The impact of embedded valleys on daytime pollution transport over a mountain range

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Abstract. Idealized large-eddy simulations were performed to investigate the impact of different mountain geometries on daytime pollution transport by thermally driven winds. The main objective was to determine interactions between plain-to-mountain and slope wind systems, and their influence on the pollution distribution over complex terrain. For this purpose, tracer analyses were conducted over a quasi-two-dimensional mountain range with embedded valleys bordered by ridges with different crest heights and a flat foreland in cross-mountain direction. The valley depth was varied systematically. It was found that different flow regimes develop dependent on the valley floor height. In the case of elevated valley floors, the plain-to-mountain wind descends into the potentially warmer valley and replaces the opposing upslope wind. This superimposed plain-to-mountain wind increases the pollution transport towards the main ridge by an additional 20 % compared to the regime with a deep valley. Due to mountain and advective venting, the vertical exchange is 3.6 times higher over complex terrain than over a flat plain. However, the calculated vertical exchange is strongly sensitive to the definition of the convective boundary layer height. In summary, the impact of the terrain geometry on the mechanisms of pollution transport confirms the necessity to account for topographic effects in future boundary layer parameterization schemes.

1 Introduction

Daytime transport and mixing processes of air pollutants primarily occur within the convective boundary layer (CBL) and are mostly well understood for flat and homogeneous terrain (Steyn et al., 2013). The typical CBL, which forms under fair weather conditions over horizontally homogeneous and flat terrain, consists of a superadiabatic surface layer, a mixed layer (ML), and a stably stratified layer called the entrainment layer (EL); the latter separates the CBL from the free atmosphere (Stull, 1988). Turbulent mixing in the ML induced by rising thermals leads to nearly height-constant profiles of conserved quantities, such as potential temperature and specific humidity up to the EL (Schmidli, 2013; Wagner et al., 2014a). Inside the EL, overshooting thermals cause mixing of potentially cooler air from the ML with air from the stably stratified free atmosphere aloft. This relatively weak exchange with the free atmosphere limits the vertical dispersion of pollutants mostly to the ML. Over complex terrain, interactions between the terrain and the overlying atmosphere lead to a horizontally inhomogeneous CBL structure (Zardi and Whiteman, 2013). Additionally, thermally driven flows increase the vertical transport of pollutants, moisture, and other components. Often this transport goes beyond the CBL top into the free atmosphere (e.g., Gohm et al., 2009; Rotach et al., 2014; Wagner et al., 2014b; Weigel et al., 2007).

Thermally driven winds develop due to differential heating of adjacent air masses and are characterized by a reversal of wind direction twice per day (Zardi and Whiteman, 2013). Generally, thermally driven winds can be divided into three different types within respective boundary sub-layers, such
as slope winds within the slope layer, valley winds within the valley atmosphere, and plain-to-mountain winds within the mountain atmosphere (Ekhart, 1948; Whiteman, 2000). Under weak synoptic forcing, the interaction of these three wind systems dominates the flow pattern over complex terrain (Zardi and Whiteman, 2013).

Observational and modeling studies have shown that thermally driven winds and especially upslope winds can enhance the daytime vertical moisture and mass exchange between the CBL and the free atmosphere over a valley by a factor of 3 to 4 compared to pure turbulent exchange processes over a plain (Henne et al., 2004; Weigel et al., 2007). By means of idealized simulations, Wagner et al. (2014b) show that this increase in vertical transport to the free atmosphere can even be up to 8 times larger depending on the CBL height definition used as the reference surface for the vertical transport. In addition to slope and valley winds, vertical transport can be further enhanced by plain-to-mountain winds, which have been explored in the Vertical Transport and Orography (VERTIKATOR) campaign (Weissmann et al., 2005) and in several modeling studies (e.g., De Wekker et al., 1998). Plain-to-mountain winds develop due to a horizontal temperature gradient between the mountain ridge and the adjacent plain. This mesoscale flow transports low-level air from the foreland to the mountain ridge. The slope winds superposed by the plain-to-mountain winds transport the air further upslope and form vertical updrafts above the mountain peaks. Under ideal conditions an upper-branch return flow closes the circulation by blowing air from regions above the peaks backwards in the direction of the foreland (De Wekker et al., 1998). This transport process is referred to as mountain venting and can be an important additional exchange mechanism between the CBL and the free atmosphere over complex topography (Henne et al., 2004). In more detail, Kossmann et al. (1999) differentiate between mountain venting and advective venting. Both are mesoscale flows exporting CBL air to the free atmosphere, where mountain venting is characterized by a vertical transport and advective venting by a horizontal transport through the CBL top. Advecive venting usually occurs if an inclined CBL height exists and the mean wind direction is not parallel to the CBL top (Kossmann et al., 1999).

Thermally driven flows not only provide a vertical transport mechanism; they also impact the temperature and humidity distribution via horizontal and vertical advection and hence the CBL height over complex terrain. When determining the CBL height based on temperature profiles it is assumed that the temperature structure is dominated by vertical mixing. This may often not be the case over complex terrain. Several studies reported shallow (e.g., Adler and Kalthoff, 2014; Rampanelli et al., 2004) or non-existent (e.g., Khodayar et al., 2008) mixed layers in valleys, although convection was present. Thus, the definition of the CBL height over complex terrain may be often problematic (e.g., Catalano and Moeng, 2010; Weigel and Rotach, 2004), and many conventional concepts for the determination of the CBL height might not hold for complex topography. Accordingly, the observational and modeling study of De Wekker et al. (2004) shows that during the day, aerosol layer (AL) heights detected with an airborne lidar differ from CBL heights determined by temperature-based methods over complex terrain, whereas this is not the case over homogeneous, flat terrain. Temperature-based CBL heights mostly show a more terrain-following behavior and are lower than AL heights (De Wekker et al., 2004).

As about 50 % of the earth’s land surface consists of mountainous terrain (Rotach et al., 2014), differences in transport and mixing processes over complex terrain and the flat plain are of great importance for regional weather and climate studies. Today’s operational global numerical weather prediction and climate models have horizontal grid resolutions larger than 10 km, which is too coarse to properly resolve topographically induced transport processes. Present-day boundary layer parameterization schemes are not capable of accounting for these missing subgrid-scale effects (Rotach et al., 2014). It is therefore necessary to quantify these effects, e.g., with high-resolution numerical simulations and, based on these results, develop new boundary layer schemes for complex terrain. The need for such a development has already been stressed by Noppel and Fiedler (2002).

This paper relates to recent idealized studies (Wagner et al., 2014b, 2015), which investigate the impact of different valley topographies on the CBL structure, and the vertical exchange between the CBL and the free atmosphere under idealized daytime conditions with a constant surface sensible heat flux. The present work aims at investigating interactions between plain-to-mountain and slope wind systems, and their influence on daytime pollution transport and distribution over complex terrain. This is achieved by tracer analyses over a quasi-two-dimensional mountain range with embedded valleys and a flat foreland on each side of the mountain in cross-mountain direction. The embedded valleys used in the present simulations are bordered by two mountain ridges of different crest heights. This is in line with a case study of transport processes in a valley with similar asymmetric crest heights (Adler and Kalthoff, 2014) and extends recent idealized simulations of Wagner et al. (2014a, b, 2015) to account for a typical geometric feature of real terrain. Simulations for valleys with different depths are performed and compared to a single-ridge topography to quantify the impact of varying valley floor heights on different transport processes of pollutants over complex terrain, e.g., mountain venting and return flows in the free atmosphere.

The paper is organized as follows. In Sect. 2 the numerical model and the experimental setup are described. Section 3 explains the procedures of flow decomposition and averaging, and Sect. 4 summarizes the different CBL height definitions used in this study. The simulation results are presented in Sect. 5, and a conclusion is given in Sect. 6.
2 Model and setup

In this study, idealized large-eddy simulations (LES) of daytime thermally driven flows are performed with the Advanced Research version of the Weather Research and Forecasting model (WRF-ARW), version 3.4. The WRF model is a fully compressible, non-hydrostatic, terrain-following numerical modeling system, which can be run in LES mode (Skamarock et al., 2008).

A third-order Runge–Kutta (RK3) time integration scheme, a fifth-order horizontal and a third-order vertical advection scheme are applied in the numerical simulations (Skamarock et al., 2008). Subgrid-scale turbulence is parameterized by a three-dimensional, 1.5-order turbulent kinetic energy (TKE) closure (Deardorff, 1980). The fully turbulent flow is decomposed into its resolved turbulent and mean advective parts according to the method of Wagner et al. (2014a), which is described in Sect. 3. A statistics module for online averaging and flux computation has been implemented in the WRF model which reduces the demand for data storage.

At the surface a Monin–Obukhov similarity scheme (Monin and Obukhov, 1954) is used to compute turbulent momentum fluxes. This scheme couples the surface and the first model level using the four stability regimes of Zhang and Anthes (1982). The surface roughness length is set to 0.16 m. Following the approach of Wagner et al. (2014a), surface moisture fluxes are disabled, and a constant sensible heat flux of 150 W m\(^{-2}\) is prescribed at the surface. These quite substantial simplifications are supported by sensitivity tests performed by Schmidli (2013), which reveal similar flow and CBL developments over an idealized valley when prescribing either a constant or a time-dependent surface sensible heat flux. Further, the recent study of Leukauf et al. (2015) shows an approximately linear relation between the amplitude of the sensible heat flux and the amplitude of the net shortwave radiation. Hence, prescribing the heat flux instead of the radiative forcing will not fundamentally change the results. The simulations are run for 6 h. The resulting integrated heat input would be the same as prescribing a more realistic sinusoidal heating with an amplitude of about 235 W m\(^{-2}\) that is reached after 6 h, i.e., at noon. Such heating conditions are typical for non-arid mid-latitude valleys (Bonan, 2008; Rotach et al., 2008; Schmidli, 2013). The simulations are initialized with an atmosphere at rest, with a potential temperature of 280 K at sea level height, and a constant vertical temperature gradient of 3 K km\(^{-1}\). To avoid moist processes, the relative humidity is set to a constant value of 40% at the beginning. To trigger convection, randomly distributed temperature perturbations with amplitudes \(\leq 0.5\) K are added to the lowermost five model levels, The Rossby number for our problem is about one or larger\(^1\) suggesting that Coriolis force might play some minor role. Nevertheless, for the sake of simplicity we neglect Coriolis effects.

All simulations are performed with a horizontal mesh size of 100 m and 74 vertically stretched levels with a vertical grid spacing increasing from 10 m at the lowest level to 100 m higher aloft. The model top is defined at 6.2 km with a Rayleigh damping layer covering the uppermost 2 km. Periodic lateral boundary conditions are applied in both horizontal directions. The integrating time step is set to 0.5 s.

The analytical expression for the quasi-two-dimensional model terrain \(h(x)\) is defined as the product of a large-scale mountain \(h^s(x)\) with a half width \(L_x/2\) and a small-scale cosine-squared perturbation with \(n\) number of wave cycles per length scale \(L_x:\)

\[
h(x) = h_{\text{max}} \cos^2 \left( \frac{x}{L_x} \right) h^s(x), \quad (1a)
\]

where

\[
h^s(x) = \begin{cases} 
\cos^2 \left( \frac{x}{L_x} \frac{\pi}{n} \right) & |x| \leq X_0 \\
0 & |x| > X_0 
\end{cases}, \quad (1b)
\]

and where \(h_{\text{max}}\) specifies the maximum height of the mountain range. This setup is similar to mountain configurations with several ridges used in previous studies (Klemp et al., 2003; Schär et al., 2002). In this study, the parameters are set to \(L_x = 60\) km, \(X_0 = 30\) km, and \(n = 0\) or 4. This generates a symmetric, 60 km broad mountain range consisting of a single ridge for \(n = 0\), or three ridges with two embedded valleys for \(n = 4\) (Fig. 1a). In the simulations with three ridges, the ridge at \(x = -13.9\) km and the ridge at \(x = 0\) km are hereafter referred to as the first and the main ridge, respectively. The slopes are correspondingly counted from left to right: slope 1 \((-22.5\) km \(\leq x \leq -13.9\) km), slope 2 \((-13.9\) km \(\leq x \leq -7.5\) km), and slope 3 \((-7.5\) km \(\leq x \leq 0\) km). A flat foreland extends over 30 km on each side of the mountain in cross-mountain direction (see Fig. 1b). The scale of the embedded valleys is comparable to real valleys such as the Inn Valley in the European Alps. For sensitivity runs, mountain shapes with elevated valley floors are used, where the topography is an extension of Eq. (2) and is specified by a linear combination of an upper and lower envelope:

\[
h(x) = (h_{\text{max}} - h_{\text{min}}) \cos^2 \left( \frac{x}{L_x} \frac{n \pi}{2} \right) h^s(x) + h_{\text{min}} \quad h^s(x), \quad (2)
\]

where \(h^s(x)\) is the large-scale mountain of Eq. (2), and where \(h_{\text{max}}\) and \(h_{\text{min}}\) are the maximum heights of the upper and lower envelope, respectively. When \(h_{\text{min}}\) becomes zero, Eq. (2) is identical to Eq. (2). In addition to these mountain shapes, a simulation over a flat plain is performed. An overview of the different model topographies with their maximum slope inclinations is given in Table 1.

Due to the flat foreland on each side of the mountain range, a plain-to-mountain wind system develops during the simulation. The model topography consists of infinitely long ridges

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\(^1\) \(Ro = U/(Lf) \sim 1\), with typical values of \(U = 3\) m s\(^{-1}\), \(L = 30\) km, and \(f = 10^{-4}\) s\(^{-1}\).
Tracer analyses are performed to quantify the impact of different terrain geometries on daytime pollution transport and distribution over a mountain range compared to flat terrain. In all simulations, a passive tracer is constantly emitted over the whole y direction within different cross-mountain subdomains, depending on the focus of the analysis. In the vertical, the tracer source covers the lowermost eight model levels (up to an altitude of approximately 110 m), which is comparable to pollution layer depths typically observed in the morning in the Inn Valley (e.g., Gohm et al., 2009). The emission has an arbitrary magnitude. The tracer particles are transported by three-dimensional winds and dispersed by atmospheric turbulence and diffusion.

3 LES averaging method

In order to distinguish between different heating processes, the flow is decomposed into its mean advective, resolved turbulent, and subgrid-scale parts following the approach of Schmidli (2013) and Wagner et al. (2014a). The fully turbulent variable $\bar{\psi}(x,t)$ is divided into a model grid-box average $\bar{\psi}(x,t)$ and a subgrid-scale part $\psi'(x,t)$:

$$\psi(x,t) = \bar{\psi}(x,t) + \psi'(x,t).$$

By means of Reynolds averaging, the model output $\bar{\psi}(x,t)$ can be formally separated into a mean and a fluctuating part. Therefore, the resolved turbulent part $\psi''(x,t)$ can be computed from the grid-box average by

$$\psi''(x,t) = \bar{\psi}(x,t) - \langle \bar{\psi}(x,t) \rangle,$$

where the time and along-mountain averaging operator $\langle \rangle$ is defined as

$$\langle \rangle = \frac{1}{T L_y} \int_{t-T/2}^{t+T/2} \int_0^L \bar{\psi}(x,t) \, dy \, dx,$$

with an averaging interval in time of $T = 40$ min and in space parallel to mountain range of $L_y = 10$ km. Time averaging is based on a sample interval of 1 min. In order to better compare the mean cross-mountain structure of the different sensitivity runs, all variables shown in this study are averaged in time and space (along y direction) according to Eq. (5).

The decomposed vertical fluxes are computed according to the method described in Wagner et al. (2014a). The computation of mean vertical profiles over the valley requires an interpolation from model levels to Cartesian coordinates along constant height levels which have a vertical grid spacing of 20 m.
4 CBL height detection

In this study, we distinguish between AL and CBL heights, marking the top of the tracer distribution and the top of the nearly height-constant potential temperature profile, respectively. Conventionally, both definitions are synonymously used for the CBL height detection over homogenous and flat terrain. Observational and numerical studies indicate, however, that the heights of the AL and CBL are different over mountainous terrain (De Wekker et al., 2004).

In the present work, the AL height is determined by a gradient method computing the vertical gradient extremum of aerosol concentration moving upwards from the surface (Emeis et al., 2007). We use three different methods to compute the CBL height. The first one (CBL1) is determined as the height at which the potential temperature gradient exceeds a threshold of 0.001 K m⁻¹. This gradient method is also used by Schmidli (2013) and Wagner et al. (2014b, 2015), whereby the threshold value is chosen following Catalano and Moeng (2010). To compare our results with De Wekker et al. (2004), we compute a second CBL height (CBL2) by using the same Richardson-number-based method following Vogelezang and Holtslag (1996). For this purpose, a modified bulk Richardson number is calculated on every vertical model level starting from the surface. The CBL2 height is then derived as the height where the Richardson number reaches a critical value of 0.25 (Seibert et al., 2000; Vogelezang and Holtslag, 1996). A more detailed description is given in De Wekker (2002). Seibert et al. (2000) criticize that the Richardson-method of Vogelezang and Holtslag (1996) adds a surface excess temperature to an already existing superadiabatic layer above the ground; therefore, they conclude that the calculated CBL2 height might be slightly overestimated. For comparison, an additional CBL height (CBL3) is calculated based on a Richardson number method without an additional excess temperature (Seibert et al., 2000). The temporal evolution of horizontally averaged AL and CBL heights, vertical sensible heat flux profiles, and normalized tracer mixing ratios over the PLAIN are shown in Fig. 2. Due to the definition of the CBL1 height, it marks the top of the ML and is located slightly below the altitude of the vertical heat flux minimum. This is also in line with CBL heights obtained by Schmidli (2013) and Wagner et al. (2014b, 2015). The CBL2 height follows the top of the EL and therefore lies above the CBL1 height (see Fig. 2). During the whole simulation, the vertical position of the CBL3 is situated in the middle of the EL and is about the same as the AL height in the PLAIN simulation with a homogeneous tracer source near the surface between −30 km ≤ x ≤ 0 km (see Sect. 2).

For quantifying the vertical transport from the CBL to the free atmosphere, the time dependent CBL1 height is used as reference height. Vertical transport of CBL air beyond this reference height can occur either by turbulent exchange in the EL or by thermally induced circulations.

5 Simulation results

5.1 Flow structure

In this section, the sensitivity of the flow structure on the terrain geometry is assessed. In all simulations the instantaneous flow is fully turbulent after 2 h of simulation (not shown), and the flow pattern shows similar characteristics to the results in Wagner et al. (2014a). Over the flat foreland a CBL layer and a plain-to-mountain wind is established. Inside the valleys, thermally driven upslope winds develop at the beginning of the simulations.

In order to better compare the mean flow structure of the different sensitivity runs, the flow fields are temporally and spatially averaged, and shown as cross sections after 6 h of simulation in Fig. 3. In all simulations, a CBL develops over the foreland up to 1.5 km. Despite the different valley depths, all simulations with valleys (Fig. 3a–c) have similar CBL1 heights of 1.5 to 1.7 km over the crest of the first ridge and approximately 2.5 km over the crest of the main ridge. How-

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This text is taken from a scientific paper discussing the detection of CBL heights in a mountainous terrain context.
Figure 3. Cross sections of averaged (a–d) cross-mountain wind speed and (e–h) vertical wind speed as color contours after 6 h of simulation for four different mountain shapes: (from top to bottom) HMIN0, HMIN0.5, HMIN1, and S-RIDGE (cf. Table 1). Potential temperature as black contour lines (0.25 K increment) and wind vectors for components parallel to the cross section. Variables are averaged in time and space (along y direction). The black solid line shows the reference CBL height (CBL1).
ever, in the reference run (HMIN0, Fig. 3a), due to updrafts in the upper part of slope 2 (cf. naming convention in Sect. 2), the CBL1 height is up to 600 m higher over slope 2 and nearly horizontal over the valley region. In the single-ridge simulation (S-RIDGE, Fig. 3d), the CBL1 height is comparable to the one in the simulations with elevated valleys, but the depth\(^3\) of the CBL is considerably smaller.

Depending on the valley floor height, two different flow regimes develop in the simulations with embedded valleys. The first one occurs in the reference run with the deepest valley and the second one in the two simulations with elevated valley floors. In the reference run (HMIN0, Fig. 3a), upslope winds develop over all mountain slopes with cross-mountain wind speeds of up to 2.1 m s\(^{-1}\) after 6 h of simulation. In the upper part of slope 2 and above the main ridge updrafts form due to converging upslope winds blowing from both sides of the mountain (Fig. 3e). The convergence zones lead to mean vertical wind speeds of up to 1.3 m s\(^{-1}\) and horizontal return flows towards the foreland above the CBL1 height. Above the valley region, subsidence exists with vertical wind speeds of approximately \(-0.3\) m s\(^{-1}\). Over the foreland of the reference run, a plain-to-mountain circulation develops, which surmounts the first ridge and converges over slope 2 with the upslope winds.

In the second flow regime (HMIN0.5, HMIN1 Fig. 3b, c), the plain-to-mountain wind penetrates down to the valley floor. Hence, it replaces the upslope flow over slope 2 and intensifies the upslope wind over the main ridge. The superimposed plain-to-mountain flow leads to slightly higher wind speeds and a significantly deeper slope wind layer of up to

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\(^3\)The CBL depth is defined as the CBL height minus the terrain height.

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Figure 4. Vertical profiles of temporally and spatially averaged cross-mountain wind speed at (a) the middle of slope 1 \((x = -18.2\) km\), (b) the middle of slope 2 \((x = -10.7\) km\), and the middle of slope 3 \((x = -3.7\) km\) for the mountain shapes HMIN0 (solid lines) and HMIN0.5 (dashed lines). Black and blue lines are valid for 2 and 4 h of simulation, respectively. Red lines in the inset show the location of the profiles. The averaging in time and space is done according to Eq. (5).

Figure 5. Cross sections of averaged potential temperature as contour lines (increments of 0.25 K) after (a) 2 h and (b) 4 h of simulation for the HMIN0.5 mountain shape and (c) after 4 h for the reference run (HMIN0). Wind vectors for components parallel to the cross section. Variables are averaged in time and space (along \(y\) direction).
0.5 km compared to the HMIN0 run. Furthermore, the deeper slope wind layer prevents subsidence in the center of the valley. Due to the absence of a convergence zone above the first ridge in the HMIN0.5 and HMIN1 simulation, updrafts and return flows only develop over the main ridge. This leads to a single return flow above the CBL1 height towards the foreland with wind speeds up to 2.2 m s$^{-1}$ (between 1.4 and 2.6 km), whereas in the reference run (HMIN0), two nearly separated return flows develop over the foreland with wind speeds less than 1.9 m s$^{-1}$ (between 1.4 and 1.8 km, and between 2.1 and 2.5 km).

In the S-RIDGE simulation, an upslope wind layer superposed by the plain-to-mountain wind develops with wind speeds up to 2.4 m s$^{-1}$ and a layer depth of approximately 400 m. The return flow towards the foreland is divided into two clearly separated wind layers: an upper one above crest height (between 2.2 and 2.9 km), which is deeper and has stronger winds (up to 1.4 m s$^{-1}$), and a lower one, which is located slightly above the CBL1 height with wind speeds below 0.6 m s$^{-1}$.

The two different flow regimes are also visible in vertical profiles of mean cross-mountain winds at the middle of the slopes (Fig. 4). Shown are profiles for the reference run (HMIN0) and for HMIN0.5 as a representative for the simulations with elevated valleys. After 2 h of simulation, upslope winds of up to 1.7 m s$^{-1}$ have established in both simulations.
Figure 8. Cross sections of tracer concentrations (color contours) after 6 h of simulation for all simulations: (a) PLAIN, (b) HMIN0, (c) HMIN0.5, (d) HMIN1, and (e) S-RIDGE. A passive tracer has been constantly emitted over the whole along-mountain domain within the region of \(-30 \text{ km} \leq x \leq 0 \text{ km}\) on the lowermost eight model levels (up to an altitude of approximately 110 m). Mixing ratios are averaged in time and space (along \(y\) direction), and normalized by their corresponding maximum value. CBL heights CBL1, CBL2, CBL3, and AL are plotted as black solid, dashed, dotted, and green solid lines, respectively (see also the legend shown in Fig. 8e). Potential temperature is shown as black contour lines (0.25 K increment). Additionally, vertically integrated tracer masses are shown for 2, 4, and 6 h of simulation as dotted, dashed, and solid lines in the bottom panels, respectively. These relative mass values are calculated by splitting the \(x\) direction into bins of 1 km and determining the percentage of total amount of tracers within these cross-mountain intervals (\% km\(^{-1}\)).

over all slopes. The depth of the slope wind layer is shallower over slope 3 (Fig. 4c) than over slope 1 and 2 (Fig. 4a, b). Prandtl’s (1944) analytical slope-wind model predicts shallower slope winds for steeper slopes and higher static stability of the background atmosphere. This is in agreement with our simulations in which the background stability and the slope angle are higher over the slope of the main ridge than over the slopes of the first ridge. In HMIN0.5, after 4 h
of simulation, the plain-to-mountain flow overruns the first peak, accelerates over slope 2 and finally reaches the elevated valley floor. The downslope flow has a speed of about 3.8 m s\(^{-1}\) and a depth of approximately 500 m (Fig. 4b). In the reference run, however, the upslope wind regime persists throughout the simulation and hinders the plain-to-mountain wind to penetrate into the valley. The evolution of different flow regimes was mainly caused by different temperature structures. This is discussed in detail in Sect. 5.2.

### 5.2 Temperature structure

In this section, differences in the temperature structure due to varying terrain geometries are described and explained by means of differences in heating rates. To demonstrate the evolution of the downslope wind within the elevated valley, cross sections of potential temperature are displayed for the HMIN0 and HMIN0.5 simulation in Fig. 5. After 2 h in the HMIN0.5 simulation (Fig. 5a), the air over the first ridge, advected by the plain-to-mountain flow from the foreland, is potentially cooler than the valley air and therefore able to descend into the valley. Due to a weakening of the upslope wind over slope 2, the convergence zone is continuously shifted towards the valley floor and the downslope flow eventually replaces the local slope wind circulation after 4 h of simulation (Fig. 5b). In the reference run after 4 h of simulation (Fig. 5c), the advected air at crest height over the first ridge has about the same potential temperature than the air in the upslope flow advected from the valley. Due to the deeper valley in HMIN0 compared to the elevated valleys in HMIN0.5 and HMIN1, a more distinctive upslope circulation establishes over slope 2. Both facts prevent the plain-to-mountain wind to descend to the valley floor during the entire simulation.

The convergence zone is characterized by two thermally driven opposing flows that separate from the surface. Flow separation may also occur over steep slopes for dynamical reasons without the need of a strong counter current in the valley. This has been shown in several studies of stably stratified flows past a valley based on idealized simulations (e.g., Vosper and Brown, 2008) and laboratory experiments (e.g., Lee et al., 1987; Tampieri and Hunt, 1985). For example, a critical valley depth may exist beyond which the valley atmosphere becomes decoupled from the imposed background flow aloft (e.g., Vosper and Brown, 2008). However, a more detailed study to clarify the dependence of the depth of flow penetration into the valley as a function of the valley depth would go beyond the scope of this paper.

Mean vertical profiles of potential temperature over the valley region are shown for all simulations with valleys in Fig. 6. After 2 h of simulation (Fig. 6a), potential temperatures near the valley floor are approximately 1 to 2 K colder in the reference run (HMIN0) compared to the simulations with elevated valleys (HMIN0.5, HMIN1). The mean potential temperature profile of the reference run shows a three-layer thermal structure over the valley region with a well-mixed layer (CBL1), a valley inversion layer and an upper weakly stable layer (Vergeiner and Dreiseitl, 1987; Schmidli, 2013). After 6 h of simulation (Fig. 6b), all profiles show nearly identical mean potential temperatures with a well-mixed CBL1 up to approximately 1.8 km.

To investigate the reason for these different potential temperature profiles, density-weighted and volume-averaged heating rates are computed for the largest (HMIN0) and the smallest valley volume (HMIN1) according to the method of Schmidli (2013). Both control volumes extend from the first to the main ridge and from the surface to an altitude of 2.1 km. In Fig. 7, the evolution of all heat budget components is shown, where the total tendency (TOT) is equal to the sum of the contributions due to the surface sensible heat flux (SHF), the mean flow advection (ADV), and the turbulent heat exchange between the valley volume and the free atmosphere (TRB). Due to the flux computation method used in this study, which involves averaging in time, no heating rates could be calculated before 1.5 h of simulation. Nevertheless, potential temperature profiles indicate that in the early phase (before 2 h) the heating is stronger for smaller valley volumes than for larger ones (cf. HMIN1 and HMIN0 in Fig. 6a). The result is in agreement with the concept of the valley-volume effect which states that for a given amount of energy input, the heating rate is stronger the smaller the volume (e.g., Wagner, 1932). This explains why the heating rate contribution from the surface sensible heat flux (SHF) is permanently higher in the simulation with smaller valley volume (HMIN1) compared to the reference run with larger valley volume (HMIN0, cf. Fig. 7), although the surface sensible heat flux itself is the same in both simulations. Figure 7 shows that the surface sensible heat flux is the main heating source of the valley atmosphere in both simulations, whereas mean-flow advection (ADV) cools the valley volume, and the turbulent contributions (TRB) are negligible. In contrast to the early phase, the total heating rate (TOT) of the HMIN1 simulation is smaller than of the HMIN0 run after about 1.5 h (Fig. 7). The reason is that the plain-to-mountain flow enters the control volume of the HMIN1 run and leads to a much stronger cold-air advection (ADV) than in HMIN0. Consequently, advection overcompensates the volume effect. This striking heating pattern leads to the almost same potential temperatures in the CBL until the end of all simulations (see Fig. 6b), despite the different valley volumes.

### 5.3 Pollution distribution

By means of tracer analyses, the impact of varying terrain geometries on daytime pollution distribution over a mountain range compared to the one over a flat plain is described in this section. Here, we focus on the interaction between the plain-to-mountain flow and the slope wind system which affects the vertical distribution of pollutants. The focus of the next
Figure 9. Relative tracer mass located above (dark gray) and below (light gray) the reference CBL height (CBL1) as a function of time. A tracer has been constantly emitted near the surface over the half space of the mountain range within the region of $-30 \ km \leq x \leq 0 \ km$ (see Fig. 8). Shown are all simulations (from left to right) between 2 and 6 h: PLAIN, HMIN0, HMIN0.5, HMIN1, and S-RIDGE.

Figure 10. As in Fig. 8 for the (a) HMIN0, (b) HMIN0.5, and (c) S-RIDGE simulation, but a tracer has been constantly emitted within the region between $-4 \ km \leq x \leq -3 \ km$. 
section, Sect. 5.4, is on the impact of the valley floor height on processes of pollution transport over complex terrain.

In the first step, a passive tracer is constantly emitted at the surface over the half space of the mountain range within the region of $-30 \, \text{km} \leq x \leq 0 \, \text{km}$ (see Sect. 2). Figure 8 shows cross sections of normalized tracer mixing ratios, and the AL and CBL heights for all simulations after 6 h of integration. The mixing ratio has been normalized by its maximum value occurring in the shown domain at the given time. Additionally, vertically integrated tracer masses are shown for 2, 4, and 6 h of simulation. In the PLAIN simulation (Fig. 8a), the turbulent transport results in a nearly homogeneous distribution of tracer particles inside the CBL up the EL. The CBL1 height marks the top of the nearly height-constant potential temperatures at 1.7 km. The altitude of the AL height is located at approximately 1.9 km and lies between the heights of the CBL2 and CBL3. The almost identical CBL and AL heights over the plain qualitatively confirm results of De Wekker et al. (2004). The vertically integrated tracer mass is homogeneously distributed with approximately 3.3 % km$^{-1}$. This results in slightly less than 100 % tracer mass when integrating between $-30 \, \text{km} \leq x \leq 0 \, \text{km}$, as a small part of tracer mass is horizontally transported out of this subdomain due to turbulent diffusion. In the reference run (Fig. 8b), tracer particles are advected towards both ridges by upslope winds. After 6 h of simulation, concentration maxima exist in regions of updrafts over slope 2 ($-13 \, \text{km} \leq x \leq -11 \, \text{km}$) and in the upper part of slope 3 ($-1 \, \text{km} \leq x \leq -0 \, \text{km}$). Therefore, the largest tracer masses are found with up to 5.9 % km$^{-1}$ over the valley region after 6 h of simulation. The AL and CBL heights over the foreland are in all simulations similar to the ones in the plain simulation. Over the valley region of the reference run ($-9 \, \text{km} \leq x \leq -3 \, \text{km}$), the AL height is considerably higher (up to 0.8 km for CBL1) than the CBL heights. In the HMIN0.5 (Fig. 8c) and HMIN1 (Fig. 8d) run, the superimposed plain-to-mountain flow leads to a less complex tracer distribution than in the HMIN0 case with a rather continuous horizontal increase in tracer mass towards the main ridge. In the region $x < -8 \, \text{km}$, the AL heights are considerably higher (up to 0.9 km for CBL1) than the CBL heights. As in the reference run, this implies a tracer transport towards higher altitudes than the temperature-based CBL heights. In the S-RIDGE simulation a second tracer maximum above crest height exists at approximately 2.5 km. The total horizontal mass flux of tracer particles in the return flow above the CBL is only slightly higher in the S-RIDGE run than in the other simulations (not shown) and, hence, cannot explain the formation of the elevated layer of tracers in S-RIDGE. However, the center of the return flow is located about 500 m higher in S-RIDGE which favors the formation of a pollution layer at this height compared to the other runs (cf. Figs. 3 and 8). Generally, similarly elevated pollution maxima were modeled by Fiedler et al. (2002) and elevated moist layers downstream of mountain ridges related to advective venting were observed by Adler et al. (2015).

These results corroborate the concept of an additional transport between the CBL and the free atmosphere over complex terrain in comparison to a pure convective exchange process (De Wekker et al., 2004). The CBL heights show a more terrain-following behavior than the AL height for all simulations except for the HMIN0 run. In that simulation, the different CBL heights are nearly horizontal over the valley region as a result of a strong updraft over slope 2 (cf. Sect. 5.1). Nevertheless, the CBL heights are still lower than the AL height. The comparison of the present results with those of De Wekker et al. (2004), who used the same CBL height definition as our CBL2, shows similar differences between the AL and CBL2 heights (up to 0.4 km) for various terrain geometries.

The topographically induced tracer transport in relation to the PLAIN simulation is quantified in Fig. 9. In the CBL over
a flat plain, the only process to transport pollutants into the free atmosphere is turbulent mixing in the EL. Therefore, in the PLAIN simulation nearly all of the tracer particles (up to 85 %) stay below the CBL1 height throughout the entire simulation. In contrast to the PLAIN run, approximately 40 % of tracer mass is located above the CBL1 height after 2 h in the simulations with mountains. Until the end of the simulation, the vertical transport beyond the CBL1 height increases up to 50 % for the HMIN1 case and up to 55 % for the S-RIDGE simulation. In the reference run, the relative tracer mass above the CBL1 height compared to the relative tracer mass within the CBL slightly decreases to 35 % until the simulation end. This decrease in relative tracer mass above the CBL1 height is due to the fact that the constant tracer source at the surface is stronger than the vertical tracer transport through the CBL top. In summary, topographically induced vertical tracer transport from the surface to the free atmosphere can be up to 2.5 to 3.7 times larger than pure turbulent exchange over a flat plain. Similar results were found for the vertical transport out of a valley in the real-case study of Weigel et al. (2007) and in the idealized modeling study of Wagner et al. (2014b). Repeating the same analysis of tracer exchange for the CBL3 as a reference height instead of CBL1 leads to the same qualitative results. However, in terms of quantitative exchange, the vertical transport is three times (5.5 to 10.3) higher for CBL3 than for CBL1. This result demonstrates the strong sensitivity of the magnitude of the vertical exchange on the definition of the CBL height.

5.4 Pollution transport processes

This section focuses on the impact of embedded valleys and varying valley floor heights on different transport mechanisms, such as mountain venting in updrafts and advective venting by horizontal return flows. To isolate individual horizontal and vertical transport processes, a passive tracer is constantly emitted within three different subdomains: over the slope within the mountain range, at the foot of the mountain range, and over the valley floor, respectively.

To study the pollution transport over a slope within the mountain range, a passive tracer is emitted near the surface between \(-4 \text{ km} \leq x \leq -3 \text{ km}\) which corresponds to the center of the slope 3 in the simulations with valleys. Figure 10 shows the vertical transport between the CBL and the free atmosphere over the main ridge for the reference run (HMIN0) and for HMIN0.5, and compares it to the vertical transport over the upper part of the single ridge (S-RIDGE). In all three simulations, tracers are transported within the slope wind layer towards the mountain peak and within the updrafts to the free troposphere. From there, they are captured by the horizontal return flow and are transported towards the foreland. In the simulations with valleys, the rather strong vertical updrafts transport most of the tracers vertically through the CBL top (Fig. 10a, b). Therefore, according to the def-
As previously noticed, difference in the return flow structure (cf. Fig. 3) cause different patterns of horizontal tracer transport from the main ridge towards the foreland (Fig. 10). In the HMIN0 simulation (Fig. 10a), the additional venting process over slope 2 prevents a horizontal transport of pollutants from the main ridge towards the foreland beyond the valley region. Due to the absence of updrafts over the smaller ridge in the HMIN0.5 simulation (Fig. 10b), the tracers are transported by the more homogeneous return flow almost twice the horizontal distance towards the foreland compared to the HMIN0 run. In the S-RIDGE simulation (Fig. 10c), a distinct return flow develops, which extends approximately 500 m higher up to about 3 km than in the other simulations. This leads to the previously mentioned elevated tracer layer shown in Fig. 8. These different distribution patterns are also represented in the vertically integrated tracer masses. At the end of the simulation, the integrated tracer mass in the HMIN0.5 and S-RIDGE is more evenly distributed between $-20 \text{ km} \leq x \leq 0 \text{ km}$ and $-30 \text{ km} \leq x \leq 0 \text{ km}$, respectively, whereas in the HMIN0 run a non-uniform tracer distribution remains with a mass maximum over the valley region.

To investigate the pollution transport from the foreland towards the mountain crest, a passive tracer is emitted at the foot of the mountain range between $-23 \text{ km} \leq x \leq -22 \text{ km}$, which is shown for the HMIN0 and HMIN0.5 simulation in Fig. 11. Until the end of the HMIN0 simulation (Fig. 11a), tracer particles are transported horizontally by the plain-to-mountain flow up to the convergence zone in the upper part of slope 2 ($x \simeq -12 \text{ km}$). From there, particles are transported to higher altitudes within the updraft. Apart from this pronounced and stationary updraft, moving thermals distribute the tracers relatively homogeneously in the vertical up to the CBL1 height. In contrast to the reference run, the tracer particles in the HMIN0.5 simulation are transported horizontally up to the main ridge ($x = 0 \text{ km}$) until the end of the simulation (Fig. 11b).

The different transport patterns are quantified in Fig. 12 for all mountain simulations. Shown are the relative tracer masses, which are located on the left- and right-hand side of the first ridge ($x = -13.9 \text{ km}$) as a function of time. For purposes of comparison, the relative mass transport to the left and right of $x = -13.9 \text{ km}$ is also shown for the S-RIDGE simulation. In the reference run, less than 30% of the emitted tracers are transported to the right side of the first ridge until the end of the simulation. In the HMIN0.5 and HMIN1 simulations, approximately 50% of the tracer mass is located right of the first ridge after 6 h. The reason for these different transport patterns is the upslope wind along the second slope ($-13.9 \text{ km} \leq x \leq -7.5 \text{ km}$) in the HMIN0 simulation, which opposes the plain-to-mountain wind and therefore acts as an effective “barrier” between the foreland and the main ridge (cf. Fig. 3). This blocking of the plain-to-mountain flow persists during the entire simulation and allows only little tracer transport towards the main ridge. In the simulations with elevated valleys, the plain-to-mountain flow eliminates the opposing upslope winds and enhances the horizontal tracer transport to the main ridge compared to the reference run. In the HMIN1 simulation the plain-to-mountain flow penetrates towards the valley floor earlier than in the HMIN0.5 run. Therefore, the horizontal transport in the HMIN1 run is significantly faster than in the HMIN0.5 run. In the S-RIDGE simulation, a similar horizontal tracer transport develops as in the HMIN0.5 and HMIN1 runs. However, due to the more homogeneous upslope flow in the S-RIDGE simulation, the tracer transport is less variable and, hence, leads to a rather continuous increase in time in tracer mass towards the main ridge.
To study the pollution transport within a mountain valley, a passive tracer is emitted at the valley floor between $-8 \text{ km} \leq x \leq -7 \text{ km}$, which is shown in Fig. 13 for the HMIN0 and HMIN0.5 simulation. Due to the existence of the typical slope wind system within the valley in the reference run (Fig. 13a), subsidence above the valley center mainly limits the tracer transport to the valley region and most tracer particles remain below the CBL1 height during the whole simulation. In the HMIN0.5 run (Fig. 13b), tracers are transported by the superimposed plain-to-mountain wind towards the main peak and within the updraft to the free troposphere. From there, the tracer is transported by the return flow towards the foreland.

The vertical part of this transport by mountain and advective venting is quantified for all simulations with valleys in Fig. 14. After 2 h, the turbulent transport by convection is the dominant process for the tracer distribution and barely 20 to 25 % of the tracer mass is mixed beyond the CBL1 height. After 3 h in the HMIN1 and 5 h in the HMIN0.5 simulation, the distribution pattern changes due to the additional tracer transport by the plain-to-mountain wind within the valley. Therefore, until the end of the simulations with elevated valleys (HMIN0.5, HMIN1), up to 60 % of the tracer particles are advected beyond the CBL1 height. However, in the reference run only 30 % of the emitted tracer mass is located above the CBL1 height due to subsidence in the valley center and a missing superimposed cross-mountain flow. Comparing tracer emissions within different cross-mountain subdomains (e.g., Figs. 10 and 13), reveals that in all simulations with valleys mountain and advective venting occurs; but whether pollutants emitted at the valley floor are transported out of the valley depends on the interactions between the plain-to-mountain and the slope wind systems.

6 Conclusions

In this study we performed idealized LES with the WRF model to investigate the interaction between plain-to-mountain and slope wind systems, and their influence on daytime pollution distribution over complex terrain. Simulations over a mountain range with embedded valleys bordered by ridges with different crest heights were compared to simulations with a single ridge and a flat plain by means of tracer analyses.

These analyses show differences in thermally driven flows and resultant pollution transport dependent on the valley floor heights. To illustrate the observed two main flow patterns, a conceptual diagram is shown in Fig. 15. In the situation of a deep valley (reference run HMIN0, Fig. 15a), the upslope wind system within the valley opposes the plain-to-mountain wind and therefore acts as an effective “barrier” between the foreland and the main ridge. In the situation of a shallow, elevated valley (Fig. 15b), the plain-to-mountain flow passes the crest of the first (smaller) ridge, descends into the potentially warmer valley, and eventually replaces the opposing upslope wind. These two differing flow structures lead to different transport patterns. In the reference run, less than 30 % of tracer particles emitted over the foreland are advected beyond the first ridge towards the main ridge until the end of the simulation. However, in the simulations with elevated valleys, the relative tracer mass located on the right-hand side of the first ridge is similar to that of a simulation with a single ridge and amounts to approximately 50 %.

The simulation results show that mountain and advective venting are important mechanisms of pollution transport from the surface to the free atmosphere in addition to the
Figure 15. Conceptual diagram of the flow pattern for (a) a deep valley (HMIN0) and (b) an elevated valley (e.g., HMIN0.5) after 6 h of simulation. The black and gray solid lines mark the temperature-based CBL and the AL height, respectively. Thick, solid arrows represent the cross-mountain flow, and thin, solid arrows mark the turbulent exchange in the entrainment layer over the foreland and the valley region. Dashed, double-lined arrows indicate the vertical transport through the CBL top as a result of horizontal flow convergence. V denotes mountain and advective venting and B indicates flow blocking.

The detected AL and CBL heights are in line with the results obtained by De Wekker et al. (2004). Over the flat plain, the spread between the temperature-based CBL heights and the AL height is rather small. However, over complex terrain, the CBL heights are up to 0.9 km lower and rather terrain-following than the AL height. In the present simulations, the mountain induced vertical transport beyond the CBL1 height is up to 3.6 times larger than pure turbulent exchange over a flat plain. Even though the quantification of the vertical exchange strongly depends on the definition of the CBL, the significant transport beyond the CBL1 height in the present simulations demonstrates the need to consider the AL height rather than temperature-based CBL heights as the relevant parameter for air pollution studies over mountainous terrain.

The results of this study extend those of Wagner et al. (2014b, 2015), and confirm that the terrain geometry has a large impact on the flow structure and the resultant transport processes over a mountain range. The change of the flow regime due to minor changes in the topography demonstrates the necessity to account for these topographically induced effects in future boundary layer parameterization schemes. Furthermore, the findings confirm a mountain-induced vertical transport of pollutants beyond the temperature-based CBL height and therefore imply a reconsideration of the conventional CBL height detection methods over mountainous terrain. However, to generalize present findings, further investigations with inhomogeneous land-use properties, time and space dependent surface forcings, and varying atmospheric background conditions will be necessary.

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