Determining the spatial and seasonal variability in OM/OC ratios across the US using multiple regression

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Abstract. Data from the Interagency Monitoring of Protected Visual Environments (IMPROVE) network are used to estimate organic mass to organic carbon (OM/OC) ratios across the United States by extending previously published multiple regression techniques. Our new methodology addresses common pitfalls of multiple regression including measurement uncertainty, colinearity of covariates, dataset selection, and model selection. As expected, summertime OM/OC ratios are larger than wintertime values across the US with all regional median OM/OC values tightly confined between 1.80 and 1.95. Further, we find that OM/OC ratios during the winter are distinctly larger in the eastern US than in the West (regional medians are 1.58, 1.64, and 1.85 in the great lakes, southeast, and northeast regions, versus 1.29 and 1.32 in the western and central states). We find less spatial variability in long-term averaged OM/OC ratios across the US (90% of our multiyear regressions estimate OM/OC ratios between 1.37 and 1.94) than previous studies (90% fell between 1.30 and 2.10). We attribute this difference largely to the inclusion of EC as a covariate in previous regression studies. Due to the colinearity of EC and OC, we find that up to one-quarter of the OM/OC estimates in a previous study are biased low. Assumptions about OC measurement artifacts add uncertainty to our estimates of OM/OC. In addition to estimating OM/OC ratios, our technique reveals trends that may be contrasted with conventional assumptions regarding nitrate, sulfate, and soil across the IMPROVE network. For example, our regressions show pronounced seasonal and spatial variability in both nitrate volatilization and sulfate neutralization and hydration.

1 Introduction

Atmospheric measurements have shown that organic mass (OM) is a major component of fine particulate matter (PM$_{2.5}$), comprising over 50% of ambient PM$_{2.5}$ in some locations (Jimenez et al., 2009; Murphy et al., 2006; Zhang et al., 2007). OM can be divided broadly into two components: organic carbon (OC), and all other mass which we will hereafter refer to as non-carbon organic mass (NCOM). NCOM is the largest component of ambient PM$_{2.5}$ that is not routinely measured. To achieve mass closure in source testing and ambient particle measurements, an OM/OC ratio (denoted as $k$ and $R_{OC}$ in some earlier literature, Frank, 2006; Malm and Hand, 2007) is often multiplied by measured OC to estimate total OM. This ratio is primarily affected by the oxygen content in the organic aerosol (Pang et al., 2006), although hydrogen, nitrogen, and sulfur also make small contributions to the NCOM.

The first estimate of OM/OC was made by White and Roberts (1977), who calculated an average ratio of 1.4 for specific organic compounds measured in Los Angeles. This value was used widely until Turpin and Lim (2001) analyzed a larger dataset to show that OM/OC is generally higher than 1.4. In recent years a range of techniques have been applied to quantify OM/OC, including gas chromatography/mass spectrometry (GC/MS) (Turpin and Lim, 2001; Yu et al., 2005), high resolution time of flight aerosol mass spectrometry (HR-ToF-AMS) (Aiken et al., 2008; Chan et al., 2010; Sun et al., 2009), Fourier Transform Infrared (FTIR) spectroscopy (Gilardoni et al., 2007; Kiss et al., 2002; Liu et al., 2009; Polidori et al., 2008; Reff et al., 2007; Russell, 2003; Russell et al., 2009), sequential extraction followed by gravimetric weighing and thermal optical measurement of carbon (El-Zanan et al., 2005, 2009; Lowenthal et al., 2009;
Polidori et al., 2008), and coupled thermal gravimetric and chemical analyses (Chen and Yu, 2007). Those studies have contributed substantially to our understanding of NCOM in many laboratory and field settings, but none of the techniques have been applied over a broad temporal and spatial range.

Numerous PM$_{2.5}$ constituents, including OC but not OM, are measured routinely across two large US networks: the Chemical Speciation Network (CSN) and the Interagency Monitoring of Protected Visual Environments (IMPROVE) network. A technique for computing OM from these networks could yield a comprehensive dataset of OM/OC ratios covering a large spatial and temporal extent. Frank (2006) developed the SANDWICH method to estimate OM from measurements across the urban-centric CSN. He calculated total OM as PM$_{2.5}$ minus the sum of other components (sulfate, nitrate, ammonium, crustal material, and elemental carbon (EC)), while making adjustments for particle-bound water (not measured directly) and nitrate volatilization. Unfortunately, the uncertainty in OC data collected at CSN sites prior to some major network changes in 2008 is comparable to the uncertainty in OM/OC ratios (Watson, 2008). Therefore, although the SANDWICH technique is useful for estimating total OM, CSN data are not yet adequate for estimating OM/OC over large multiyear periods.

The IMPROVE network tracks visibility degradation in national parks and wilderness areas via routine measurements of PM$_{2.5}$ mass and composition (Malm et al., 1994). The network began with 36 monitoring sites in 1988, and currently reports data from 178 remote and 13 urban sites across the continental US, Hawaii, Alaska and the Virgin Islands (http://vista.cira.colostate.edu/improve/Data/IMPROVE/AsciiData.aspx). PM$_{2.5}$ is collected on filters for a 24-hour period (midnight to midnight) every third day. The filters are subjected to a gravimetric analysis that measures total mass and various chemical analyses that measure bulk composition. Specifically, OC and EC are measured by the Thermal Optical Reflectance (TOR) combustion method; SO$_4^{2-}$, NO$_3^-$, and Cl$^-$ by ion chromatography; and elements with atomic weights between sodium and lead by X-Ray Fluorescence (XRF). Table 1 summarizes the IMPROVE measurements used for this paper and the filter medium on which each particle component is collected. In addition to these direct measurements, the network reports a reconstructed fine mass (RCFM) concentration which is a weighted sum of selected chemical constituents. RCFM was first calculated using Eqs. (1) and (2) (Malm et al., 1994), though our notation differs slightly from the original publication.

\[
\text{RCFM} = (\text{Na}_2\text{SO}_4 + \text{SOIL} + \text{EC} + \text{OM}) \]  \hspace{1cm} (1)

\[
\text{SOIL} = 2.20\text{Al} + 2.49\text{Si} + 1.63\text{Ca} + 2.42\text{Fe} + 1.94\text{Ti} \]  \hspace{1cm} (2)

Ammonium sulfate (\(\text{NH}_4\text{SO}_4\)) was calculated as 4.125 x S (sulfur was measured by Particle Induced X-ray Emission (PIXE) until 2002 and by XRF since then), SOIL was approximated using Eq. (2) (assuming the soil in PM$_{2.5}$ samples mimics the average composition of sedimentary rock), and OM was estimated as $1.4 \times \text{OC}$. Changes to the RCFM equation since 1994 include the addition of more components (ammonium nitrate (NH$_4$NO$_3$), non-soil potassium, and sea salt), modification of Eq. (2) to eliminate Al, and an increase of OM/OC from 1.4 to 1.8 (McDade, 2008).

Although a network-wide OM/OC ratio is commonly used to compute RCFM, a few studies have estimated site-specific OM/OC ratios from IMPROVE data. El-Zanan et al. (2005) describe a mass closure technique for calculating OM/OC,

\[
\frac{\text{OM}}{\text{OC}} = \frac{\text{PM}_{2.5} - (\text{NH}_4\text{SO}_4 + \text{NH}_4\text{NO}_3 + \text{EC} + \text{SOIL} + \text{Other})}{\text{OC}} \]  \hspace{1cm} (3)

in which “Other” is the sum of sodium, chlorine, and trace elements measured by XRF that are not associated with soil (Lowenthal and Kumar, 2003). Unfortunately, there are many uncertainties associated with a mass closure analysis of IMPROVE data. First, assumptions must be made about two unmeasured PM$_{2.5}$ components: ammonium and particle-bound water. Since ammonium is not routinely measured at IMPROVE sites, sulfate and nitrate are commonly assumed to be fully neutralized by ammonium. Estimation of water mass is complicated by the fact that filter samples are shipped at ambient conditions and weighed in a laboratory where relative humidity (RH) is not controlled. Second, nitrate measurements are made from particles collected on nylon filters downstream of a HNO$_3$ denuder, to which nitrate adheres well, whereas PM$_{2.5}$ weights are determined from Teflon filters, from which nitrate is known to volatilize (Hering and Cass, 1999). The amount of volatilization from the Teflon filter depends on which cation the nitrate is bound to as well as the temperature and RH during sampling, shipping, and analysis. Third, the IMPROVE soil equation relies on assumptions about the abundance and oxidation states of various trace elements. Since soil composition is spatially heterogeneous, this equation may not accurately estimate the soil contribution at all sites. Finally, OC measurement artifacts contribute additional uncertainty because OC is measured from quartz filters while OM is derived from gravimetric measurements on Teflon filters. Differing tendencies among these

<table>
<thead>
<tr>
<th>Analyte</th>
<th>Measurement Technique</th>
<th>Filter Type</th>
</tr>
</thead>
<tbody>
<tr>
<td>PM$_{2.5}$</td>
<td>Gravimetric</td>
<td>Teflon</td>
</tr>
<tr>
<td>Nitrate and Chloride</td>
<td>Ion Chromatography</td>
<td>Nylon</td>
</tr>
<tr>
<td>Si, S, K, Ca, Ti, and Fe</td>
<td>X-Ray Fluorescence</td>
<td>Teflon</td>
</tr>
<tr>
<td>OC and EC</td>
<td>Thermal Optical Reflectance</td>
<td>Quartz</td>
</tr>
</tbody>
</table>

Table 1. Summary of measurement techniques and filter types for each PM component included in the regression analyses. For details, see Malm et al. (2004) and the IMPROVE data guide (http://vista.cira.colostate.edu/improve/Publications/OtherDocs/IMPROVEDataguide/IMPROVEDataguide.htm).
two filter materials at retaining OM and/or adsorbing semi-volatile organic gases may affect OM/OC estimates.

To overcome some shortcomings of the mass-closure approach, Malm and collaborators developed a multiple regression technique to estimate OM/OC from 1988–2003 IMPROVE data (Hand and Malm, 2006; Malm et al., 2005; Malm and Hand, 2007). They fit seven coefficients in Eq. (4) using ordinary least squares (OLS) regression at each monitoring site. Some notation in Eq. (4) has been changed from that of Malm and Hand (2007) for consistency with the present study.

\[
\text{PM}_{2.5,i} = \beta_0 + \beta_{\text{OC}} \text{OC}_i + \beta_{\text{salt}} (\text{NH}_4)_2\text{SO}_4,i + \beta_{\text{nitr}} \text{NH}_4\text{NO}_3,i + \beta_{\text{soil}} \text{SOIL}_i + \beta_{\text{EC}} \text{EC}_i + \beta_{\text{seasalt}} \times 1.8\text{Cl}_i^{-} + \epsilon_i
\]  

(4)

The subscript, \(i\), represents a day-specific sample and \(\beta_0\) represents a site-specific intercept. The remaining \(\beta\) coefficients represent ratios of the mass associated with a given PM\(_{2.5}\) component on the Teflon filter when it was weighed to the mass of that same component determined (or estimated) via chemical analysis of a (possibly) separate filter. The residual error (\(\epsilon_i\)) denotes the difference between the measured PM\(_{2.5}\) mass and the estimated mass (based on fitted coefficients and measured chemical components) for a particular sample. The coefficient of most interest to us is \(\beta_{\text{OC}}\) because it represents OM/OC. This technique circumvents many of the assumptions needed for mass closure. For example, \(\beta_{\text{OC}}\) is insensitive to the degree of sulfate neutralization since the relative abundance of ammonium would mainly affect \(\beta_{\text{salt}}\). However, OC measurement artifacts can bias the \(\beta_{\text{OC}}\) coefficient.

In this paper we develop a nationwide dataset of seasonally- and spatially-varying OM/OC ratios across the IMPROVE network by extending the methodology of Malm and Hand (2007) while addressing some common pitfalls in multiple regression. We discuss new quantitative insights that we apply is completeness. If a major component in Eq. (5) (i.e., PM\(_{2.5}\), OC, S, NO\(_3\), Si, Ca, Fe, Ti, or EC)

\[
\text{PM}_{2.5,i} = \beta_{\text{OC}} \text{OC}_i + \beta_{\text{salt}} (\text{NH}_4)_2\text{SO}_4,i + \beta_{\text{nitr}} \text{NH}_4\text{NO}_3,i + \beta_{\text{soil}} \text{SOIL}_i + \beta_{\text{EC}} \text{EC}_i + 1.8\text{Cl}_i^{-} + 1.2\text{KNON}_i + \epsilon_i
\]  

(5)

\[\text{KNON} = K - 0.6Fe\]  

(6)

\[\text{SOIL} = 3.48\text{Si} + 1.63\text{Ca} + 2.42\text{Fe} + 1.94\text{Ti}\]  

(7)

In contrast to Eq. (4), we assume that EC has no artifact and set its coefficient to 1 because treating EC as a separate explanatory variable can bias \(\beta_{\text{OC}}\) (see Sect. 3.3 and Supplement Sect. S3). Similar to Eq. (4), we estimate sea salt as 1.8 Cl\(^{-}\) (Pitchford et al., 2007; White, 2008) but do not treat it as an explanatory variable. Although 1.8 Cl\(^{-}\) has been deemed a good estimate of sea salt mass at coastal IMPROVE sites, it may underestimate sea salt concentrations at inland locations where Cl\(^{-}\) has been displaced from the aged sea salt. However, this underestimation should not substantially affect the regression results because sea salt contributes little to PM\(_{2.5}\) mass at most inland locations. Second, we add KNON to Eq. (5) for consistency with the newest IMPROVE RCFM formula (McDade, 2008). KNON represents non-soil potassium (e.g., from wood burning) and is calculated using Eq. (6). The KNON coefficient is fixed at 1.2, the mass ratio of potassium oxide to potassium. Although KNON is influenced by soil composition (i.e., soil K/Fe ratio may deviate from 0.6), it contributes a small enough mass to total PM\(_{2.5}\) that fixing its coefficient should not adversely affect the regression as a whole. Third, we use an updated IMPROVE soil equation (compare Eqs. 2 and 7) which eliminates aluminum from the calculation because Al is not reliably measured by the IMPROVE XRF analysis (McDade, 2008).

We downloaded the IMPROVE data from http://views.cira.colostate.edu/web/DataWizard/ on 6 January 2010, and analyzed the measurements collected at 186 continental US sites between 1 January 2002 and 31 December 2008. All analyses are performed using the R statistical software package (R Development Core Team, 2010). Like Malm and Hand (2007), we segregate the data by monitoring site. In addition, we segregate data by season: quarter 1 (January, February, March), quarter 2 (April, May, June), quarter 3 (July, August, September), and quarter 4 (October, November, December), because we expect the coefficients (i.e., OM/OC and nitrate volatilization) to vary seasonally. However, we could not justify the seasonal variability in soil coefficients estimated from our initial analyses. For instance, the variability in \(\beta_{\text{soil}}\) was not correlated to Asian dust plumes or other seasonally varying dust sources. We therefore hold the soil coefficient constant throughout the year by first performing a multiyear regression at each site using all data from 2002–2008 and then fixing \(\beta_{\text{soil}}\) in each quarter-specific regression to the \(\beta_{\text{soil}}\) value obtained from the multiyear regression at that given site.

Within site- and quarter-specific datasets, the only data filter that we apply is completeness. If a major component in Eq. (5) (i.e., PM\(_{2.5}\), OC, S, NO\(_3\), Si, Ca, Fe, Ti, or EC)
Fig. 1. Flow diagram outlining regression methodology used in this work. Some results appear in multiple tables as indicated by the footnotes.
organosulfur atoms. A conservative lower bound could be calculated assuming that all sulfur mass associated with organic molecules would be included in the $\beta_{\text{OC}}$. Surratt et al. (2008) report that up to 20% of sulfur may be contained in these organic compounds, so we expect the lowest reasonable value of $\beta_{\text{sulf}}$ to equal 0.59 (0.74 ± 0.8) to capture an admittedly extreme scenario in which all inorganic sulfate is in the form of sulfuric acid and 20% of the total sulfur is contained in organic compounds. A sulfate coefficient above 1 would indicate that there is extra mass associated with the particulate sulfate. This extra mass could come from water if the aerosol remains hydrated during gravimetric analysis. During the history of the IMPROVE network, RH in the gravimetric measurement laboratory was only recorded intermittently. We obtained laboratory measurements of RH during the gravimetric analysis of filters collected from September 2003 to May 2005 and from May to December of 2008 (personal communication, Charles McDade, 2009). The maximum reasonable $\beta_{\text{sulf}}$ is estimated using the 99th percentile of those measurements (i.e., 52% RH). At this humidity, the AIM model (Wexler and Clegg, 2002) (available at: http://www.aim.env.uea.ac.uk/aim/aim.php) computes hydrated (NH$_4$)$_2$SO$_4$ to have 53% more mass than dry (NH$_4$)$_2$SO$_4$ and hydrated NH$_4$HSO$_4$ to have 32% more mass than dry NH$_4$HSO$_4$. Therefore, 1.53 is a reasonable upper bound for $\beta_{\text{sulf}}$.

Nitrate coefficients less than 1 likely represent volatilization of NH$_4$NO$_3$ from the Teflon filter prior to gravimetric analysis. Hering and Cass (1999) report that the absolute amount of nitrate volatilization is a function of RH and temperature, but not ambient nitrate concentration (unless the calculated nitrate loss exceeds the ambient nitrate available). Thus, a proportional coefficient captures the average volatilization behavior reasonably well. Because a value of 0 (complete nitrate volatilization) would imply no statistical relationship between nitrate mass and PM$_{2.5}$ mass, a slightly negative $\beta_{\text{nit}}$ value caused by measurement error is just as likely as a slightly positive $\beta_{\text{nit}}$ value. Consequently, for each regression performed, we set the lowest reasonable value for $\beta_{\text{nit}}$ as 1.5 standard errors below 0 (calculation of standard errors is described in the Supplement, Sect. S1.1). There are 129 site/quarter groupings exhibiting negative $\beta_{\text{nit}}$ values within 1.5 standard errors of 0. To show that these negative values really represent slight variations around 0, we repeat each of these regressions without the nitrate term and find that $\beta_{\text{OC}}$ band $\beta_{\text{sulf}}$ coefficients change by less than 3% on average (no $\beta_{\text{OC}}$ and only six $\beta_{\text{sulf}}$ coefficients change by more than 5%). A $\beta_{\text{nit}}$ greater than 1 indicates that the assumption of dry NH$_4$NO$_3$ underestimates the actual nitrate mass on the Teflon filter at the time of weighing. This would occur either if the cation has a larger molar mass than ammonium (e.g. Na) or if there is water associated with the nitrate during weighing. Again a maximum reasonable value for $\beta_{\text{nit}}$ is determined by computing increases in water mass at 52% RH with the AIM model for both NH$_4$NO$_3$ and NaNO$_3$. This analysis shows that hydration can add 35% extra mass to the nitrate, so 1.35 is a reasonable upper bound for $\beta_{\text{nit}}$.

### 2.3 Effects of measurement uncertainty

Despite the aforementioned advantages of the regression method, it is subject to several pitfalls. One is that measurement uncertainty in the explanatory variables can bias the regression coefficients. An OLS regression assumes that explanatory variables are measured without error, but this assumption conflicts with the reality of our application in which measurement uncertainty is associated with all explanatory variables: OC, (NH$_4$)$_2$SO$_4$, NH$_4$NO$_3$, and SOIL. For regressions with a single explanatory variable that is uncertain, the coefficient is biased towards zero (Fuller, 1987; Saylor et al., 2006; White, 1998). With multiple explanatory variables, bias in the coefficients exhibits a complex dependency on the relative uncertainties in various components, the correlation between explanatory variables, the correlation between measurement errors, and other factors. White (1998) examined this problem in a simplified case with two correlated explanatory variables of which one was measured without error. For that case, he showed that the coefficient for the perfectly measured explanatory variable was artificially inflated while the other coefficient was diminished.

To evaluate this bias within the more complex conditions of the present study, we analyze synthetic datasets that mimic the IMPROVE data. Assuming that the actual values for each measurement were exactly equal to the reported value, we create 200 synthetic datasets for each site- and quarter-specific dataset that represent “observed” data with error in the explanatory variables. Errors are added by perturbing the reported values of OC, sulfate, nitrate, and PM$_{2.5}$ using the reported uncertainty and assuming that “observed” values would be normally distributed around the actual value. For each site- and quarter-specific dataset, we then perform an OLS regression on the reported dataset and the 200 synthetic datasets. The reported dataset is considered the “truth” in this exercise, so OLS regression yields “true” coefficients for comparison with the results from our synthetic datasets. Results from one such analysis for a regression with typical OLS biases (Gila Wilderness in New Mexico during quarter 1) are shown in the left half of each plot in Fig. 2. The dotted lines represent the “true” coefficients and the box plot shows the distribution of coefficients obtained from the 200 synthetic datasets. Although the true value could be accurately estimated from some synthetic datasets in this example, $\beta_{\text{OC}}$ is typically under-estimated while $\beta_{\text{sulf}}$ and $\beta_{\text{nit}}$ are over-estimated.

To overcome the biases associated with the OLS assumption of error-free explanatory variables, a class of methods has been developed to explicitly account for the existence of such errors; these are often collectively called measurement error models or errors-in-variables (EIV) models. Such methods typically assume that for all observations of each

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covariate, the errors are independent, identically distributed and follow a normal distribution with mean zero and a fixed (possibly unknown) standard deviation. In the IMPROVE data, the standard deviation is not fixed because we have a different estimated error associated with each observation of a given covariate, which we take as the standard deviation of the error distribution. To accommodate this added complexity, we turn to an advanced measurement error model described by Fuller (1987) (Sect. 3.1.2). The following discussion is based entirely on Fuller’s work, conforming to his original notation as much as is feasible.

To begin, we define $Y_t$ as the value of the response variable for observation $t$, such that $t = 1, 2, \ldots, n$, with $n$ representing the number of observations. For the multiyear regression, this response is given by $\text{PM}_{2.5} = (1.2 \text{ KNON} + 1.8 \text{ Cl}^- + \text{EC})$, and for the quarter-specific regression it is $\text{PM}_{2.5} = (1.2 \text{ KNON} + 1.8 \text{ Cl}^- + \text{EC} + \beta_{\text{soil}} \text{ SOIL})$. The row vector $X_t$ contains the observed values of the explanatory variables associated with observation $t$. The first element is the observed value of OC, the next element corresponds to (NH₄)₂SO₄, the third is NH₄NO₃, and the fourth is SOIL. (In the quarter-specific regression case, the SOIL component is omitted.) Note that the order of these explanatory variables mimics their order in Eq. (5) and is preserved in the various mathematical representations of their coefficients, errors, etc., which follow.

Additionally, we let $\sum_{\text{aunt}}$ represent the covariance matrix associated with $X_t$. Assuming that errors in each covariate are independent, this is a diagonal matrix. The elements along the diagonal contain the variance (square of the error standard deviation) associated with the explanatory variables, in the specified order. As an initial estimate for the regression coefficients, we use the method-of-moments estimator, the column vector $\hat{\beta}$, given by Eq. (8)

$$\hat{\beta} = \left[ n^{-1} \sum_{t=1}^{n} (X'_t X_t - \sum_{\text{aunt}}) \right]^{-1} \left[ n^{-1} \sum_{t=1}^{n} X'_t Y_t \right] \quad (8)$$

Having obtained this initial estimate, we work to refine it, as outlined by Fuller (1987). We define for each observation $t$ the matrix $\sum_{\text{aunt}}$. This is also a diagonal matrix, with the elements along the diagonal consisting of the variance for the response followed by the variances for the explanatory variables in the specified order. We take the square of the reported measurement uncertainty for each chemical constituent in a particular sample as its variance. (Note that the $\sum_{\text{aunt}}$ feature in Eq. (8) is simply a submatrix of $\sum_{\text{aunt}}$.) We also let $Z_t$ represent the row vector containing the observed response and the observed explanatory variables for each $t$; i.e., $Z_t = (Y_t, X_t)$. We then define the matrices $M$ and $A$ as

$$M = \sum_{t=1}^{n} \sum_{\text{aunt}} \quad \text{and} \quad A = \sum_{t=1}^{n} Z'_t Z_t$$

With these defined, we can now obtain an estimate of the variance associated with the regression error, denoted $\sigma_{\text{qq}}$. We first solve for the eigenvalues of the matrix product $M^{-1}A$. If the minimum of these eigenvalues is less than one, then $\sigma_{\text{qq}}$ is 0. Otherwise, $\sigma_{\text{qq}}$ is given by Eq. (9):

$$\sigma_{\text{qq}} = \sum_{t=1}^{n} \left[(n - k)^{-1} (Y_t - X_t \hat{\beta})^2 - n^{-1} (1, -\hat{\beta}')(\sum_{\text{aunt}} (1, -\hat{\beta}'))' \right] \quad (9)$$

Both $\hat{\beta}$ and $\sigma_{\text{qq}}$ are then used to obtain an estimate of the error associated with the linear relationship between the observed (with error) response and covariates, $\hat{\sigma}_{\text{vq}}$ (Eq. 10):

$$\hat{\sigma}_{\text{vq}} = \sigma_{\text{qq}} + \sigma_{\text{wq}} + \hat{\beta} (\sum_{\text{aunt}}) \hat{\beta} \quad (10)$$

where $\sigma_{\text{wq}}$ is the measurement variance associated with the response at time $t$. To obtain our final estimate, $\hat{\beta}$, of the regression coefficients, we combine the previous elements to obtain Eq. (11):

$$\hat{\beta} = \left[ \sum_{t=1}^{n} \sigma^{-1}_{\text{vq}} (X'_t X_t - \sum_{\text{aunt}}) \right]^{-1} \left[ \sum_{t=1}^{n} \sigma^{-1}_{\text{vq}} X'_t Y_t \right] \quad (11)$$

Here $\hat{\beta}$ is a column vector containing our estimates of $\beta_{\text{OC}}$, $\beta_{\text{aunt}}$, $\beta_{\text{nit}}$, and $\beta_{\text{soil}}$ (for the multiyear regression). Fuller (1987) also provides an estimator for the covariance matrix of $\hat{\beta}$. We use the diagonal elements of this matrix to obtain the standard errors for our estimated regression coefficients. In the interest of brevity, we leave further discussion of this variance estimate to the Supplement (Sect. S1). In
addition, sample R code used to perform these regressions is also supplied in Sect. S1.

We recognize that our method includes several assumptions. Perhaps most notable is the assumption that the measurement errors are independent among all the covariates and the response measured at a given date and location. The method could be extended to include information about the correlation between measurement errors, if such were known. This would result in non-diagonal matrices $\Sigma_{\text{uat}}$ and $\Sigma_{\text{uut}}$. Another key assumption is that the measurement error distributions are normal. If this is an unreasonable assumption, we could explore more complex statistical models that allow for nonnormal measurement errors, which are currently a subject of statistical research.

To demonstrate that this new technique reduces the bias in coefficients, we reanalyze all of our synthetic datasets using the EiV regression methodology. The results for quarter 1 data from Gila Wilderness are shown in the right-hand box plots of Fig. 2. Clearly, the EiV method yields coefficients that are much closer to the “truth” than the OLS methodology. To confirm the generality of this result, Fig. 3 shows the distribution of bias across all site- and quarter-specific datasets. Substantial bias in $\beta_{\text{OC}}$ (under-prediction), $\beta_{\text{sulf}}$ (over-prediction), and $\beta_{\text{uat}}$ (over-prediction) arise from the OLS regression, but these biases are greatly mitigated with the EiV technique. White (1986) provides a similar analysis of regression performance using measurements from the 1981–1982 Western Regional Air Quality Study. His analysis, which includes three explanatory variables (sum of ionic sulfate, nitrate, and ammonium; organic carbon; sum of silicon dioxide and calcium oxide), also found that correcting for measurement uncertainty reduces bias in the coefficients.

Although the EiV methodology shows improved results, it should be noted that additional error arises if the measurement uncertainties are biased themselves. Hyslop and White (2008) report some systematic biases in the measurement uncertainty from XRF, ion chromatography, and TOR carbon measurements at IMPROVE sites. If future updates to the IMPROVE data include substantial changes to uncertainty estimates for these components, it may warrant some repetition of the present work. For all subsequent analyses discussed in this paper, we apply the EiV method (instead of OLS).

### 2.4 Statistical identification of high-confidence regressions

After applying the EiV method to each multiyear and quarter-specific dataset, it is tempting to begin examining spatial and temporal patterns in the regression coefficients. However, as emphasized by Malm and Hand (2007), “Regression coefficients are vulnerable to a variety of systematic and random errors.” In this subsection, we establish some empirical guidelines for flagging or eliminating datasets that do not conform to Eq. (5). As summarized in the lower half of

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Fig. 3. Distribution of bias in regression coefficients for quarter-specific regressions at all IMPROVE sites. For each technique, we compute the median bias from 200 synthetic datasets at each site/quarter using ordinary least squares (blue) and errors-in-variables regression (black) and plot the distribution of those median values across all 612 site- and quarter-specific regressions. The red vertical line shows zero bias.

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Fig. 1, these guidelines are subsequently applied to identify regression results that can be used with “high confidence” for applications such as air quality model evaluations, source-apportionment analyses, epidemiology studies, and radiative calculations.

#### 2.4.1 Multicollinearity among explanatory variables

One requirement of our regression method (irrespective of choosing EiV or OLS) is that all explanatory variables be independent of each other. If any two $\text{PM}_{2.5}$ components are linearly related, the dataset is not suitable for regression analysis because the technique may over-estimate one coefficient and under-estimate another due to excess degrees of freedom. To identify such datasets, Pearson correlation coefficients ($r_p$) are calculated for all six couplings among the four explanatory variables ($\text{OC}$, ($\text{NH}_4)_2\text{SO}_4$, $\text{NH}_4\text{NO}_3$, and $\text{SOIL}$) in each site- and quarter-specific dataset. We examine all datasets having any $|r_p|$ values greater than 0.65 and look for cases in which the coefficient on one of the highly correlated explanatory variables appears to be over-estimated while the other appears under-estimated relative to the ranges established in Sect. 2.2. For example, sulfate and nitrate from 4th quarter measurements at the Puget Sound monitoring site are correlated with $r_p = 0.86$. In that regression, $\beta_{\text{sulf}} = 0.83$...
Fig. 4. Empirical selection of the 0.85 threshold \(|r_P|\) value for identifying site- and quarter-specific regressions which may be biased due to multicollinearity. See Sect. 2.4.1 for an explanation of what constitutes a regression that is “suspect.” The 452 EiV regressions with max \(|r_P| < 0.65\) were not examined when determining this empirical threshold.

A summary of our analysis across all sites and quarters is shown in Fig. 4, from which we determine that \(|r_P|\) values greater than 0.85 often indicate suspect results. We acknowledge that our empirical approach for setting this threshold value is not foolproof since (1) coefficients that appear skewed may actually be accurate, and (2) some regressions which are affected by co-linearity may not be identifiable if the estimated coefficients fall well within their physically reasonable ranges. However, our approach yields an easy-to-use procedure for screening out regression results that may be biased due to co-linearity in speciated PM$_{2.5}$ data. Seven quarter-specific datasets are eliminated from our analysis based on the max \(|r_P| > 0.85\) criterion (see list in Supplement Table S3).

2.4.2 Assessing the fit of the regression model

A second requirement for accurate regressions is that the equation used to fit coefficients is physically realistic. Based on our knowledge of ambient aerosol across the US, Eq. (5) includes all the essential PM$_{2.5}$ components. However, if a true coefficient for EC, Cl$^{-}$, or KNON is substantially different from our fixed coefficients for those species, the regression could be adversely affected. In addition, if the actual SOIL coefficient varies greatly throughout the year at any site, then our assumption of temporally-invariant \(\beta_{\text{soil}}\) could also degrade the regression results at that site. Finally, if the relationship between PM$_{2.5}$ mass and any major chemical component is nonlinear, our regression analysis will be inaccurate. For instance, if OC artifact corrections were biased high in clean conditions and vice versa, OC concentrations would be negatively (positively) biased in clean (polluted) conditions and the relationship between reported OC and total PM$_{2.5}$ would be nonlinear.

To identify cases influenced by one or more of these phenomena, we examine the residual errors \((\varepsilon_i)\) in Eq. (5) resulting from each site- and quarter-specific regression. Spearman rank order correlation coefficients \((r_S)\) are calculated between the \(\varepsilon_i\) values and each species used in Eq. (5): OC, S, NO$_3^-$, SOIL, EC, Cl$^{-}$, and KNON. Any strong correlation indicates that Eq. (5) is an inadequate representation of PM$_{2.5}$ at the given site/quarter. Examples are shown in Fig. 5. Following this analysis, a criterion of \(|r_S| > 0.4\) is imposed to eliminate 12 quarter-specific datasets that are likely affected by the problems discussed above (see list in Supplement Table S4). Nine of these datasets exhibit a strong correlation between \(\varepsilon_i\) and Cl$^{-}$, largely due to an abundance of negative Cl$^{-}$ concentrations in the underlying IMPROVE data. The negative Cl$^{-}$ values in 2002 and 2003 were caused by variability in filter blanks and a change of filter suppliers in 2004 corrected this problem (White, 2008). This exemplifies
2.4.3 Dataset selection and segregation

A third key element to obtaining meaningful regression coefficients from IMPROVE measurements is appropriate segregation of data. For this analysis, data are grouped by season and monitoring site with the intention that samples taken within each subset should yield fairly constant regression coefficients. However, sites that are strongly influenced by time-varying sources may not match our intent and therefore may not be ideal input for the regression analyses. For instance, a monitoring site that is impacted heavily on certain days by wildfires and on other days by diesel traffic will exhibit varying OM/OC ratios that violate our assumption of constant $\beta$ coefficients by quarter.

To check for temporal trends or irregularities during our 7 year study period, residual error values were binned by year and examined for each site- and quarter-specific dataset. This analysis was designed to identify three possible problems: (1) a one-time abrupt change in $\epsilon_i$ which could indicate a change in measurement methods, (2) a monotonic temporal trend in $\epsilon_i$ which could indicate changing aerosol characteristics at the site possibly due to emission regulations, and (3) a single year which shows vastly different $\epsilon_i$ from other years indicating that a distinct and infrequent event (e.g., forest fire or abnormal meteorology) affected the monitoring site.

Visual inspection of all datasets shows no evidence of problem 1. There was a change in EC and OC measurement equipment between 2004 and 2005 (White, 2007) as well as a coincident change in the calibration of the XRF sulfur measurements (White, 2009a). Details about these and other such changes to IMPROVE data can be found at [http://vista.cira.colostate.edu/improve/Data/QA_QC/Advisory.htm](http://vista.cira.colostate.edu/improve/Data/QA_QC/Advisory.htm). Despite these changes in OC, EC, and sulfur, no shift in residual values is apparent between 2004 and 2005 for the network as a whole (see Fig. 6). That year-to-year change is no greater than other inter-annual variations. Though we find no observable effect, we acknowledge that any change in measurement techniques adds uncertainty to our final results.

Seven site- and quarter-specific datasets exhibit temporal trends in which median residual values or the inter-quartile range of residual values either increase or decrease monotonically from 2002–2008 (i.e., problem 2 outlined above). One example is shown in Fig. 7a and all seven are listed in Supplement Table S6. Further investigation of these datasets by people with site-specific expertise would be worthwhile. Though we report these 7 sets of regression coefficients, we do not regard them as high-confidence results.

Finally, sites affected by an infrequent event are identified using two criteria: the inter-quartile range of $\epsilon_i$ in a single year does not overlap the inter-quartile range from any other year; or the year with the broadest inter-quartile range is greater than two times the second broadest inter-quartile range. An example of each phenomenon is shown in Fig. 7b and c. We re-run these regressions without the errant year and report results from both the full and abridged datasets in Table S6 of the Supplement. Of the 28 cases flagged, we regard 10 as high-confidence results because none of their coefficients are perturbed by more than 0.1 when the outlier year is removed. These cases are shaded in gray in Supplement Table S6 and also appear in Table S5. In the remaining 18 cases, further examination of the underlying measurements by site-specific experts is warranted.

3 Results

Table S2 in the Supplement shows our multiyear regression results. Tables S5, S6, and S7 show coefficients for all quarter-specific regressions along with standard error values, normalized mean errors (NME), and normalized mean biases (NMB). NME and NMB are calculated using Eqs. (12) and (13). NMB and NME values are generally small (mean NMB for all regressions in Tables S5, S6, and S7 = $-0.2\%$, maximum absolute NMB = $2.6\%$, mean NME = $8.5\%$, maximum NME = $22.6\%$) indicating that the IMPROVE data fit Eq. (5) quite well.

$$\text{NME} = \left( \frac{\sum_{i=1}^{n} |\epsilon_i|}{\sum_{i=1}^{n} \text{PM}_{2.5,i}} \right) \times 100\% \quad (12)$$
There is a substantially larger spread in \( \beta \) values across all US sites, with a median \( \beta_{\text{soil}} \) for all sites at 0.27. Of these, 2 have \( \beta_{\text{soil}} \) values that are physically unreasonable (see Table S2). Of these, 2 have \( \beta_{\text{soil}} \) values of 0.21 and 0.27 falling below those of known soil profiles (see Sect. 2.2). Both low \( \beta_{\text{soil}} \) values come from urban IMPROVE sites (New York City and Washington DC). In these locations, there are likely non-soil sources of Si, Ca, Fe, or Ti. For instance, residential wood combustion is a major source of all four elements, on-road vehicle exhaust is a major source of Si, Ca, Fe, and surface coating operations are a major source of Ti (Reff et al., 2009). In urban areas where such sources may dominate, Eq. (7) would overestimate total soil mass and might yield an erroneously low value of \( \beta_{\text{soil}} \). The other 5 problematic multiyear regressions have low \( \beta_{\text{soil}} \) values, for which the cause is unclear. We are nevertheless able to extract high-confidence values of \( \beta_{\text{OC}} \) at these sites by using the multiyear \( \beta_{\text{soil}} \) value in our quarter-specific regressions.

In total, 61 quarter-specific regressions (10%) have at least one physically unreasonable coefficient (see Supplement Table S7). The number of regressions with problematic coefficients is greatest in quarter 1 (\( n = 21 \)) and quarter 3 (\( n = 22 \)) and least in quarters 2 and 4 (\( n = 13 \) and \( n = 5 \) respectively). Problematic \( \beta_{\text{soil}} \) values from the multiyear regressions account for 8 of these (2 in each quarter).

Twenty of the 61 regressions with physically unrealistic coefficients are due to low \( \beta_{\text{OC}} \) values less than one, 17 of which occur in quarter 1. These low \( \beta_{\text{OC}} \) values may be caused by errors in OC artifact correction, as discussed in Sect. 3.3 and Supplement Sect. 3. Although the low \( \beta_{\text{OC}} \) values predominantly occur in quarter 1, this may be exacerbated by the fact that \( \beta_{\text{OC}} \) values are lower in quarter 1 than in other quarters (median \( \beta_{\text{OC}} \) in quarters 1, 2, 3, and 4 are 1.39, 1.83, 1.81, and 1.59 respectively). Therefore, a slight low bias would push more OM/OC ratios below 1 in the winter than in other seasons.

Eighteen of the 61 problematic regressions are due to negative \( \beta_{\text{nit}} \) values that are more than 1.5 standard errors below zero. Fourteen of these occur in quarter 3. There are two possible explanations for the high occurrence in quarter 3. First, nitrate concentrations are generally low in the summer. In quarter 3, network-wide median nitrate concentrations were only 3% of median PM\(_{2.5}\) (versus 11% and 6% for quarter 1 and the annual average, respectively). When the mass of an explanatory variable is low compared to the mass of other PM\(_{2.5}\) components, the model fit is not very sensitive to large changes in that coefficient. Second, these problematic \( \beta_{\text{nit}} \) estimations may be due to a large number of cases in quarter 3 when all the nitrate volatilized from the Teflon filter (see Sect. 2.2). The lower-bound for negative \( \beta_{\text{nit}} \) values (1.5 standard errors below 0) may be too conservative, leading us to flag regressions in which nitrate volatilization is 100% (i.e. \( \beta_{\text{nit}} \) is essentially 0) as problematic.

The third most frequent error comes from high \( \beta_{\text{nit}} \) values: 13 regressions estimate \( \beta_{\text{nit}} > 1.35 \). In general these data points have higher than average standard errors (the mean nitrate standard error for these regressions is 0.50 while the mean nitrate standard error for all site-specific regressions is 0.21). These large standard errors indicate highly uncertain estimates of \( \beta_{\text{nit}} \), possibly due to low nitrate concentrations.

Overall, 90% of our quarter-specific regressions yield physically reasonable coefficients for all explanatory variables. This leaves 511 high-confidence regressions (see Fig. 1) from which we can assess spatial and seasonal trends.

### 3.2 Spatial and temporal trends in \( \beta_{\text{soil}}, \beta_{\text{sulf}} \) and \( \beta_{\text{nit}} \)

Figure 8 shows the spatial pattern of \( \beta_{\text{soil}} \). Much of the country has \( \beta_{\text{soil}} \) values near 1, confirming that Eq. (7) does a reasonable job of estimating soil concentrations. Some notable departures from this are high values displayed in orange and

\[
\text{NMB} = \left( \frac{\sum_{i=1}^{n} \varepsilon_i}{\sum_{i=1}^{n} \varepsilon_{\text{PM2.5},i}} \right) \times 100\% \tag{13}
\]

3.1 Physically unreasonable results

Only 7 of the multiyear regressions (i.e., <5% of all IMPROVE sites) have a coefficient that is physically unreasonable (see Table S2). Of these, 2 have \( \beta_{\text{soil}} \) values of 0.21 and 0.27 falling below those of known soil profiles (see Sect. 2.2). Both low \( \beta_{\text{soil}} \) values come from urban IMPROVE sites (New York City and Washington DC). In these locations, there are likely non-soil sources of Si, Ca, Fe, or Ti. For instance, residential wood combustion is a major source of all four elements, on-road vehicle exhaust is a major source of Si, Ca, Fe, and surface coating operations are a major source of Ti (Reff et al., 2009). In urban areas where such sources may dominate, Eq. (7) would overestimate total soil mass and might yield an erroneously low value of \( \beta_{\text{soil}} \). The other 5 problematic multiyear regressions have low \( \beta_{\text{soil}} \) values, for which the cause is unclear. We are nevertheless able to extract high-confidence values of \( \beta_{\text{OC}} \) at these sites by using the multiyear \( \beta_{\text{soil}} \) value in our quarter-specific regressions.

In total, 61 quarter-specific regressions (10%) have at least one physically unreasonable coefficient (see Supplement Table S7). The number of regressions with problematic coefficients is greatest in quarter 1 (\( n = 21 \)) and quarter 3 (\( n = 22 \)) and least in quarters 2 and 4 (\( n = 13 \) and \( n = 5 \) respectively). Problematic \( \beta_{\text{soil}} \) values from the multiyear regressions account for 8 of these (2 in each quarter).

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Overall, 90% of our quarter-specific regressions yield physically reasonable coefficients for all explanatory variables. This leaves 511 high-confidence regressions (see Fig. 1) from which we can assess spatial and seasonal trends.
red in the southwestern US and lower values (green and blue) in much of the Midwest. Both of these are consistent with the calculated \( \beta_{\text{soil}} \) values for different soil types (Simon et al., 2010). They report \( \beta_{\text{soil}} \) values for desert soil between 1.25 and 1.4 and \( \beta_{\text{soil}} \) values for agricultural soil between 0.78 and 1.10.

In order to evaluate spatial and temporal trends for \( \beta_{\text{sulf}} \) and \( \beta_{\text{nit}} \), regression results are grouped by region, matching the organizations designated by the EPA to address regional haze (EPA, 2010). Hereafter, states included in WRAP, CENRAP, LADCO, MANE-VU, and VISTAS will be referred to as the western, central, great lakes, northeast, and southeast regions, respectively.

Maps of \( \beta_{\text{sulf}} \) during each quarter are given in the Supplement (Figs. S6–S9). Figure 9 shows a summary of \( \beta_{\text{sulf}} \) values from 593 quarter-specific regressions. Apart from the western region, \( \beta_{\text{sulf}} \) follows a seasonal trend in which values are lowest in the winter (median values in the central, southeast, great lakes, and northeast regions are 0.90, 0.92, 0.91, and 0.88, respectively) and highest in the summer (corresponding medians are 1.05, 1.04, 1.09, and 1.09). The median wintertime values less than 1 suggest that sulfate is not fully neutralized by ammonium in quarter 1. The summertime values greater than 1 suggest wet sulfate. Further analysis presented in the Supplement Sect. S2 suggests that the trends in Fig. 9 (excluding the western region) are reasonably explained by the seasonal variation in laboratory RH where samples were weighed and by the degree of sulfate neutralization.

Quarter-specific maps of \( \beta_{\text{nit}} \) are given in the Supplement (Figs. S10–S13). Figure 10 summarizes the temporal and spatial trends. In general, \( \beta_{\text{nit}} \) values are lower (i.e. higher percentages of nitrate is volatilized from the Teflon filter) in locations and seasons where temperature is higher. For example, the southeast is warmer, on average, than the rest of the country throughout the year. Median \( \beta_{\text{nit}} \) in this region are lower than all other regions in every quarter. Similarly, summer \( \beta_{\text{nit}} \) values are lower than winter values in all regions. In addition, regions which experience the most dramatic seasonal temperature variations (central, great lakes, and northeast) have the most dramatic variation in median \( \beta_{\text{nit}} \) values. Finally we posit that any site whose \( \beta_{\text{nit}} \) value is within 1.5 standard deviations of 0 is prone to total nitrate volatilization. The number of sites falling into this category increase from 6 in the winter to 71 in the summer, again showing that more nitrate volatilizes in warmer months. Since nitrate volatilization is governed by the temperature-dependent nitrate equilibrium (Hering and Cass, 1999), this behavior is expected. Figure 10 also exhibits a broad variability among \( \beta_{\text{nit}} \) values in quarter 3 which may be due, in part, to low nitrate concentrations. This large variation coupled with the large standard error for \( \beta_{\text{nit}} \) in quarter 3 (median = 0.34, versus 0.06, 0.16, and 0.08 in other quarters) indicate that the regression model is not precisely estimating \( \beta_{\text{nit}} \) in the summer months, though the seasonal variations in \( \beta_{\text{nit}} \) are believable.

3.3 OM/OC results

Our analyses of spatial and temporal trends in \( \beta_{\text{sulf}}, \beta_{\text{nit}}, \) and \( \beta_{\text{soil}} \) show that they mostly can be explained by known aerosol properties and sampling artifacts. Those results build
confidence in our estimates of the OM/OC ratio, $\beta_{OC}$. Table 2 summarizes the distribution of $\beta_{OC}$ values across all regions for all quarters. Table 2 and Fig. 11a show that wintertime OM/OC ratios are generally higher in the eastern US than the West. Median $\beta_{OC}$ values during quarter 1 in the great lakes, southeast, and northeast regions are 1.58, 1.64, and 1.51 respectively while the west and central regions exhibit 1.29 and 1.32 respectively. Higher OM/OC ratios in the eastern US may be a result of high residential wood smoke emissions (see Fig. S10f of Reff et al., 2009). In addition, high values in the southeast may be due to SOA, which is more abundant in this region than in other US regions during winter months (Yu et al., 2007). Figure 11b suggests that OM/OC ratios in the summer do not vary substantially by region; median $\beta_{OC}$ values are 1.80, 1.81, 1.93, 1.87, and 1.81 in the west, central, great lakes, southeast, and northeast regions, respectively. The range of $\beta_{OC}$ values within regions is also quite consistent across the US during quarter 3 (see Table 2). Maps of $\beta_{OC}$ during quarters 2 and 4 are given in the Supplement Fig. S14.

Seasonal variations in $\beta_{OC}$ can also be seen in Fig. 12, which shows $\beta_{OC}$ values are generally higher during summer than in winter. This is consistent with higher SOA concentrations in the summer and more aging of primary OC due to higher oxidant concentrations than in winter. Although this seasonal trend is seen at the vast majority of IMPROVE sites, it is important to note that local conditions have caused higher wintertime $\beta_{OC}$ values in a small number of locations. Regressions at only 12 sites yield higher $\beta_{OC}$ values in quarter 1 than 3 (out of 146 available pairs). While the winter medians are low, $\beta_{OC}$ is more variable than in other seasons: in quarter 1, 90% of $\beta_{OC}$ values fall between 0.79 and 1.84; in quarter 3, 90% fall between 1.44 and 2.08.

As mentioned in Sect. 2.2, $\beta_{OC}$ is influenced by differences in the OC sampling artifacts on quartz versus Teflon filters. Whereas the literature is inconclusive regarding negative artifacts, quartz filters are more prone to positive artifact than Teflon filters. The IMPROVE data include a network-wide and month-specific correction for positive OC artifact on the quartz filter, but no correction for the Teflon filter. We evaluate the effects of site-to-site variability in positive OC artifact (quartz filter) on our regression results (see Supplement Sect. S3) and conclude that the network-wide artifact correction does not substantially affect our estimates of $\beta_{OC}$. However, the $\beta_{OC}$ value could be skewed if (1) IMPROVE’s back-up filter method does not completely capture all positive artifact on quartz filters, (2) Teflon filters have non-negligible positive artifact, or (3) the magnitude of negative artifact differs on the quartz and Teflon filters. An in-depth exploration of OC artifact is beyond the scope of this paper, but these uncertainties should be kept in mind when interpreting our regression results.

Our low wintertime $\beta_{OC}$ estimates in the west and central regions (medians near 1.3) suggest an aerosol dominated by fresh, mobile-source emissions. Although oxidative aging and SOA formation are limited in these regions during winter, the US National Emissions Inventory indicates that other PM sources (e.g., wood smoke) increase $\beta_{OC}$ to 1.5 or 1.6. Our low $\beta_{OC}$ results may be a consequence of systematic biases in the reported measurement uncertainty, which the EiV
Table 2. Summary of $\beta_{OC}$ distributions across sites within quarter and region.

<table>
<thead>
<tr>
<th>Region</th>
<th>Quarter</th>
<th>5th percentile</th>
<th>25th percentile</th>
<th>50th percentile</th>
<th>75th percentile</th>
<th>95th percentile</th>
<th>Number of regressions</th>
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<td>1.69</td>
<td>1.83</td>
<td>1.94</td>
<td>2.15</td>
<td>148</td>
</tr>
<tr>
<td>all</td>
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<td>1.44</td>
<td>1.72</td>
<td>1.81</td>
<td>1.91</td>
<td>2.08</td>
<td>146</td>
</tr>
<tr>
<td>all</td>
<td>4</td>
<td>1.24</td>
<td>1.44</td>
<td>1.59</td>
<td>1.68</td>
<td>1.87</td>
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</tr>
<tr>
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<td>all</td>
<td>1.10</td>
<td>1.44</td>
<td>1.66</td>
<td>1.83</td>
<td>2.06</td>
<td>593</td>
</tr>
</tbody>
</table>

regression is dependent upon (see Sect. 2.3). Another possibility is that our low $\beta_{OC}$ results are somehow tied to the high wintertime $\beta_{sulf}$ values in the western region, which we are unable to explain (see Sect. 3.2).

3.4 Differences with previous regression estimates of OM/OC

Differences between our methodology and that used by Malm and Hand (2007), referred to hereafter as MH07, are summarized in Table 3. A major difference is that we emphasize seasonal $\beta_{OC}$ values, whereas MH07 focused on multiyear regression results. Beyond that, it is interesting to explore which of our subtle revisions to the MH07 methodology cause substantial changes in $\beta_{OC}$. Figure 13 compares $\beta_{OC}$ results from our multiyear regressions (Supplement Table S2) with the MH07 results. Our $\beta_{OC}$ estimates at 37% of sites differ from MH07 by more than 0.2, and 61% differ by more than 0.1. Within each region, our $\beta_{OC}$ estimates exhibit less site-to-site variability than MH07. For example, our low $\beta_{OC}$ values in the great lakes and southeast regions (5th percentile = 1.7 and 1.5, respectively) are higher than MH07 (1.4 and 1.3) despite similar medians. In addition, 95th percentile $\beta_{OC}$ values in the west and central regions are lower in our multiyear regressions (1.9) than in MH07 (2.1).

To isolate the main cause of these different $\beta_{OC}$ results, we perform a series of regressions, beginning with the approach of MH07, that incrementally incorporates each methodological revision listed in Table 3. The three parameters which have the largest effect on $\beta_{OC}$ are the dataset download date, the years analyzed (i.e. 1988–2003 vs. 2002–2008), and the choice of explanatory variables (i.e. differences between Eqs. 4 and 5). The use of EiV rather than OLS affects $\beta_{OC}$ to a smaller degree. Using S instead of $SO_2^-$ to calculate ammonium sulfate and Eq. (7) instead of Eq. (2) to compute SOIL has almost no effect on the $\beta_{OC}$ estimates. The download dates are important because the IMPROVE data archive is updated whenever errors are found. For example, historic chlorine data were adjusted in November 2009 because the original blank correction was deemed too low (White, 2009b). The large effect of the years analyzed may indicate a long-term trend in $\beta_{OC}$ (about 64% of the sites have higher $\beta_{OC}$ values when using 2002–2008 data than when using 1988–2003 data), or result from changes to measurement protocols and hardware which occurred during these time periods. Taken together, the effects of download date
Table 3. Differences between our regression methodology and that of Malm and Hand (2007).

<table>
<thead>
<tr>
<th>Methodological Aspect</th>
<th>Malm and Hand (2007)</th>
<th>This work</th>
</tr>
</thead>
<tbody>
<tr>
<td>IMPROVE dataset</td>
<td>Download date: 3 Dec 2004</td>
<td>Download date: 6 Jan 2010</td>
</tr>
<tr>
<td>Data segregated by</td>
<td>Monitoring site</td>
<td>Monitoring site for $\beta_{\text{SOIL}}$ Monitoring site and quarter for all other coefficients</td>
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<td>Regression type</td>
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<td>Errors-in-variables</td>
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<td>PM$_{2.5}$ – (1.2KNON + 1.8Cl$^{-}$ + EC)</td>
</tr>
<tr>
<td>Intercept ($\beta_0$)</td>
<td>Included</td>
<td>Excluded</td>
</tr>
<tr>
<td>Explanatory variables</td>
<td>($\text{NH}_4$)$_2\text{SO}_4$, $\text{NH}_4\text{NO}_3$, OC, EC, SOIL, sea salt*</td>
<td>($\text{NH}_4$)$_2\text{SO}_4$, $\text{NH}_4\text{NO}_3$, OC, SOIL</td>
</tr>
<tr>
<td>Calculation of explanatory variables</td>
<td>($\text{NH}_4$)$_2\text{SO}_4 = 1.37 \times \text{SO}_4^{2-}$</td>
<td>($\text{NH}_4$)$_2\text{SO}_4 = 4.125 \times S$</td>
</tr>
<tr>
<td></td>
<td>($\text{SO}_4^{2-}$ measured by ion chromatography)</td>
<td>(S measured by XRF)</td>
</tr>
<tr>
<td></td>
<td>SOIL from Eq. (2)</td>
<td>SOIL from Eq. (7)</td>
</tr>
</tbody>
</table>

* Note: Malm and Hand (2007) did not use sea salt as an explanatory variable at sites with few available Cl$^{-}$ measurements: ADPI1, AGTI1, ARENI1, BALD1, BOAF1, BRLA1, CACR1, CADH1, CAPI1, CEHI1, ChER1, CHOL1, COHU1, CRES1, CRM01, DVA1, DOM1, ELDO1, ELL1, FOPE1, GAMO1, GGRU1, HALE1, HEG1, HOO1, IKBA1, JARI1, JOS1, LASU1, LIGO1, LIVO1, LOST1, MACA1, MELA1, MING1, MKGO1, MOM1, MONT1, NEBR1, NOCH1, PMRF1, QUCH1, QURE1, QUA1, SAFO1, SAGA1, SAGU1, SAMI1, SAPE1, SENE1, SHRO1, SIK1, SIP1, SPDK1, SWAN1, TALL1, THBA1, THRO1, ULBE1, WHRI1, WICA1, WIMO1, ZION1.

Fig. 13. Comparisons of $\beta_{\text{OC}}$ values reported by Malm and Hand (2007) to multiyear $\beta_{\text{OC}}$ values from this work.

and years analyzed indicate a sensitivity of $\beta_{\text{OC}}$ to changes in the measurements and data processing methodology.

Next, we analyze which specific changes between Eqs. (4) and (5) cause the largest difference in $\beta_{\text{OC}}$ values. We find that accounting for KNON, removing the intercept ($\beta_0$), and fixing the Cl$^{-}$ coefficient to 1.8 have almost no impact on $\beta_{\text{OC}}$. However, fixing the EC coefficient to 1 changes $\beta_{\text{OC}}$ by more than 0.2 at 15% of the sites. We attribute this sensitivity to the fact that EC and OC are highly collinear in the IMPROVE data ($|r_P|$ exceeds 0.85 and 0.65 at 20% and 88% of sites, respectively). These high correlations between covariates imply that inclusion of EC as an explanatory variable will likely attribute some EC mass to $\beta_{\text{OC}}$ or some OM to $\beta_{\text{EC}}$. In the Supplement (Sect. S3), we investigate our assumption of $\beta_{\text{EC}} = 1$ and find that it has little impact on our $\beta_{\text{OC}}$ estimates. However, we also find that MH07 grossly underestimated $\beta_{\text{OC}}$ at about 1/4 of the IMPROVE sites due to unrealistically large values of $\beta_{\text{EC}}$. This helps explain why our 5th percentile $\beta_{\text{OC}}$ values are higher than MH07.

4 Summary and future work

This work has helped to develop a robust technique for estimating OM/OC ratios that can be applied to an expansive dataset, such as the IMPROVE monitoring network data. Our ability to estimate physically reasonable spatial and seasonal trends in $\beta_{\text{sulf}}$, $\beta_{\text{Huat}}$, and $\beta_{\text{SOIL}}$ builds confidence in our $\beta_{\text{OC}}$ results. Furthermore, our major methodological improvements include the use of an errors-in-variables regression and the elimination of EC as an explanatory variable. These two changes provide more realistic results and eliminate substantial biases from approximately 1/4 of the regressions performed by Malm and Hand (2007). The reader is cautioned that all of our conclusions about OM/OC ratios rely on quartz
and Teflon filter measurements and, hence, depend on accurate and complete OC artifact corrections on both filter types. Techniques for quantifying these artifacts are still an active area of research. Comparison of our $β_{OC}$ results with other OM/OC estimation methods will be the subject of future work.

In addition, this work has identified future areas of research into the IMPROVE data. First, our analysis shows that sulfate is often not fully neutralized so ammonium measurements will greatly assist future mass closure efforts. Second, nitrate volatilization appears to vary substantially by site and season. A measurement study could be performed to verify the nitrate volatilization estimates made here. In addition, samples could be shipped in refrigerated conditions to prevent nitrate volatilization during transport. At a minimum, these results demonstrate the importance of recording the temperature and RH to which filters are exposed during sampling, transport, and measurement. Most importantly, this work has identified general temporal and spatial trends in OM/OC ratios. We find that summertime OM/OC ratios are larger than wintertime values across the US and that winter values are larger in the eastern US than in the West. Considering this work plus the results of Malm and Hand (2007) and El-Zanan et al. (2005), users of the IMPROVE data should revise the common assumption of a fixed network-wide OM/OC ratio when calculating reconstructed fine mass.

**Supplementary material related to this article is available online at:**

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