Technical Note: Temporal change in averaging kernels as a source of uncertainty in trend estimates of carbon monoxide retrieved from MOPITT

J. Yoon1, A. Pozzer2, D. Y. Chang1, S. Beirle1, T. Wagner1, S. Schloegl2, J. Lelieveld1,3, and H. M. Worden4

1Atmospheric Chemistry Department, Max-Planck Institute of Chemistry, P.O. Box 3060, 55020 Mainz, Germany
2Institute of Atmospheric Physics, Johannes Gutenberg University, 55099 Mainz, Germany
3The Cyprus Institute, Energy, Environment and Water Research Center, P.O. Box 27456, 1645 Nicosia, Cyprus
4National Center for Atmospheric Research (NCAR), Boulder, CO, USA

Correspondence to: J. Yoon (jongmin.yoon@mpic.de)

Received: 18 June 2013 – Published in Atmos. Chem. Phys. Discuss.: 5 August 2013
Revised: 1 October 2013 – Accepted: 18 October 2013 – Published: 21 November 2013

Abstract. It has become possible to retrieve the global, long-term trends of trace gases that are important to atmospheric chemistry, climate, and air quality from satellite data records that span more than a decade. However, many of the satellite remote sensing techniques produce measurements that have variable sensitivity to the vertical profiles of atmospheric gases. In the case of constrained retrievals like optimal estimation, this leads to a varying amount of a priori information in the retrieval and is represented by an averaging kernel (AK). In this study, we investigate to what extent the estimation of trends from retrieved data can be biased by temporal changes of averaging kernels used in the retrieval algorithm. In particular, the surface carbon monoxide data retrieved from the Measurements Of Pollution In The Troposphere (MOPITT) instrument from 2001 to 2010 were analyzed. As a practical example based on the MOPITT data, we show that if the true atmospheric mixing ratio is continuously 50 % higher or lower than the a priori state, the temporal change of the averaging kernel at the surface level gives rise to an artificial trend in retrieved surface carbon monoxide, ranging from −10.71 to +13.21 ppbv yr⁻¹ (−5.68 to +8.84 % yr⁻¹) depending on location. Therefore, in the case of surface (or near-surface level) CO derived from MOPITT, the AKs trends multiplied by the difference between true and a priori states must be quantified in order to estimate trend biases.

1 Introduction

Since the Industrial Revolution human activity has brought about a significant change in atmospheric trace gas concentrations (Hansen et al., 2007), which has important consequences for global air quality and the earth’s atmosphere radiative budget, thus causing climate change (Forster et al., 2007, IPCC AR4). One of the most important trace gases is carbon monoxide (CO). It is produced by the oxidation of methane (CH₄) and non-methane hydrocarbons (NMHC), and directly emitted by biomass burning and combustion of fossil fuels (Wallace and Hobbs, 2006). It acts as a major sink for the tropospheric hydroxyl radical (OH) (Crutzen, 1974). OH, in turn, regulates the lifetimes of various tropospheric trace gases (Khalil and Rasmussen, 1990; Wallace and Hobbs, 2006). The oxidation of CO also leads to the formation of carbon dioxide (CO₂) and tropospheric ozone (O₃) (Crutzen and Gidel, 1983; Fishman and Crutzen, 1978; Burrows et al., 1995). Because of its moderately long lifetime (weeks to months) and inhomogeneous distribution in the troposphere, CO is an ideal tracer for monitoring the air pollution sources and transports (Cicerone, 1988; Logan et al., 1981; Shindell et al., 2006; Lelieveld et al., 2001; Hoor et al., 2005; Edwards et al., 2004, 2006; Pan et al., 1995; Worden et al., 2013a; Liu et al, 2011, 2013).

Remote sensing from satellites provides the unique opportunity to study regional and global changes in atmospheric composition (Burrows et al., 2011). Since its launch on board the EOS-Terra satellite in 1999, MOPITT has provided
global and long-term CO products, which may be used to estimate trends of tropospheric CO and the influence of anthropogenic emissions on atmospheric chemistry (Worden et al., 2013a). To retrieve CO vertical profiles using MOPITT observations, the theory developed by Rodgers (1976, 2000) is employed in the retrieval algorithm (Pan et al., 1998; Deeter et al., 2003). The algorithm is designed to use a priori profiles derived from a climatology based on simulations by the Model for Ozone and Related chemical Tracers-4 (MOZART-4) model (Pan et al., 1998; Deeter et al., 2003; Deeter, 2009; Worden et al., 2013a). The retrieval sensitivity is generally evaluated through averaging kernels (AKs) (Pan et al., 1998; Rodgers, 2000; Deeter et al., 2003; Eskes and Boersma, 2003). The AKs are essential for meaningful comparisons of satellite products against in situ data and model results (Rodgers, 2000; Rodger and Connor, 2003; Eskes and Boersma, 2003). However, we will show that their temporal change can lead to a significant error in the trend estimation of retrieved CO.

The goal of this paper is to investigate the uncertainty caused by temporal AKs change in the trend estimation of retrieved state. It is shown that without adequate knowledge of the differences between the a priori and true profiles of the observed trace gases, AKs uncertainty cannot be eliminated in the trend estimation of retrieved state. Although MOPITT monthly surface CO data were used in this study, we emphasize that the uncertainties in trend estimations apply to any remote sensing observations based on similar AKs concepts.

In Sect. 2, the MOPITT CO data and the standard method used for trend estimation are described. Section 3 presents the analysis of uncertainties and a practical example based on MOPITT CO surface data. Section 4 analyzes possible issues associated with statistically merging Level 3 MOPITT data, and Sect. 5 summarizes this work and presents conclusions.

2 MOPITT surface CO and linear trend model

The MOPITT instrument on the EOS-Terra spacecraft provides tropospheric CO and CH$_4$ distributions on a global scale (Deeter et al., 2003). The temperature constraints of the MOPITT radiometric calibration (University of Toronto and NCAR MOPITT Team, 1996, MOPITT ATBD) are ±0.5 K for the CO profile channels and ±1 K for the CO and CH$_4$ column channels for the expected precisions, being 10% for CO and 1% for CH$_4$ products (Pan et al., 1995, 1998). The global MOPITT retrieved CO data have been used for estimating CO distributions, atmospheric transport, sources, and sinks (e.g., Drori et al., 2012; Fortems-Chiney et al., 2011; Hooghiemstra et al., 2011; Kanakidou et al., 2011; Arellano and Hess, 2006; Choi and Chang, 2010; Stroppiana et al., 2010). Recently the MOPITT Version 5 (V5) Level 3 (L3) thermal infrared (TIR) retrievals (in daytime) lead to an improved sensitivity for the lower tropospheric CO retrieval, a reduced retrieval bias drift associated with long-term instrumental degradation, and a more exact representation of the effects of random errors in the radiances (Clerbaux et al., 2009; Worden et al., 2010, 2013a; Deeter et al., 2007a, 2011, 2012, 2013), and are used in this study. Figure 1 shows the global mean distribution of monthly surface CO products (spatial resolution: 1° × 1°) from 2001 to 2010.

The linear trends (ω) in a unit of ppbv yr$^{-1}$ are estimated using a linear least squares fit based on monthly data as follows:

$$y_t = \omega x_t + \tilde{y}_m + n_t + \mu,$$

where $x_t$, $\mu$, $n_t$, and $\tilde{y}_m$ denote the time index term ($t/12$), the constant term, the monthly noise for the analyzed periods ($t = 1...T$), and the monthly climatology mean of $y_t$ ($m = 1...12$) (i.e., the climatological monthly varying pattern), respectively. This linear trend model is applied to the data time series for each point that represents complete yearly data sets defined as encompassing at least 9 months of data per year. Otherwise, the location is discarded to avoid statistical inconsistencies. In general, the noise term can include random and systematic measurement errors and autocorrelation due to atmospheric variability (Weatherhead et al., 1998, 2002).

Figure 2 presents the linear trends of surface CO from MOPITT V5 TIR L3 products during daytime from 2001 to 2010. Here we have included all the MOPITT V5 data, including scenes that used water vapor climatology when the NCEP (National Centers for Environmental Prediction) Global Data Assimilation System (GDAS) product was not available. The use of water vapor climatology can produce anomalous results in the CO retrievals, as found by the MOPITT team, in particular, off the coast of California. Therefore, we do not have confidence in the higher CO values or trends that can be seen in this region in Figs. 1 and 2.

An overall decrease of the surface CO from biomass burning over South America/Africa (Wallace and Hobbs, 2006; Liu et al., 2011) and fossil-fuel combustion over Eastern USA, Western Europe and Southeast Asia (Wallace and Hobbs, 2006; Liu et al., 2011; Buchwitz et al., 2007) is indicated. This tendency is consistent with the decreasing trends in total CO columns retrieved from MOPITT, the Atmospheric InfraRed Sounder (AIRS), the Tropospheric Emission Spectrometer (TES), and the Infrared Atmospheric Sounding Interferometer (IASI), which are reported in Worden et al. (2013a). However, the trends in Fig. 2 are affected by intrinsic uncertainty due to temporal changes of averaging kernels (AKs).

3 Uncertainty from temporal change of averaging kernels

The V5 MOPITT CO retrieval algorithm is based on the maximum a posteriori (MAP) that is an iterative optimal estimation technique (Pan et al., 1998; Rodgers, 2000; Deeter et al., 2003, 2010). The V5 algorithm employs the log (VMR:...
Fig. 1. Total mean distribution of global surface CO from MOPITT Version 5 TIR Level 3 product, referring to daytime from 2001 to 2010.

Fig. 2. The linear trends of surface CO from MOPITT (Version 5 TIR, Level 3, daytime) from 2001 to 2010. “Not Enough Data” represents the data series discarded to avoid statistical inconsistencies. Complete yearly data sets encompass at least nine months of data over the year.

Volume Mixing Ratio) retrievals (Deeter et al., 2013) that are the basis of this study. A statistical technique to solve the inversion problem is employed to find the optimal CO retrieval using the MOPITT measured radiances, based on a priori defined CO vertical profiles. If the forward model error is neglected, the relation equation between retrieved and true states can be expressed as follows (Rodgers, 1990; Pan et al., 1998; Deeter et al., 2003, 2010):

\[
\hat{x} \cong x_0 + A(x - x_0) = Ax + (I - A)x_0, \tag{2}
\]

where \(\hat{x}\), \(x_0\), and \(x\) represent the retrieved, the a priori, and the true states of the atmosphere, respectively, which are arranged in 10 rows and 1 column for the 10 layers from surface to 100 hPa. \(A\) and \(I\) denote the AKs and identity matrices with 10 rows and 10 columns, respectively. For the surface layer, Eq. (2) is given as follows:

\[
\hat{x}_{\text{surface}} \cong x_{0,\text{surface}} + A_{\text{surface}}(x - x_0) \nonumber \tag{3} = A_{\text{surface}}x + (I_{\text{surface}} - A_{\text{surface}})x_0,
\]

where \(\hat{x}_{\text{surface}}\), \(x_{0,\text{surface}}\), \(I_{\text{surface}}\) and \(A_{\text{surface}}\) represent the retrieved, the a priori surface CO data (arranged in 1 row and 1 column), the surface identity, and the surface AK (arranged in 1 row and 10 columns), respectively.

The AKs matrix \((A)\), which reflects the sensitivity of the retrieved state to the true state, is the most important diagnostics of the retrieval (Pan et al., 1998; Rodgers, 2000; Deeter et al., 2003; Eskes and Boersma, 2003). When the AKs matrix is exactly equal to the identity matrix, the retrieved state is identical to the representation of the true atmospheric state on the altitude grid of the retrieval. However, in practice, the AKs matrix does not match up with \(I\). For example, Fig. 3
shows the mean AK for surface CO ($A_{\text{surface}}$), a priori ($x_0$), and retrieved CO profiles ($\hat{x}$) over the grid cell defined by 30° E, 45° E, 110° N, and 120° N in East China, where large quantities of CO are emitted into the atmosphere from the combustion of fossil fuels (see Fig. 1) (Liu et al., 2011; Buchwitz et al., 2007). The AK theoretically represents how much the true and a priori profiles contribute to the retrieved CO at the surface ($\hat{x}_{\text{surface}}$) as shown in Eq. (3). The surface retrieved CO is therefore the weighted mean contribution of the true (x) and a priori profiles ($x_0$) in multiple layers. However, there is a clear difference between the a priori and retrieved CO profiles as shown in Fig. 3. For example, the retrieved CO at the surface is higher by about 52% compared to the a priori CO.

Most importantly, we are interested in the temporal change of the retrieved state, and its possible connection to the true trend. The retrieved trend can be expressed by the partial differential of Eq. (2) as follows:

$$\frac{\partial \hat{x}}{\partial t} \equiv \frac{\partial x_0}{\partial t} + \frac{\partial A}{\partial t} (x - x_0) + A \frac{\partial x}{\partial t}$$

Equation (4)

In the same manner, the trend of surface retrieved CO is given from Eq. (3) as follows:

$$\frac{\partial \hat{x}_{\text{surface}}}{\partial t} \equiv \frac{\partial x_0}{\partial t} + \frac{\partial A_{\text{surface}}}{\partial t} (x - x_0) + A_{\text{surface}} \frac{\partial x}{\partial t}$$

Equation (5)

Again, if the AKs matrix is the identity matrix (i.e., $A = I$ in Eq. (7) and $A_{\text{surface}} = I_{\text{surface}}$ in Eq. 7), the temporal change of the retrieved state is the same as the change of the true state ($\frac{\partial \hat{x}}{\partial t} = \frac{\partial x}{\partial t}$ and $\frac{\partial \hat{x}_{\text{surface}}}{\partial t} = \frac{\partial x}{\partial t}$). Even if the AKs matrix is not the identity matrix, but the AKs have no temporal change ($A \neq I$, but $\frac{\partial A}{\partial t} = 0$ and $A_{\text{surface}} \neq I_{\text{surface}}$, but $\frac{\partial A_{\text{surface}}}{\partial t} = 0$) then the change of the retrieved state is an averaged contribution of the true changes in multiple layers ($\frac{\partial x}{\partial t} = A \frac{\partial x}{\partial t} + A_{\text{surface}} \frac{\partial x}{\partial t}$). In other words, no temporal change of AKs ($\frac{\partial A}{\partial t} = 0$ and $\frac{\partial A_{\text{surface}}}{\partial t} = 0$) is an ideal condition for the trend estimation. However in fact, the AKs do have a significant variability because they are influenced by all variables as inputs to the forward radiative transfer model (e.g., atmospheric temperature profile, surface pressure, and surface temperature) (Deeter et al., 2003). In addition, the changes in AK values over time are likely due to the changes in CO itself since retrieval sensitivity depends on CO amount as shown in Deeter et al. (2007b) and Worden et al. (2013b). Therefore, the trend of the retrieved state ($\frac{\partial \hat{x}}{\partial t}$ and $\frac{\partial \hat{x}_{\text{surface}}}{\partial t}$) can be biased by the term ($\frac{\partial A}{\partial t} (x - x_0)$ and $\frac{\partial A_{\text{surface}}}{\partial t} (x - x_0)$), whose value (and even sign) is unknown, as the true state (and hence its difference with the a priori state) is unknown.

To estimate the general uncertainties caused by temporal varying AKs, we make the assumption that the true state is 50% more (less) than the a priori state (i.e., $x = x_0 \pm 50\% \times x_0$). This 50% difference could be estimated from the difference between retrieved and a priori states at the surface as

---

*Fig. 3. Mean MOPITT averaging kernel for surface CO, a priori, and retrieved CO profiles over the grid cell defined by 30° E, 45° E, 110° N, and 120° N over East China on October 2002. The relative difference between retrieved CO with a priori profiles is shown to estimate the difference of true with a priori states ($x - x_0$). The retrieved CO at the surface is about 52% higher than the a priori CO mixing ratio.*
shown in Fig. 3. In addition, Fig. 4 shows the global distributions of maximum and minimum differences between them, and demonstrates that the assumption is reasonable globally. Eventually, the AKs uncertainty in the trend analysis of MOPITT CO at the surface is balancing between these extremes.

Following this assumption, the trend of the constructed “true state” is the same as the trend of the a priori state, which theoretically equals to zero (i.e., $\frac{\partial x}{\partial t} = \frac{\partial x_0}{\partial t} = 0$) (Pan et al., 1998; Deeter et al., 2003; Deeter, 2009; Worden et al., 2013a). Nevertheless, some significant trends of the hypothetically retrieved CO (i.e., $\hat{x}_\text{surface} = x_0 \pm 50 \% \times x_0$) at the surface are present, ranging from $-10.71$ to $+13.21$ ppbv yr$^{-1}$ (−5.68 to +8.84 % yr$^{-1}$) in Fig. 5. They are derived by fitting the hypothetically retrieved MOPITT surface CO (i.e., $\hat{x}_\text{surface} = x_0 \pm 50 \% \times x_0$) to Eq. (1). The largest deviation from a null trend is found over China where large surface CO emissions are reported (Liu et al., 2011; Buchwitz et al., 2007). Figure 5a is in contrast with Fig. 5b, as the difference between true and a priori state (i.e., $(x - x_0)$ in Eq. 7) is constant in both figures but with a different sign. In general, the magnitude of the uncertainty depends on the temporal AKs change ($\frac{\partial \Delta x_\text{surface}}{\partial t}$). For instance, in Fig. 5a, b when the difference is $-50 \% \times x_0$ $(+50 \% \times x_0)$, the temporal increase of the AK for surface CO state force an under- (over-) estimation of the trends of retrieved state. Therefore, for both assumed conditions of true state (i.e., $x = x_0 \pm 50 \% \times x_0$), the trend of the retrieved data is determined by the AKs trends multiplied by the difference between true and a priori states ($\frac{\partial \Delta x_\text{surface}}{\partial t} (x - x_0)$).

Since the true state (and hence its difference with the a priori state) is unknown, it is impossible to estimate the actual AKs uncertainty. Furthermore, this issue is relevant for all instrumentation and algorithms that rely on temporally varying AKs. Therefore, future trend studies using similar atmospheric sounding data like MOPITT retrievals, need to first check the temporal changes of AKs. Furthermore, because the difference between true and a priori states could be insignificant at higher level as shown in Fig. 3, the AKs uncertainty could be less than the expectation.

### 4 Temporal variation of Level 3 a priori

In Eqs. (6) and (7), we assumed that no trends are present in the a priori profiles (i.e., $\frac{\partial x_0}{\partial t} = 0$ and $\frac{\partial \Delta x_\text{surface}}{\partial t} = 0$). In fact, the a priori profiles are obtained from the MOZART-4 model, which does not present an interannual variability (Pan et al., 1998; Deeter et al., 2003; Deeter, 2009; Worden et
Fig. 5. The linear trends of retrieved states under the assumption that the true state is (a) $-50\%$ or (b) $+50\%$ higher than the a priori state (i.e., $x = x_0 \pm 50\% \times x_0$). The trends of retrieved states range from $-10.71$ to $+13.21$ ppbv yr$^{-1}$ ($-5.68$ to $+8.84$ $\%$ yr$^{-1}$).

Nevertheless, this is strictly valid only for Level 2 (daily) products, where the model climatology is spatially and temporally interpolated to the exact location and day of the observation for each retrieval (Deeter et al., 2010). In the Level 3 (monthly) data, instead, the surface a priori can have small temporal variation globally (i.e., $\frac{\partial x_{\text{surface}}}{\partial t} \neq 0$), as shown in Fig. 6a, even though it is negligible compared to the trend of retrieved surface CO ($\frac{\partial \hat{x}_{\text{surface}}}{\partial t}$) (see Fig. 2). This small trend can be attributed to the mathematical/statistical aggregation (e.g., cloud filtering-out process) to monthly (Level 3) $1^\circ \times 1^\circ$ data. Figure 6b shows the MOPITT a priori CO at the surface between 2001 and 2010 for the location where the highest trend of the a priori CO is present (i.e., $+4.08$ ppbv yr$^{-1}$ at $89.5^\circ$ E and $43.5^\circ$ N, red star symbol in Fig. 6a). The anomaly of surface a priori CO (i.e., the difference between surface a priori and seasonal mean) includes an interannual variability and a net distinction in 2005.

Hence not only does the temporal variation of Level 3 a priori data make it more difficult to predict the difference between true and a priori states (i.e., $(x - x_0)$), it also creates the additional uncertainty ($\left(I - A\right) \frac{\partial x_0}{\partial t}$ and $\left(I_{\text{surface}} - A_{\text{surface}}\right) \frac{\partial x_{\text{surface}}}{\partial t}$) in the trend estimation as shown in Eqs. (4) and (5).

## 5 Summary and conclusions

Time varying AKs have been shown to be a significant source of uncertainties/errors in the estimation of temporal variation in retrieved data. The uncertainty test applied in this study, based on the MOPITT V5 TIR Level 3 CO products at the surface, demonstrates that the temporal changes of AKs and the differences between true and a priori states can cause significant uncertainties in the trend estimation. Unfortunately, it is not possible to eliminate the AKs uncertainty solely based on satellite observations, as the true state
is unknown. Retrieved total column CO product might also be affected, since it is the vertical integral of the retrieved CO profiles (Worden et al., 2013a). However, the related uncertainties at high altitudes are expected to be smaller than for the near-surface layers because of smaller difference between the true and a priori state. Future studies should investigate this aspect. Furthermore, trend studies based on satellite- and ground-based data products, which have been derived using similar atmospheric sounding methods like the MOPITT retrieval, need to carefully estimate uncertainties and errors that may be caused by time varying AKs.

Acknowledgements. The authors would like to thank the NASA Langley Research Center (Atmospheric Science Data Center, https://eosweb.larc.nasa.gov/project/mopitt/mopitt_table) for providing the MOPITT Version 5 TIR Level 3 products used in the study. The work of Peter Hoor and Sebastian Schlögl was funded by the German French DFG/INSU-CNRS project POMODORO.

The service charges for this open access publication have been covered by the Max Plank Society.

Edited by: T. von Clarmann
References


bon monoxide and ozone, Atmos. Meas. Tech., 6, 1633–1646,