In general, XCO₂ proxy (mean = -1.57 %) shows larger relative differences than XCH₄ proxy (mean = -0.95 %). A latitudinal dependence can be observed, with increasing biases towards stations at higher latitudes. This can be explained by increased aerosol scattering at larger sun angles, as the light path through the atmosphere is longer. For all the stations, the mean difference is negative which is expected for aerosol scattering-induced errors at the low surface albedos of the TCCON sites (Houweling et al., 2004). The smaller bias values for XCH₄ proxy than XCO₂ proxy and XCH₄ proxy confirm that scattering-induced errors cancel out in their ratio, which motivated the proxy approach (Frankenberg et al., 2005). Overall, we observe that Xratio (mean bias = 0.59 %) is the larger contributor to the error in XCH₄ proxy than MACC (XCO₂ proxy, mean bias = 0.01 %) and CarbonTracker (XCO₂, mean bias = 0.24 %).

3.2 Inversion results

3.2.1 Assimilation statistics

Figure 2 summarizes the statistics of the model–measurement comparison. The prior Xratio mismatches typically fall in the range ±1 % (with mean = 0.007 ppb/ppm and 1σ = 0.043 ppb/ppm). The inversions reduce the average mismatch by about a factor of 10, and the variation of single column mismatches by about a factor of 2. The XCH₄ proxy of PR-CT and PR-MA have bimodal prior mismatches, because the a priori model overestimates the north–south gradient of CH₄. The bottom panels of Fig. 2 show mismatches between TM5 and surface flask measurements of CH₄ and CO₂. The CH₄ a priori measurement mismatch has a mean of -18.30 ppb and a 1σ of 42.30 ppb. The RATIO, SURF, PR-CT, and PR-MA inversions are all able to fit the NOAA data to a similar extent, reducing the a priori differences by more than a factor of 20. CO₂ flask measurements are assimilated in SURF and RATIO. Both inversions reduce the a priori mismatch (mean = -2.12 ppm, 1σ = 3.88 ppm), with RATIO (mean = -0.04 ppm, 1σ = 3.69 ppm) fitting.
the CO$_2$ flask data as well as SURF (mean = −0.06 ppm, 1σ = 3.72 ppm).

### 3.2.2 CH$_4$ fluxes

Optimized annual CH$_4$ fluxes, integrated over the TransCom regions are shown in the left panel of Fig. 3. The fluxes obtained with the RATIO inversion are on average more similar to fluxes from other GOSAT inversions than to the surface inversion, with a few exceptions. Differences between satellite and surface inversion are most prominent over tropical South America, where the latter is closer to the prior, which can likely be explained by the lack of surface measurement coverage. We will return to the inversion results for tropical South America in Sect. 3.2.6, where validation results are shown using aircraft data.

The most significant difference between the satellite inversion and SURF is found for temperate Eurasia, where SURF reduces the CH$_4$ fluxes from 121 Tg y$^{-1}$ in the prior estimate to 66 Tg y$^{-1}$. When satellite data are added, the fluxes increase again to 100 Tg y$^{-1}$. The large flux correction in the SURF inversion is compensated by increases in other TransCom regions of 5–10 Tg y$^{-1}$ (see for example temperate North and South America). In those regions satellite inversions remain closer to the prior than the SURF inversion, which may well be driven by the much smaller flux corrections for temperate Eurasia. The exception is Europe, where the satellite inversions show larger reductions of up to 15 Tg y$^{-1}$. The large adjustments over temperate Eurasia are analyzed further in Sect. 3.2.7. PR-CT and PR-MA result in relatively similar posterior annual fluxes for all regions. RATIO is in good agreement with the proxy inversions except for tropical South America and southern Africa. The right panel of Fig. 3 shows annual fluxes integrated over large regions on the globe. We find a consistent adjustment in the north–south gradient of CH$_4$ compared to the prior in all inversions, corresponding to a flux shift from the Northern to the Southern Hemispher of approximately 50 Tg y$^{-1}$. This might be due to an overestimation of the a priori fluxes from northern wetlands, as discussed in Spahni et al. (2011). A bias in inter-hemispheric transport in TM5 is not a likely cause, since the use of ECMWF-archived convective fluxes in TM5 has been shown to lead to a realistic simulation of the north–south gradient of SF6 (Van der Laan et al., 2015). Houweling et al. (2014) found similar CH$_4$ flux shifts between the hemispheres, after bringing the inter-hemispheric transport in agreement with SF6 using a parameterization of horizontal diffusion.

Next we shift focus to seasonal differences between the inversion-derived methane fluxes (see Fig. 4). Also on the seasonal scale, RATIO resembles the two PROXY inversions more than SURF. In boreal North America, the satellite inversions that assimilate GOSAT soundings are in better agreement with the prior. We observe an increase in summertime CH$_4$ fluxes in SURF estimates for boreal and temperate North America. The differences in annual mean fluxes discussed earlier for tropical South America and temperate Eurasia do not show a seasonal dependence. Large differences in seasonality are obtained for Australia and the African regions, which also show important differences between the two proxy inversions (see Sect. 3.2.4). In southern Africa, all inversions show increased CH$_4$ fluxes compared to the prior estimate; however, small differences can be seen between the two proxy inversions, especially in 2010. SURF remains in good agreement with PRIOR (a priori fluxes), which is expected as no surface observations are available to constrain the fluxes in this region.

### 3.2.3 CO$_2$ fluxes

Annual CO$_2$ fluxes from the SURF and RATIO inversions, integrated over TransCom regions, are shown in Fig. 5. Overall, we find good consistency between the results from RATIO and SURF except for temperate Eurasia, where RATIO results in a higher CO$_2$ uptake of 0.5 PgC y$^{-1}$. Corresponding reductions in CH$_4$ fluxes are found for this region in the RATIO inversion. This can be understood by realizing that the satellite information that is used consists of the ratio of
Figure 4. Monthly fluxes of CH$_4$ integrated over TransCom regions. The vertical lines represent a 1σ uncertainty of the monthly fluxes. The gray region in each plot represents the period in which no measurements are assimilated.

Figure 5. Annual fluxes of CO$_2$ (excluding fossil fuel emissions) integrated over different regions.
CH$_4$ and CO$_2$ columns. A RATIO inversion can simultaneously reduce the CO$_2$ and CH$_4$ fluxes over a region without changing the X$_{\text{ratio}}$ in the atmosphere. SURF points towards a natural sink of 0.5 PgC y$^{-1}$ in boreal North America. RATIO and the a priori fluxes are carbon-neutral in this region. This agreement is also seen on the CH$_4$ side of the RATIO inversion. Only small differences between the posterior and prior fluxes of SURF and RATIO are found over the oceans except for the temperate North Pacific, which is neutral in both inversions compared to a sink of $-0.5$ PgC y$^{-1}$ in the prior fluxes, and in tropical India which is turned into a net sink. Interestingly, RATIO leads to posterior fluxes for Europe that are close to carbon-neutral for the analysis period. This is in contrast with the findings of several inversions using GOSAT full physics XCO$_2$ retrievals, suggesting a largely underestimated European carbon sink of the order of 1 PgC y$^{-1}$ (Basu et al., 2014; Chevallier et al., 2014; Reuter et al., 2014; Houweling et al., 2015).

The RATIO and SURF inversions increase the global CO$_2$ sink of the terrestrial biosphere compared to the a priori fluxes. This is primarily caused by the bottom-up CASA model, which has been reported to underestimate the carbon uptake of the northern biosphere sink in the summer season (Yang et al., 2007). Basu et al. (2013) also find a global natural sink of 3 to 4 PgC y$^{-1}$ for GOSAT and NOAA inversions. This natural sink is needed to fit the atmospheric growth rate of CO$_2$ in the presence of about 9 PgC y$^{-1}$ anthropogenic emissions. The Southern Hemisphere land is turned into a source of 1 PgC y$^{-1}$ in both inversions.

3.2.4 Errors in CO$_2$ model

In this section, we analyze the differences between the two proxy retrievals (XCH$_4$$_{\text{proxy}}$ and XCH$_4^{\text{ma}}$) and how they propagate into posterior CH$_4$ fluxes. Note that these differences arise only from differences in XCO$_2$$_{\text{model}}$, and therefore large differences between the XCH$_4$$_{\text{proxy}}$ measurements point towards high uncertainties in the model representations of atmospheric CO$_2$. Figure 6 further displays the result of these inversions. We find a mean difference between XCH$_4^{\text{ma}}$ and XCH$_4^{\text{ct}}$ of $-2.36$ ppb and a $\sigma$ of 4.55 ppb. This is caused by mean differences between XCO$_2^{\text{ma}}$ and XCO$_2^{\text{ct}}$ of $-0.50$ ppm and a $\sigma$ of 0.97 ppm (not shown in the figure). We find a seasonal variation in the difference with the largest amplitudes of about 10 ppb in the northern tropics. The phasing varies with latitude, with positive values during boreal summer to autumn. The smallest differences are found in the Southern Hemisphere. Figure 6b shows how this seasonal pattern propagates into the posterior CH$_4$ fluxes. The seasonal and latitudinal variation in the CH$_4$ flux difference follows the variation in the XCH$_4$$_{\text{proxy}}$ difference, with an amplitude of 0.5 Tg month$^{-1}$ gridded$^{-1}$. The regions without satellite data coverage, i.e., below 60° S and above 60° N, show smaller differences in the optimized fluxes.

PR-CT and PR-MA yield different CH$_4$ fluxes in northern Africa and Australia (see Fig. 4). We plot these fluxes with the corresponding regional averaged XCH$_4$ values in Fig. 7. For northern Africa, the difference in XCH$_4$$_{\text{proxy}}$ of up to 10 ppb around January 2010 gives rise to a difference in the monthly posterior flux of 1 Tg month$^{-1}$. In Australia, XCH$_4^{\text{ma}}$ and XCH$_4^{\text{ct}}$ are in relatively good agreement with each other, with differences within 2 ppb. However, because the a priori fluxes from this region are very small, the difference in the optimized seasonal cycle of fluxes nevertheless becomes relatively large. In particular, PR-MA causes significant deviations from the a priori fluxes, with decreases in the posterior fluxes during Australian summer, and large increases during winter. Another reason for these flux adjustments is the limited land area in the Southern Hemisphere that is available for CH$_4$ flux adjustments (over the open ocean the a priori flux uncertainties are small, limiting their adjustment).

Detmers et al. (2015) reported an enhanced CO$_2$ sink over central Australia in the second half of 2010 lasting until 2012, caused by an increase in vegetation due to enhanced precipitation during La Niña conditions. If not properly represented in inversions using surface measurements, this negative CO$_2$ anomaly causes XCO$_2$$_{\text{model}}$ to be overestimated. In that case, the anomaly propagates to the proxy retrievals, resulting in overestimation of XCH$_4$$_{\text{proxy}}$, leading to overestimated a posteriori CH$_4$ fluxes. RATIO estimates a significantly stronger sink of CO$_2$ in agreement with Detmers et al.
validate the inversion-optimized CH$_4$.

3.2.5 Aircraft validation

To further investigate the performance of our inversions, we validate the inversion-optimized CH$_4$ and CO$_2$ mixing ratios against independent aircraft measurements obtained during the projects described in Sect. 2.2. The results of the HIPPO and CONTRAIL validation are shown in Fig. 8 and the values for $\kappa$ for CH$_4$ and the root-mean-square difference (RMSD) for CO$_2$ are given in Fig. 9. $\kappa$ values are not calculated for CO$_2$ because we do not have the CO$_2$ model representation errors used in MACC and CarbonTracker. More details on statistics of the validation are provided in Table S1 in the Supplement.

The difference between HIPPO and PRIOR reflects the overestimated north–south gradient that is found using a priori CH$_4$ fluxes, as already discussed in Sect. 3.2.2. In addition, PRIOR shows a uniform bias of 13.5 ppb. SURF and RATIO correct the north–south gradient and reduce biases to 5.56 and 6.68 ppb, respectively. All the models are performing equally well in terms of $\kappa$. The original MACC and CarbonTracker CO$_2$ fields have RMSD values of 1.08 and 1.09 ppm, respectively, which is lower than the RMSD of RATIO (1.64 ppm) and SURF (1.65 ppm). We suggest that CarbonTracker and MACC have a better representation of CO$_2$ than PR-CT, PR-MA, and SURF as they assimilate a larger number of flask measurements sites and also few continuous in situ sites.

Compared with the large CONTRAIL data set of CO$_2$ measurements, only a limited number of CH$_4$ measurements are available, mostly over the Pacific Ocean (see Fig. 1). We observe the same north–south gradient mismatch with PRIOR as seen in the comparison to HIPPO. PR-CT is able to improve the PRIOR $\kappa$ of 6.99 to 4.56, followed in order of decreasing performance by PR-MA (4.71), SURF (5.33), and RATIO (5.47). The values of $\kappa$ are larger than 1, which points to significant errors in all the inversion results. The RMSD of the different inversions is comparable. The large data set of CONTRAIL CO$_2$ measurements covers a much larger area, including flight tracks to Europe and southeast Asia. Our validation shows a mean error of 2.23 ppm in PRIOR. The NOAA and RATIO inversions reduce this bias to $-0.43$ and $-0.41$ ppm, respectively. However, similar to the HIPPO validation, MACC (mean bias $=-0.2$ ppm) and CarbonTracker-derived CO$_2$ (mean bias $=0.11$ ppm) fields are in better agreement with the CONTRAIL measurements than the inversions.

3.2.6 Tropical South America

Tropical South America contains the Amazon Basin, which is a large reservoir of standing biomass and contains one of the largest wetlands in the world. Therefore, it plays an important role in the annual global budget of both CO$_2$ and CH$_4$. Inversion results for the region have been validated using AMAZONICA measurements (see Fig. S5 and Table S1 in the Supplement). Generally, the model results using PRIOR fluxes underestimate the measured CH$_4$ mixing ratios (mean offset $=-32.02$ ppb). All inversions correct this offset, with SURF performing best (mean mismatch $=-14.18$ ppb). RATIO closely follows SURF with a mean mismatch of $-17.18$ ppb. The proxy inversions have a higher mismatch than RATIO and SURF, with means of $-20.30$ and $-24.11$ ppb, respectively for PR-MA and PR-CT. The $\kappa$ values for the AMAZONICA CH$_4$ measurements (see Fig. 9) again show that fluxes from RATIO lead to lower mismatches than those from PR-CT and PR-MA. RATIO predicts this region as a significantly high CH$_4$ source for the first half of 2010 (see Fig. 4), and is in good agreement with aircraft measurements.

To check whether this is caused by errors in XCO$_2$\textsuperscript{model}, we perform similar comparisons using AMAZONICA CO$_2$.
measurements. We find that the two original models represent CO₂ about equally well in terms of RMSD (see Table S1 in the Supplement). Therefore, the higher mismatch of PR-CT and PR-MA for CH₄ is not due to a poor representation of the XCO₂ model over the region. This raises the question as to why RATIO performs better. In Sect. 3.1, we observe that the error in CO₂ model is generally lower than the error in the GOSAT X ratio retrievals. In proxy inversions, this retrieval error, which is coming from X ratio (see Eq. 2), is directly transferred to CH₄ fluxes, whereas in RATIO it is distributed over the CH₄ and CO₂ part of the state vector. The high posterior CO₂ flux uncertainties for RATIO in the region support this further (see Fig. 5).

Flux maps of the region show that the satellite inversions provide a more spatially resolved adjustment of the CH₄ fluxes than SURF (see Fig. S3 in the Supplement). The satellite inversions estimate higher fluxes in the northwest corner of the region near Colombia. Similar increases have been reported in earlier studies, assimilating satellite-retrieved XCH₄ (Monteil et al., 2013; Frankenberg et al., 2006). The spatial pattern of the flux adjustment suggests that the proxy inversions compensate the increase over Colombia by reducing the fluxes in the Amazon Basin, which is less well covered by satellite retrievals due to frequent cloud cover. This may explain why the proxy inversions end up underestimating the observations inside the basin. SURF is mainly constrained by the large-scale inter-hemispheric gradient. This leads to a different pattern of flux adjustments, increasing only the fluxes in the southern part of the region while keeping the fluxes in Amazon Basin close to the prior. This solution brings SURF in relatively close agreement with the measurements. RATIO also shows a flux enhancement in Colombia, but at the same time represents the Amazon Basin better than the proxy inversions, likely because of its larger number of degrees of freedom in modifying regional flux patterns of both CO₂ and CH₄.

Gatti et al. (2014) and Van der Laan et al. (2015) reported an anomalous natural source of CO₂ in the region in 2010, also using AMAZONICA aircraft measurements. In this
study, RATIO predicts a more enhanced CO$_2$ natural source than the SURF and PRIOR. RATIO (RMSD = 3.23 ppm) is also in better agreement in terms of RMSD with AMAZONICA CO$_2$ data than SURF (RMSD = 3.31 ppm) and PRIOR (3.38 ppm). This demonstrates, like in the case of Australia, that the RATIO method is capable of informing us about the CO$_2$ fluxes, from which the CH$_4$ flux estimation benefits also.

### 3.2.7 Temperate Eurasia

As mentioned in Sect. 3.2.2, SURF leads to a drastic flux reduction in temperate Eurasia, whereas all satellite inversions show comparatively smaller decreases. Here, we investigate this in further detail by analyzing the inversion-optimized fits to the NOAA measurements at five surface sites located in this region (see Fig. 10). We find large mismatches between the a priori simulated concentrations and the measurement at these sites, with mean offsets ranging between 29.1 ppb at Mt. Waliguan and 174 ppb at Shangdianzi. All inversions correct for this mismatch by decreasing the regional fluxes. Surprisingly enough, the satellite inversions are able to fit the flask measurements even better than SURF, despite smaller corrections to the fluxes. For example, the mean posterior mismatch at Shangdianzi is 24.3 ppb for SURF, and only 7.5 to 9.8 ppb for the satellite inversions. A possible explanation is the double counting of surface data in the satellite inversions, as the satellite data have been bias corrected using an inversion that was already optimized using surface data. However, the bias correction is only applied as a zonal and annual mean. All inversions show similar reductions in the fluxes from eastern temperate Eurasia (mostly China) to match the NOAA measurements. However, the satellite inversions tend to compensate for this flux decrease over China by increased fluxes in India and the central part of temperate Eurasia.

4 Discussion

We have demonstrated that the application of the ratio method to GOSAT data yields realistic solutions for CO$_2$ and CH$_4$ fluxes. Its performance is comparable, and may in some regions even be better than the proxy inversion method. This is an important finding because the $X_{ratio}$ retrieval approach provides a useful alternative to the full-physics method in that cloud filtering is less critical. In the case of GOSAT, it increases the number of useful measurements by about a factor of 2 (Butz et al., 2010; Fraser et al., 2014). At the same time, the RATIO inversion method avoids using the model-derived CO$_2$ fields as a hard constraint, which is an important limitation of the proxy method.

The realistic performance of the ratio method is certainly not a trivial outcome, since it prompts the user for specification of new uncertainties, influencing the way in which measurement information is shared between CH$_4$ and CO$_2$. The joint CO$_2$ and CH$_4$ inversion problem has a larger number of degrees of freedom, as a result of which CH$_4$ flux adjustments can compensate for errors in CO$_2$ and vice versa. Assimilating surface measurements helps to decouple CH$_4$ and CO$_2$, which works best in regions that are relatively well covered by the surface network.

In other regions, the method can be improved further by accounting for correlations between a priori fluxes of CH$_4$ and CO$_2$. This study does not specify such correlations, which correspond to the assumption that a priori CO$_2$ and CH$_4$ flux uncertainties are independent of each other. Fraser et al. (2014) accounted for a priori uncertainty correlations for biomass burning fluxes of CO$_2$ and CH$_4$, based on the available information about emission ratios. Imposing such a priori constraints increased posterior uncertainty reduction compared to other methods for both CH$_4$ and CO$_2$ in some regions.

It is noteworthy that the inversions are run assuming uncorrelated measurements and a perfect transport. Also, as we are not optimizing the atmospheric sink of CH$_4$, all the information from its budget is used to constrain the surface fluxes. Hence, the estimates of posterior uncertainties tend to be optimistic in this study. The $\chi^2$ statistic indicates whether the assumed measurement and prior errors are statistically consistent (Meirink et al., 2008). We find $\chi^2/n_s = 0.93$ for RATIO, 0.96 for PR-CT, 0.93 for PR-LM, and 1.14 for SURF in the CH$_4$ inversions ($n_s$ is the number of observations assimilated in the inversion). This shows that we are not drastically underestimating the prior uncertainties in our CH$_4$ inversions.
One problem with the ratio method is the assimilation of $X_{\text{ratio}}$ over oceans. The uncertainty of CH$_4$ fluxes over the open oceans is relatively small. As a result, the model–data mismatch over the ocean is mostly accounted for by adjusting the CO$_2$ fluxes, which has a larger a priori uncertainty. At the same time, CO$_2$ over oceans tend to be very sensitive to small and systematic model–data mismatches of a few tenths of a ppm (Basu et al., 2013). Any bias in atmospheric transport, affecting both CO$_2$ and CH$_4$, is projected on the CO$_2$ fluxes, which may lead to rather unrealistic estimates of the annual CO$_2$ exchange over oceanic regions. Palmer et al. (2006) proposed to account for cross correlations in the model representation error between the components of a dual tracer inversion, which could reduce the extent of this problem.

Our surface-only inversion shows a large decrease in the fluxes from temperature Eurasia. To better understand this, we look at results of other recently published CH$_4$ inversion results. We group the studies into three groups: (1) studies not using EDGAR v4.2 as a priori fluxes, comprising Houweling et al. (2014), Monteil et al. (2013), Bruhwiler et al. (2014), and Fraser et al. (2013); (2) studies using EDGAR v4.2 but not assimilating the Shangdianzi site, comprising Alexe et al. (2015) and Bergamaschi et al. (2013); (3) studies using EDGAR v4.2 and assimilating Shangdianzi site comprising this work and Thompson et al. (2015). The inversions of group 1 do not show a systematic reduction in fluxes of temperate Eurasia. Inversions of group 3 tend to reduce the fluxes from the region the most; whereas, group 2 reduces fluxes by an intermediate amount. This outcome is partly explained by the EDGAR 4.2 fluxes being substantially higher in temperate Eurasia than previous EDGAR versions, as found also by Bergamaschi et al. (2013). In addition, however, these increased fluxes have the largest impact on surface-only inversions assimilating measurements from the Shangdianzi site, possibly due to a nearby hotspot in EDGAR v4.2. The hotspot is located near Jiexiu in the Shanxi province (112$^\circ$ E, 37$^\circ$ N), and has coal emissions of 10.83 Tg y$^{-1}$ for the year 2010 from a 10 $\times$ 10 km grid. According to the EDGAR team (G. Meahnout, personal communication, 2015), this unrealistically high local source of CH$_4$ is the consequence of disaggregating large emission from Chinese coal mining using the limited available information on the location of the coal mines. Thompson et al. (2015), the other study in group 3, show a large a priori mismatch with a root-mean-square error of 103 ppb at Shangdianzi. Their inversions reduce their a priori east Asian CH$_4$ fluxes of 82 Tg y$^{-1}$ by 23 Tg y$^{-1}$, with large adjustments in the fluxes from rice cultivation. Further research is needed to investigate the implications of the shortcomings of EDGAR v4.2. It is noteworthy, however, that when satellite data are assimilated in these studies, the improved regional coverage reduces the impact of this local disaggregation problem on the estimated regional fluxes.

5 Conclusions

This study investigated the use of GOSAT-retrieved $X_{\text{ratio}}$ for constraining the surface fluxes of CO$_2$ and CH$_4$. First, we validated the XCH$_4$, XCO$_2$, and $X_{\text{ratio}}$ retrievals, as well as the model-derived XCO$_2$ fields used in the proxy methods, using TCCON measurements. This analysis confirmed that biases in non-scattering XCH$_4$ and XCO$_2$ retrievals largely cancel out in $X_{\text{ratio}}$. $X_{\text{ratio}}$ has a larger mean bias than model-derived XCO$_2$ from CarbonTracker and MACC, suggesting that mostly retrieval biases, rather than CO$_2$ model errors, limit the performance of the proxy method. This is true, especially at a large temporal and spatial scale. To account for biases in GOSAT-retrieved $X_{\text{ratio}}$, a TCCON-derived correction was applied as a function of surface albedo, resulting in a mean adjustment of $-0.74 \%$. An additional correction was applied to $X_{\text{ratio}}$, XCH$_4$ and XCH$_4^\text{proxy}$ to account for a bias between NOAA-optimized CH$_4$ fields in TM5 and TCCON-observed XCH$_4$, amounting to $-0.76$, $-0.80$, and $0.59 \%$, respectively.

We optimized monthly CH$_4$ and CO$_2$ fluxes for the year 2009 and 2010 by assimilating GOSAT-retrieved $X_{\text{ratio}}$ data using the TM5–4DVAR inverse modeling system. Additional inversions, assimilating XCH$_4^\text{proxy}$ and NOAA surface flask measurements, were performed in a similar setup for comparison. The posterior uncertainties of the fluxes are calculated with a Monte Carlo approach.

Overall, the ratio and proxy inversions show similar results for annual CH$_4$ fluxes. Significant seasonal differences in CH$_4$ are found between the two proxy inversions for TransCom regions northern Africa and Australia, which can be traced back to differences in XCO$_2^\text{model}$. The CO$_2$ models show a systematic difference in the seasonal cycle of CO$_2$, resulting in a seasonally varying mismatch in the northern tropics. The ratio method has the advantage that it allows adjustment of the CO$_2$ fluxes, whereas the proxy inversions can only account for this mismatch by adjusting CH$_4$. For Australia, the proxy inversions predict an anomalous CH$_4$ increase in the second half of 2010. This difference can be explained by errors in XCO$_2^\text{model}$, which does not account for the anomalous carbon sink reported by Detmers et al. (2015) for lack of surface measurement coverage. The ratio method has the built-in flexibility needed to attribute the anomaly to CO$_2$ instead of CH$_4$, and is therefore is not affected.

Inversions using satellite data show a better agreement among each other compared to the NOAA-only inversions, which use only surface data. This is true in particular for temperate Eurasia, where the NOAA-only inversion reduces the annual CH$_4$ flux by as much as 55 Tg y$^{-1}$, relative to an a priori flux of 121 Tg y$^{-1}$. This is traced back to a large overestimation of atmospheric CH$_4$ concentration in the prior model at NOAA sites in the region, especially at Shangdianzi, where the prior model overestimates the data by 179 ppb on average. When satellite measurements are assimilated, the CH$_4$ flux reduction for temperate Eurasia is
limited to 21 Tg y\(^{-1}\), while accounting for the a priori mismatch in Shangdianzi.

We validated the inversion-optimized atmospheric tracer fields, as well as the CarbonTracker and MACC CO\(_2\) fields used in the proxy inversions, against three independent aircraft measurement projects. For CH\(_4\), the ratio and NOAA-only inversions showed a lower mismatch with HIPPO and AMAZONICA measurements than the two proxy inversions. Further analysis shows that this is not due to a better representation of atmospheric CO\(_2\) in the ratio inversion. However, the ratio inversion accounts for inconsistent constraints from X\(_{\text{ratio}}\) by correcting both CH\(_4\) and CO\(_2\) fluxes, whereas the proxy inversions can only attribute such constraints to CH\(_4\) fluxes. The ratio inversion predicts an enhanced CO\(_2\) natural source in this region during 2010 compared with the NOAA-only and a priori model. This is in accordance with the findings of Gatti et al. (2014) and Van der Laan et al. (2015), and is also supported by the AMAZONICA aircraft measurements. Overall, this study shows that the ratio method is capable of informing us about surface fluxes of CH\(_4\) and CO\(_2\) using satellite measurements, and that it provides a useful alternative for the proxy inversion method.

Data availability

Level 2 XCH\(_4\) and X\(_{\text{ratio}}\) data from GOSAT/TANSO are calculated using the RemoTeC algorithm. The data are publicly available from the ESA’s Climate Change Initiative website (http://www.esa-ghg-cci.org/). NOAA’s GGGRN CH\(_4\) measurements are publicly available at ftp://aftp.cmdl.noaa.gov/data/trace_gases/ch4/flask/surface/. CarbonTracker CO\(_2\) fluxes are provided by NOAA ESRL, Boulder, Colorado, USA from the website at http://carbontracker.noaa.gov.
Appendix A: Bias correction

We apply a two-step correction to reduce the influence of biases in our inversions.

1. TCCON-based: residual biases in $X_{\text{ratio}}$ remain that are not accounted for by calculating the ratio between $X_{\text{CH}_4}^{\text{obs}}$ and $X_{\text{CO}_2}^{\text{obs}}$. The standard bias correction procedure in the RemoTeC $X_{\text{CH}_4}^{\text{proxy}}$ retrieval assumes a linear dependence on surface albedo (Guerlet et al., 2013). However, this procedure would also correct biases in $X_{\text{CO}_2}^{\text{model}}$, which are not expected to vary with surface albedo. Therefore, we apply the albedo-based bias correction only to the GOSAT-measured $X_{\text{ratio}}$. To determine the bias correction, we use GOSAT retrievals that are co-located with TCCON measurements; i.e., they are within 5° latitude and longitude and within 2 h of TCCON measurements. The relationship between surface albedo at 1593 nm and the monthly difference between GOSAT and TCCON is shown in Fig. A1. A global bias correction function, obtained by linear regression, results in a mean adjustment of $-0.74\%$ of GOSAT $X_{\text{ratio}}$.

2. NOAA-based: a systematic mismatch between the NOAA and GOSAT-optimized TM5 $\text{CH}_4$ fields has been discussed in Monteil et al. (2013). The cause of this problem is still unresolved, but may be explained in part by transport model uncertainties in representing $X_{\text{CH}_4}$ in the stratosphere. Several other studies have reported similar biases and applied NOAA-based bias corrections, in addition to the TCCON-derived retrieval corrections in order to restore consistency between the observational constraints provided by surface and total column measurements (Alexe et al., 2015; Houweling et al., 2014; Basu et al., 2013). We use a similar procedure for $X_{\text{ratio}}$ and $X_{\text{CH}_4}^{\text{proxy}}$ data by comparing the TCCON-corrected GOSAT retrievals to the NOAA-optimized TM5 model. The mean difference is corrected using a linear function of latitude. This results in a mean adjustment of $-0.76\%$ in $X_{\text{ratio}}$, $-0.59\%$ in $X_{\text{CH}_4}^{\text{ma}}$, and $-0.80\%$ in $X_{\text{CH}_4}^{\text{ct}}$ (see Figs. A2 and A3).

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**Figure A1.** Linear regression analysis between GOSAT–TCCON $X_{\text{ratio}}$ and surface albedo at 1593 nm.

**Figure A2.** NOAA-based bias correction applied to $X_{\text{CH}_4}$ in the PR-CT inversion.

**Figure A3.** NOAA-based bias correction applied to $X_{\text{ratio}}$ in the RATIO inversion.
Appendix B: Posterior uncertainty

As discussed in Pandey et al. (2015), the $X_{\text{ratio}}$ inversion problem is weakly nonlinear and is solved using the quasi-Newtonian optimizer M1QN3. The standard implementation of M1QN3 does not provide an estimate of posterior uncertainties. Therefore, we use the Monte Carlo approach as described in Chevallier et al. (2007) to calculate posterior flux uncertainties. For the linear SURF and proxy inversions, we use the conjugate gradient optimization method. The posterior flux uncertainties of these inversions are derived using the same approach to keep the comparison between the uncertainties consistent. A sensitivity test has been performed to determine the size of the ensemble needed to properly capture the $1\sigma$ of the prior fluxes. Figure B1 shows the results of this experiment. We choose an ensemble size of 24 for our experiments, which gives a $1\sigma$ estimate with 14.4% uncertainty.

Figure B1. The gray lines represent the percentage error of $1\sigma$ of ensemble size $n$ from the $\sigma$ of ensemble size of 200 of the a priori CH$_4$ flux integrated over TransCom regions. The dark black line represents the average deviation in the gray lines. The green line represents the analytical variation of the error of $1\sigma$ (Bousserez et al., 2015). A constant difference of approx. 6% between the estimates comes from the finite size of the largest sample (200).
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