Using boundary layer equilibrium to reduce uncertainties in transport models and CO₂ flux inversions

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Received: 18 February 2011 – Published in Atmos. Chem. Phys. Discuss.: 13 April 2011
Revised: 27 August 2011 – Accepted: 30 August 2011 – Published: 16 September 2011

Abstract. This paper reexamines evidence for systematic errors in atmospheric transport models, in terms of the diagnostics used to infer vertical mixing rates from models and observations. Different diagnostics support different conclusions about transport model errors that could imply either stronger or weaker northern terrestrial carbon sinks. Conventional mixing diagnostics are compared to analyzed vertical mixing rates using data from the US Southern Great Plains Atmospheric Radiation Measurement Climate Research Facility, the CarbonTracker data assimilation system based on Transport Model version 5 (TM5), and atmospheric reanalyses. The results demonstrate that diagnostics based on boundary layer depth and vertical concentration gradients do not always indicate the vertical mixing strength. Vertical mixing rates are anti-correlated with boundary layer depth at some sites, diminishing in summer when the boundary layer is deepest. Boundary layer equilibrium concepts predict an inverse proportionality between CO₂ vertical gradients and vertical mixing strength, such that previously reported discrepancies between observations and models most likely reflect overestimated as opposed to underestimated vertical mixing. However, errors in seasonal concentration gradients can also result from errors in modeled surface fluxes. This study proposes using the timescale for approach to boundary layer equilibrium to diagnose vertical mixing independently of seasonal surface fluxes, with applications to observations and model simulations of CO₂ or other conserved boundary layer tracers with surface sources and sinks. Results indicate that frequently cited discrepancies between observations and inverse estimates do not provide sufficient proof of systematic errors in atmospheric transport models. Some previously hypothesized transport model biases, if found and corrected, could cause inverse estimates to further diverge from carbon inventory estimates of terrestrial sinks.

1 Introduction

Coupled carbon-climate models predict that the fraction of anthropogenic CO₂ emissions absorbed by ecosystems will decline over the 21st century (Friedlingstein et al., 2006; Denman et al., 2007), but how accurately these models represent current ecosystem CO₂ sources and sinks remains unclear. Uncertainties in ecosystem sources and sinks result from errors in atmospheric transport models used to infer ecosystem exchanges from concentration measurements (Denning et al., 1995; Dargaville et al., 2003; Baker et al., 2006). The strongest vertical mixing coincides with ecosystem uptake, in summer, with weaker vertical mixing in winter when ecosystems release CO₂. This covariance between atmospheric dynamics and ecosystem exchanges, known as the seasonal rectifier effect, produces enhanced annual-mean near-surface concentrations in northern latitudes even over annually-balanced ecosystems (Fung et al., 1983; Denning et al., 1995). Inversions of modeled transport having erroneously strong rectification will compensate by overestimating northern and underestimating tropical terrestrial sinks, to balance the global CO₂ budget (Denning et al., 1995; Stephens et al., 2007). Observational constraints could help reconcile atmospheric inversions that infer strong northern terrestrial sinks, with carbon inventories that estimate weaker northern but stronger tropical terrestrial sinks. However, different observations support different conclusions about transport model errors that would imply either stronger or weaker northern
terrestrial sinks. Boundary layer mixing intuitively plays a role in rectification of CO$_2$ vertical gradients, by diluting the effects of summer northern terrestrial uptake through deeper mixing. Atmospheric transport models tend to underestimate summer mixing depths (Denning et al., 1995; Chen et al., 2004; Yi et al., 2004; Denning et al., 2008), but correcting these errors could lead to even larger inferred northern terrestrial sinks in the inversions (e.g. Denning et al., 1995; Yi et al., 2004), increasing the discrepancy with terrestrial carbon inventories. On the other hand, differences between modeled and observed CO$_2$ vertical profiles suggest systematically overestimated summer vertical mixing (Stephens et al., 2007), implying that transport model inversions would support weaker northern and stronger tropical terrestrial sinks if other aspects of the models were improved, such as tropospheric transport and cloud mass fluxes.

Comparisons of transport models and observations have not taken into account the timescale dependence of transport and mixing, which has led to hypotheses of both overestimated and underestimated vertical mixing in transport models, corresponding to both overestimated and underestimated northern terrestrial carbon sinks in the inversions. The dilution by transientboundary layer growth approximately balances surface CO$_2$ fluxes when analyzed during the daytime or over a few days (Raupach, 1991; Raupach et al., 1992; Levy et al., 1999; Lloyd et al., 2001; Styles et al., 2002), and can successfully explain the diurnal rectifier effect (Yi et al., 2004). However over longer periods of time boundary layer depth reflects a statistical equilibrium between surface heat fluxes acting to increase, and radiative cooling acting to decrease boundary layer depth, with clouds coupled through their effect on radiative cooling (Bets, 2004). Radiative cooling in turn balances adiabatic warming in subsiding branches of the circulation, bringing boundary layer trace gas concentrations into a statistically steady state that reflects an approximate equilibrium between surface fluxes and transport by the subsiding flow (Helliker et al., 2004; Bets et al., 2004).

This paper uses boundary-layer equilibrium concepts to interpret discrepancies between modeled and observed concentration gradients in terms of transport model errors. Our results show that these discrepancies most likely result from overestimated as opposed to underestimated vertical transport and mixing, implying overestimated northern terrestrial carbon sinks in the inversions. However we find that seasonal concentrations alone cannot distinguish transport model errors from errors in prior-specified surface fluxes, and propose a new diagnostic to isolate the effects of transport and mixing.

2 Methods

2.1 Mixed-layer approximation

The tracer conservation equation allows us to relate transport and mixing to modeled or observed trace gas concentrations. We assume dry convection maintains well-mixed trace gases in the boundary layer, and refer to this boundary layer as the mixed-layer. The corresponding tracer conservation equation (e.g. Bets, 1992) is given by

$$\rho_m \frac{\partial}{\partial t} (hc_m) - \rho_f c_f \frac{\partial h}{\partial t} + \rho_f w (c_f - c_m) + \rho_m hv \cdot \nabla c_m = F$$

where $h$, $c_f$, $c_m$, $\rho$, $w$, $v$, and $\nabla$ are the mixed-layer depth, free troposphere and mixed-layer trace gas mixing ratios, atmospheric molar density, vertical wind velocity evaluated at the mixed layer height, horizontal wind velocity vector, and horizontal gradient operator, respectively; subscripts $f$ and $m$ denote quantities at the free-troposphere level just above the mixed-layer and averaged within the mixed layer, respectively. The surface flux or net ecosystem exchange ($F$) balances the sum of mixed-layer CO$_2$ storage (first left-hand side term), entrainment of free-troposphere CO$_2$ owing to growth of the mixed-layer into the free-troposphere (second term), vertical advective transport averaged over the mixed-layer (third term), and horizontal advection (fourth term). Note the horizontal gradient operator and horizontal wind vector have components in both the meridional and zonal directions, and therefore the horizontal advection term includes both meridional and zonal advection.

It helps to keep in mind that the terms involving $\partial h/\partial t$ (first and second left-hand side terms of Eq. (1)) and the vertical advection (third left-hand side term) represent two separate physical processes (Bets, 1992). The former accounts for entrainment of free-troposphere CO$_2$ by the mixed-layer growing into the free-troposphere, whereas the latter implicitly accounts for the entrainment of free-troposphere CO$_2$ that has descended to the top of the mixed-layer through vertical CO$_2$ advection. We refer to these processes as entrainment and vertical advective transport, respectively, but use the term vertical transport and mixing when referring to the combination of both processes. Note also that net loss of mixed-layer air to the free-troposphere by ascending winds does not directly affect mixed-layer concentrations, in which case we must replace $c_f$ with $c_m$ as the top boundary condition on CO$_2$ in Eq. (1). This dynamic boundary condition arises because the mixed-layer top moves relative to the vertical wind, and vice versa.

We computed the first and second left-hand side terms of Eq. (1) from day-to-day changes in afternoon (01:00–04:00 p.m. local time) mixed-layer depths and concentrations. Turbulence becomes shallow and surface emissions (e.g., ecosystem respiration) accumulate in a shallow nocturnal boundary layer at night. However the rapid decay of turbulence after sunset leaves a relic mixed-layer, or...
so-called residual layer, extending from the nocturnal boundary layer to the depth of the afternoon mixed-layer, where CO₂ concentrations are similar to the afternoon mixed-layer (Yi et al., 2001). Therefore, we take \( z_f \) as the total depth of the residual-layer and mixed-layer system and integrate (Eq. 1) over the diurnal cycle by assuming (1) much larger depth-integrated advective tendencies (third and fourth terms of Eq. 1) in the residual layer than in the nocturnal boundary layer, due to the much larger residual layer depth and wind speed; and (2) steady nighttime vertical concentration gradients between free-troposphere and residual layer that can be approximated by afternoon concentrations. Any accumulation of CO₂ in the shallow nocturnal boundary layer shows up in the mixed-layer concentrations the following day. Previous studies used these same approximations in various forms, to close the CO₂ budget over diurnal cycles (Chou et al., 2002; Bakwin et al., 2004; Helliker et al., 2004; Yi et al., 2004).

3 Measurements and model data

Our study uses atmospheric concentration measurements collected at the Central Facility (36.61° N, 97.49° W) of the US Southern Great Plains Atmospheric Radiation Measurement Climate Research Facility (SGP) between January 2003 and January 2008. More than 80% of the land surface of the Southern Great Plains is managed for agriculture and grazing (Fischer et al., 2007). Winter wheat grows from November through June over 40% of the region (Fischer et al., 2007), mostly to the southeast (Riley et al., 2009), with the remaining area dominated by pasture (40%) and a mixture of C3 and C4 crops (20%) that grow from April through August (Cooley et al., 2005).

A precision gas system (Bakwin et al., 1995) was used to obtain mixed-layer CO₂ concentrations at 15-minute intervals on the 60 m tower. Pressurized air samples have been collected approximately weekly on the 60 m tower and in the free-troposphere at SGP for subsequent analysis at NOAA/ESRL. The continuous mixed-layer CO₂ concentrations were compared with the flask-based measurements to account for and correct possible drifts. These flask-based measurements include, but are not limited to, CO₂, CH₄, CO, N₂O, CO, SF₆, H₂, and \(^{13}\)C and \(^{18}\)O in CO₂. The sample collection procedures have been described in detail in Conway et al. (1994). Typically, air was pumped into a pair of 2.5 L glass flasks, connected in series, and slightly pressurized above ambient pressure. For the free-troposphere concentrations we used the first available flask sample just above the CT/TM5 mixed-layer depth (samples were typically available at altitudes of 457.2, 609.6, 914, 1219.2, 1524, 1828.8, 2133.6, 2438.4, and 2743.2 m above ground, and higher, with an uncertainty of about 30 m).

The 2008 CarbonTracker data assimilation system (hereafter CT/TM5) provided mixed-layer depths and three-dimensional distributions of CO₂ mole fractions and surface fluxes at 1°×1° spatial resolution every 3-h (Peters et al., 2007). CT/TM5 accounts for the effect of surface energy forcing on mixed-layer depth, through the prognostic energy budget in the underlying transport model (Transport Model 5, Krol et al., 2005). CT/TM5 incorporates surface flux measurements and model representations of ecosystem exchanges in a global, two-way nested atmospheric transport model driven by meteorological fields from the European Centre for Medium-Range Weather Forecasts (ECMWF).

Our analysis includes observations from the SGP tower, and CT/TM5 data averaged over the two model grid points nearest to three sites including SGP, described in the section above; LEF (45.95° N, 90.27° W), characterized by a managed forest of mixed northern hardwood, aspen, and wetlands; and Harvard Forest (HFM, 42.54° N, 72.17° W), a managed, deciduous forest. These sites correspond to some of the North American aircraft flask sampling locations used in a related study (Stephens et al., 2007).

The CT/TM5 dataset did not archive vertical advection, which we recreated here with vertical velocities from the ECMWF interim reanalysis, based on the same general circulation model and parameterization schemes in CT/TM5. Differences between CT/TM5 and our recreated advective tendencies are expected in part due to differences in the forecast time-steps used to create each dataset, and interpolation of the ECMWF meteorological data from 1.5°×1.5° to 1°×1° resolution in CT/TM5. We averaged the two CT/TM5 grid-points closest to each of our study sites for use with the ECMWF reanalysis vertical velocities, due to the difference in resolution of these products. Additional spatial averaging had little effect on the results. Resolution sensitivity of the recreated vertical advective tendency was investigated by spatially averaging ECMWF velocities over the 1 through 4 grid-cells nearest the SGP site, and was found to be small. Sensitivity was further tested using vertical velocities from three independent data assimilation systems (RUC, NCEP, and NARR), which were qualitatively similar to ECMWF velocities and did not have a notable effect on our results.

4 Timescale dependence

4.1 Scaling

Previous studies made approximations to the conservation equation (Eq. 1) by neglecting either entrainment and storage (Bakwin et al., 2004; Helliker et al., 2004) or vertical advection (e.g. Yi et al., 2004), referred to here as the equilibrium and non-equilibrium approximations, respectively. The choice of approximation has important implications for transport model errors. We apply dimensional analysis to Eq. (1) to inform the appropriate approximation, by scaling the ratio of the sum of CO₂ storage and entrainment to vertical advection according to the ratio of a
mixed-layer relaxation time ($\tau$) to a characteristic timescale ($T$) of Eq. (1). We introduce the mixed-layer relaxation time as the ratio of characteristic mixed-layer depth to a characteristic subsidence rate ($\tau = H/W$). We refer to the ratio of these timescales as $\tau^*=H/WT$. The timescale ($T$) can be chosen to represent the timescale of interest, for the purpose of scaling the advective and storage and entrainment terms. Note that we later apply a running time-average to Eq. (1), which imposes a lower limit on the timescale $T$ as determined by the averaging time.

The relaxation time $\tau = H/W$ characterizes how long it takes for tracer concentrations to come into equilibrium with vertical transport by the subsiding flow. The characteristic subsidence rate $W$ reflects the aggregate of all processes affecting subsidence, including synoptic systems. Frontal passages and other mechanisms of ascent are coupled to subsidence through the conservation of mass and energy (e.g. Lawrence and Salzmann, 2008). Adiabatic warming approximately balances infrared radiative cooling in the subsiding branches of the circulation, which in turn balances latent heating by moist convection in the precipitating storm systems that comprise the ascending branches.

Dimensional analysis predicts that the equilibrium approximation applies to the seasonal cycle when the relaxation time is significantly shorter than a season (i.e. $\tau^* \ll 1$), in which case the storage and entrainment terms can be neglected relative to vertical advection. We tested this prediction by calculating the storage, entrainment, and vertical advection in Eq. (1) and applying a running average for averaging times ranging from 1 to 90 days. The averaging time corresponds to the shortest timescale resolved by the averaged equation, which helps quantify the relative importance of each process at different timescales. We added storage and entrainment together to form a single budget term, and divided the timeseries of this and the other terms into non-overlapping segments of length ranging from 1 to 90-days, to obtain a statistical ensemble of CO$_2$ budgets for each averaging time. We used non-overlapping segments to minimize statistical dependence among ensemble members. The 90-day non-overlapping segments have only one sample for each season in each year, for a total of 5 and 7 ensemble members for the SGP and CT/TM5 data, respectively (one for each year of data), whereas the 45-day non-overlapping segments contain 10 and 14 ensemble members, and so on.

We quantified the relative importance of each term as a function of timescale, by taking the magnitudes of these budget terms, and taking the ensemble-median of their ratios (Figs. 1 and 2).

Our results imply that previous studies based on non-equilibrium approximations did not capture the transport and mixing processes most important at seasonal timescales, when surface fluxes (Fig. 1) and vertical advective transports (Fig. 2) exceed storage and entrainment by an order of magnitude. We obtained similar results when calculating the budget terms from observed concentrations at SGP (Fig. 3) or from CT/TM5 data for SGP, LEF and HFM (Fig. 4). We split the seasonally-averaged vertical advection term into a linear and non-linear part (i.e., $w\Delta c = \bar{w}\Delta \bar{c} + w'\Delta c'$), for reasons that will become clear in Sect. 5. This Reynolds decomposition follows from writing the components of vertical advection in terms of 90-day averages and departures from these averages (e.g., $w = \bar{w} + w'$, $\Delta c = \Delta \bar{c} + \Delta c'$, where primes denote departures from the 90-day average) and $\Delta \bar{c}$ denotes the 90-day averaged vertical concentration gradient ($\Delta \bar{c} = \bar{c}_m - \bar{c}_f$). The

![Fig. 1. Ratios of the sum of entrainment and storage to net surface flux, for various averaging times between 1 and 90-days during June, July, August (JJA) and December, January, and February (DJF). Ratios were calculated using the CT/TM5 model output at all three sites (SGP, LEF, HFM), combined with meteorological data from ECMWF (see text for details).](image-url)
I. N. Williams et al.: Boundary layer equilibrium and CO₂ inversions

Fig. 2. As in Fig. 1 but for the ratio of the sum of entrainment and storage to vertical advection calculated from 60-m tower and aircraft observations at SGP (a) and from CT/TM5 at SGP, LEF, and HFM (b).

Fig. 3. Contribution of mixed-layer budget terms to the surface flux at SGP, calculated from 90-day running averages using 60-m tower and aircraft mixing ratios, and decomposed into horizontal advection (green), vertical advection (blue), storage plus entrainment (red) and the sum of all terms (thick black).

non-linear vertical advection is on the order of the horizontal advection at SGP and LEF, which highlights the importance of weather disturbances on seasonal transport. The surface flux predicted using the equilibrium approximation (Fig. 5a, calculated from Eq. (1) after neglecting storage and entrainment) approximately agrees with the surface flux predicted from the data assimilation scheme internal to CT/TM5 (Fig. 5b).

5 Vertical gradients and rectifier effect

We explored how seasonality in vertical transport contributes to seasonal rectification, by examining height-time cross sections of the vertical wind field (Fig. 7, top three panels), with seasonal variability in mixed-layer depth overlaid as solid black lines in the top three panels of Fig. 7. The cross section shows the 90-day running average subsidence velocities as a function of height above the surface, for the seven annual timeseries extending from 1 January–31 December, for January 2001–2008. Note that the 90-day average subsidence velocity at the 90-day average mixed layer depth (as indicated by the top three panels of Fig. 7) is not
Fig. 5. Surface flux inferred from the equilibrium approximation (a) and the CT/TM5 assimilated surface flux (b) for SGP (red), LEF (dashed black), and HFM (blue), using 90-day averages. Equilibrium fluxes (a) are given by the sum of horizontal and total vertical advection shown in Fig. 4.

Fig. 6. Vertical mixing ratio gradient inferred from the equilibrium approximation (a) and from the CT/TM5 data assimilation system (b) at SGP (red), LEF (dashed black), and HFM (blue), using 90-day averages.

The results show that mixed layer depth alone does not fully explain the seasonal rectification of vertical concentration gradients. Subsidence rates vary seasonally and therefore also contribute to the seasonal rectifier effect. In fact we find an anti-correlation between mixed-layer depths and subsidence rates at HFM, where the coincidence of strongest subsidence with strongest respiratory fluxes in winter helps to reduce winter mixed-layer concentrations relative to the free troposphere, bringing the winter vertical gradients at HFM closer to those of other sites. Other locations across eastern North America and the eastern Atlantic also have reversed seasonality in subsidence rates (see Supplement, Fig. S2), possibly related to topographic forcing and stationary wave patterns (Saltzman and Irsch, 1972).

6 Relaxation times and vertical mixing diagnostic

Our results call for a new vertical mixing diagnostic that takes into account both the strength of the divergent circulation and mixed layer depth variations. The boundary layer relaxation time $\tau = H/W$ (see Sect. 4.1) provides one such measure, which we can estimate from autocorrelations of vertical concentration gradient fluctuations. To obtain the relationship between vertical mixing and concentration autocorrelations, we draw an analogy between Eq. (1) and a first-order autoregressive process defined by

$$\frac{dX(t)}{dt} + aX(t) = Z(t)$$  \hspace{1cm} (3)

where $X(t)$ is a continuous random variable, $a$ is a constant, and $Z(t)$ represents a white noise process with zero mean (e.g. Jones, 1975; Chatfield, 2004). We make this analogy explicit by rearranging Eq. (1) to yield

$$\frac{d}{dt}(h\Delta c) + \langle \nabla \cdot \mathbf{v} \rangle h\Delta c = G(t)$$  \hspace{1cm} (4)

where we assumed that free-troposphere mixing ratios vary slowly in time compared to mixed layer mixing ratios. Note that $h\Delta c$ is analogous to $X(t)$ in Eq. (3) and the equation is evaluated at a fixed latitude and longitude. We used the vertically-integrated continuity equation,

$$\rho_f w = -\rho_m \langle \nabla \cdot \mathbf{v} \rangle h$$  \hspace{1cm} (5)

to relate the subsidence rate at the mixed-layer top ($w$ in Eq. (1)) to the vertically-averaged horizontal wind divergence (bracketed term in Eq. (4)), assuming constant divergence in the mixed-layer and zero vertical velocity at the surface (e.g. Betts, 1992). The term $G(t)$ represents the combination of surface fluxes and horizontal advection

$$G(t) = F/\rho_m - h\mathbf{v} \cdot \nabla c_m.$$  \hspace{1cm} (6)

The weighting of the vertical gradient $(\Delta c)$ by $h$ in Eq. (4) reflects the fact that the divergent circulation transports more mixed-layer mass per surface area as the depth of the mixed-layer increases, requiring either larger surface flux or smaller tracer vertical gradients to balance tracer transport.
Fig. 7. Top: Mean annual cycle of subsidence velocity (where $w < 0$) calculated from ECMWF data (years 2001-2007), contoured every 0.25 cm s$^{-1}$, overlaid with CT/TM5 90-day running average maximum daily mixed layer height (error bars indicate standard deviation of the mean). Below: Subsidence velocity at the 90-day running average mixed layer top ($w_{zf}$) (solid line) and at the annual average (constant) mixed layer depth (dashed line).

Fig. 8. Autocorrelation coefficient for perturbations in daily vertical mixing ratio gradients from aircraft and 60-m tower observations (blue square markers), and from CT/TM5 (red circle markers). Error bars indicate the standard deviation of the mean over all years (2003–2005 for observations, 2001–2007 for CT/TM5). Panels (a) and (b) correspond to summer and winter, respectively. The gray line indicates exponential decay toward the 90-day average value, according to Eq. (7) (width of the line indicates the standard deviation).

The diagnostic follows from Eq. (4) after noting that the autocorrelation of a first-order autoregressive process decays exponentially as a function of time lag, with a rate constant $a$ (cf. Eq. (3)). We therefore expect the autocorrelation of perturbations in $h \Delta c$ to decay according to

$$A = \exp[-(\nabla \cdot v)(t - t')]$$  \hspace{1cm} (7)
CT/TM5 and observationally-derived divergence rates (e.g. between $6.23 \times 10^{-6}$ for CT/TM5 and $6.10 \times 10^{-6}$ s$^{-1}$ for observations, in summer) were not statistically significant, and would amount to vertical concentration gradient errors on the order of 0.1 ppm (using $\Delta c \sim -F w^{-1}$ from Eq. (2)), much smaller than the errors reported in a previous study at other sites (Stephens et al., 2007).

These results do not necessarily conflict with previous work suggesting large errors in vertical transport and mixing (Stephens et al., 2007), particularly because we have not applied our diagnostic to sites showing large discrepancies between observations and transport models inversions. The CT/TM5 vertical concentration gradient is inconsistent with ECMWF reanalysis subsidence rates at HFM (see supplement, Fig. S2), which warrants further study, but those subsidence rates are model-derived and so may also be in error. Note that CT/TM5 comes into closer agreement with carbon inventories and has overall smaller concentration profile errors compared to the TransCom3 model inversions (Peters et al., 2007). Also, CT/TM5 uses a higher resolution (two-way nested) version of the TM5 model than what inverse studies have used, and assimilates observed and model-derived surface fluxes every 3-h, including effects of interannual variability and vegetation fires.

Our proposed diagnostic has the capability of determining if the systematic errors seen in transport model inversions result from errors in the modeled divergent wind field. Transport model inversions predict vertical concentration gradients almost twice as large as observations at some sites (Stephens et al., 2007). The equilibrium boundary layer approximation implies that these errors should appear as similarly large errors in mixed-layer divergence rates, or equivalently in subsidence rates at the mixed-layer depth (i.e. twice as fast in transport models as in observations, according to $\Delta c \sim -F w^{-1}$). Such large errors are on the order of the difference between winter and summer divergence rates at SGP, which is statistically significant in our analysis, and therefore should be detectable using the methods presented here.

We conclude that boundary layer relaxation times can diagnose vertical transport and mixing relevant to seasonal CO$_2$ budgets. Drawbacks to this method include the requirement that fluctuations about the seasonally averaged surface flux represent temporally uncorrelated noise. The validity of this assumption will vary according to the measurement site, but could be tested by comparing autocorrelations of CO$_2$ to those of other conserved tracers whose surface fluxes are less likely to be correlated at sub-seasonal timescales. Previous studies reported mixed-layer SF$_6$ autocorrelations (Denning et al., 1999), which were similar to our results using CO$_2$, but were not compared to the divergent wind field. Our work provides a method to relate these concentration statistics to transport and mixing in atmospheric models.

7 Discussion

Boundary layer equilibrium has important consequences for the interpretation of CO$_2$ flux inversion errors. Given the surface flux, equilibrium predicts a simple inverse proportionality between CO$_2$ vertical gradients and the vertical wind ($\Delta c \approx -F w^{-1}$), consistent with the hypothesis that models systematically underestimate summer vertical gradients due to overestimated vertical mixing (Stephens et al., 2007). However, the simple inverse proportionality between errors in vertical gradients and mixing only works when there are no systematic errors in the surface flux, horizontal advective transport, or non-linear vertical advective transport (i.e., synoptic-scale eddies), according to Eq. (2).

Systematic biases in vertical gradients could also result from errors in the initial fluxes specified in Bayesian-synthesis inversions, or in the biospheric models used for these inversions (and in CT/TM5), without having to invoke systematic transport model errors. Other studies also suggested inversion errors due to these prior fluxes, possibly resulting from seasonality in fossil fuel emissions (Gurney et al., 2005; Erickson et al., 2008) or errors in the seasonal amplitude or timing of modeled biospheric fluxes (Peters.
et al., 2007; Yang et al., 2007), which were not considered in past analyses of inversion sensitivity. Previous studies using SF6 did not indicate such large systematic errors in summer modeled transport (Gloor et al., 2007; Patra et al., 2009). Overestimated prior fluxes would overestimate boundary-layer CO2 concentrations relative to the free-troposphere in forward transport model simulations (Fig. 9a), similar to observed errors (Stephens et al., 2007) in transport model inversions.

As a counter example to the hypothesis that vertical mixing is systematically biased in transport models, consider a hypothetical transport model simulation having perfect vertical mixing and transport but subject to specification of overestimated summer prior surface fluxes (shown schematically in Fig. 9). Accurate transport implies that subsidence ($w < 0$) in this simulation always matches that of the real atmosphere. Overestimated summer fluxes (i.e. $F$ less negative than observed) require larger free-tropospheric concentrations in the forward simulation (solid circles in Fig. 9a) than in observations (squares in Fig. 9a), and correspondingly weaker vertical gradients, according to $\Delta c \approx -Fw^{-1}$.

Unless the inversion of this transport is tightly constrained to observed concentrations, the post-inversion vertical gradient may remain underestimated, falsely indicating summer overestimated mixing, while free-tropospheric concentrations would remain overestimated, falsely indicating underestimated summer mixing. This example illustrates why either CO2 concentrations or vertical CO2 gradients taken alone do not always indicate transport model errors, and how opposite conclusions about these errors can be drawn when free-troposphere concentrations are considered separately of mixed-layer concentrations.

Previous studies cited underestimated model mixed layer depths as a mechanism for underestimated summer mixing (Yi et al., 2004; Denning et al., 2008), and as an explanation for underestimated seasonal amplitudes of modeled free-tropospheric and column-average CO2 (Yang et al., 2007). However, we found an anticorrelation between mixed-layer depth and the strength of the divergent circulation at some sites, such that vertical mixing diminishes in summer when the boundary layer is deepest. We illustrate these errors schematically in Fig. 9b,c (circles and squares indicate model and observations, respectively). Boundary layer equilibrium predicts that underestimated summer mixing should lead to overestimated vertical concentration gradients (Fig. 9c), whereas observational studies found underestimated gradients (Stephens et al., 2007). In the case of overestimated summer mixing (Fig. 9b), the hypothetical perfect prior flux would be adjusted to take up more CO2 in order to minimize differences between the forward-transport simulation and observations, after the inversion procedure. Overestimated summer mixing would therefore be more desirable with regard to explaining why the northern land carbon sink is stronger in inversion estimates than in land carbon inventories.

The equilibrium boundary layer approach does not consider mixing by convective clouds, and so may underestimate the extent to which spring and summer flux inversions could be in error due to transport model errors. However, the resolved-scale subsidence velocity in the data assimilation systems used here accounts for the larger-scale effects of transport and mixing at the sub-grid scale, due to separate enforcement of mass and energy balance at both sub-grid and global scales in the models underlying these datasets (Lawrence and Salzmann, 2008). This process is reflected in the reasonable agreement between surface fluxes and vertical gradients from data assimilation systems and those reconstructed using the equilibrium approximation and resolved-scale model winds. Improvements to the parameterization of mixing and transport by convective clouds are still needed, especially since these parameterizations were designed to realistically simulate energy balances for climate studies rather than tracer transport.

8 Conclusions

Previously reported discrepancies between modeled and observed concentration gradients most likely result from overestimated as opposed to underestimated vertical transport and mixing, implying overestimated northern terrestrial carbon sinks in the inversions. However, seasonal concentration gradients alone cannot distinguish between transport model errors and errors in prior-specified surface fluxes, according to boundary layer equilibrium concepts. We propose using the additional information contained in concentration gradient fluctuations, to diagnose vertical mixing errors independently of errors in seasonal surface fluxes.

Previous studies assumed that boundary layer depth indicates vertical mixing strength, whereas we found anticorrelations between these quantities at some sites. Underestimated model boundary layer depth therefore does not provide sufficient evidence to conclude that transport models underestimate northern terrestrial sinks. Vertical CO2 advection by the divergent wind field strongly contributes to observed vertical concentration gradients, and does not always track boundary layer depth. We recommend considering subsidence or mass divergence rates together with boundary layer depth when assessing transport model errors.

The equilibrium approximation neglects much of the complexity of atmospheric transport and mixing, yet even this simplified description contains more degrees of freedom than typical diagnostics constrain. Our results imply that discrepancies between modeled and observed vertical concentration profiles alone are not sufficient to prove that the models have systematic vertical transport and mixing errors. The methods developed here provide additional observational constraints needed to diagnose the several factors leading to errors and uncertainties in transport model inversions.
Supplementary material related to this article is available online at:

Acknowledgement. Funding for this study was provided by the US Department of Energy, BER Program, Contract # DE-AC02-05CH11231. CarbonTracker 2008 results provided by NOAA ESRL, Boulder, Colorado, USA from the website at http://carbontracker.noaa.gov. Andy Jacobson assisted with the CarbonTracker data.

Edited by: C. Gerbig

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